

# Alternative to the standard cosmological model

A photograph of a galaxy, likely the Milky Way, showing a bright central core and a dense field of stars against a dark background. The galaxy is oriented diagonally across the frame, with the core at the top center. The stars are numerous and vary in brightness, with some appearing as bright white points and others as smaller, dimmer specks. The overall color palette is dominated by deep blues and blacks, with the warm tones of the galaxy's core providing a focal point.

**B. Famaey (Strasbourg)**

Dark matter in galaxies poses a list of interesting open questions leading to essential information on either

(i) the galaxy formation process,

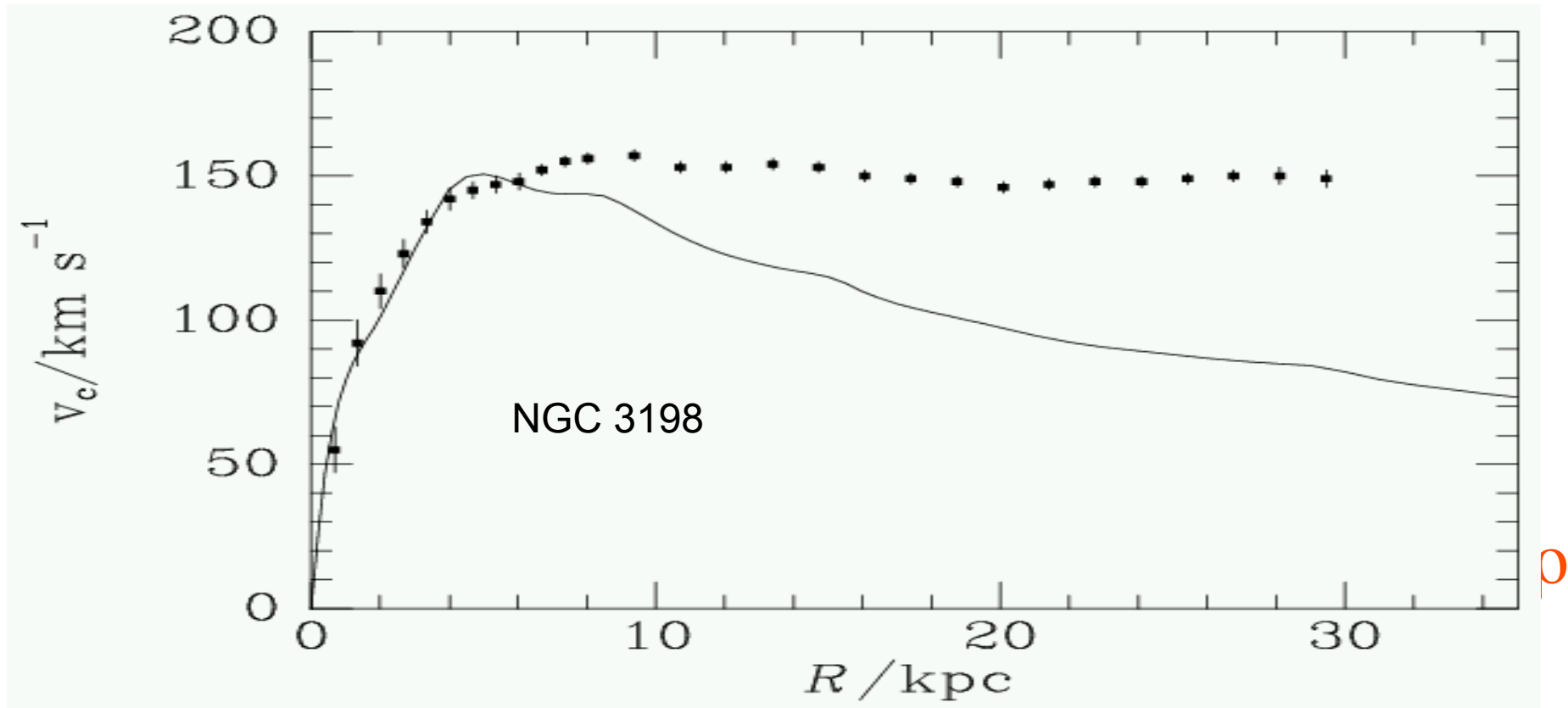
(ii) the very nature of dark matter

or (iii) even on its existence in galaxies

# Plan of the lecture

1. (1h) Introduce 5 observational challenges for the standard picture
2. (1h) More speculative: could some of these challenges point towards an alternative cosmological model?  
Strengths and weaknesses...

# Galactic rotation curves



$(R |\partial\Phi_{\text{bar}}/\partial R|)^{1/2} = V_{c \text{ bar}}$  too low in the galactic plane compared to observed  $V_c$

=> DARK MATTER HALO

# OBSERVATIONS:

Symmetric circular rotation of a disk characterized by:

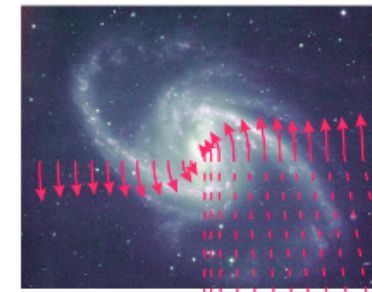
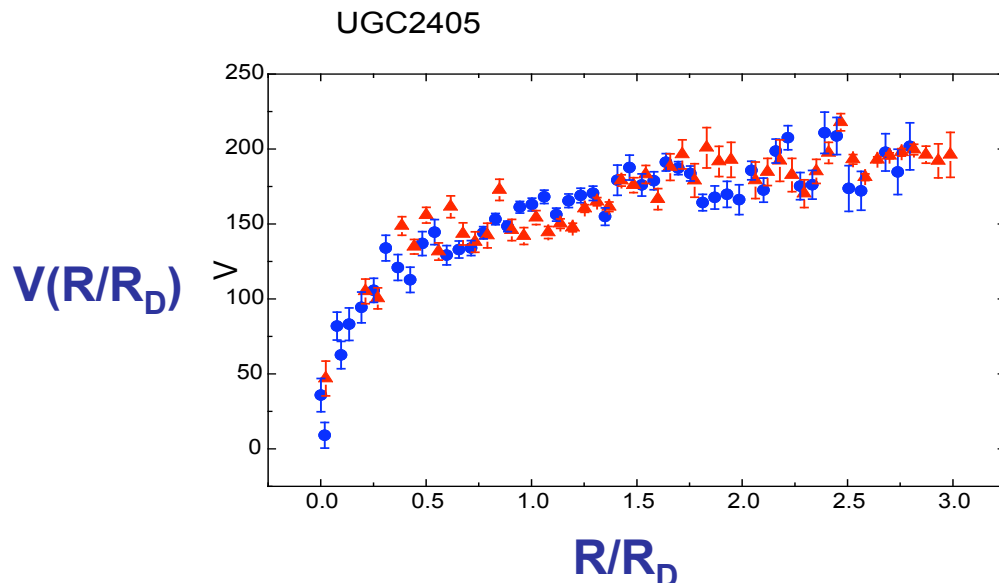
- Sky coordinates of the galaxy centre
- Systemic velocity  $V_{sys}$
- Circular velocity  $V(R)$
- Inclination angle  $i = \arccos\left(\frac{a}{b}\right)$

$$V_{obs}(\xi, \eta) = V_{sys} + V(R) \cos \theta \sin i$$

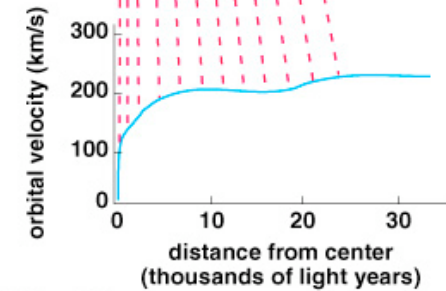
$\theta$  = azimuthal angle

Example of a recent high quality RC:

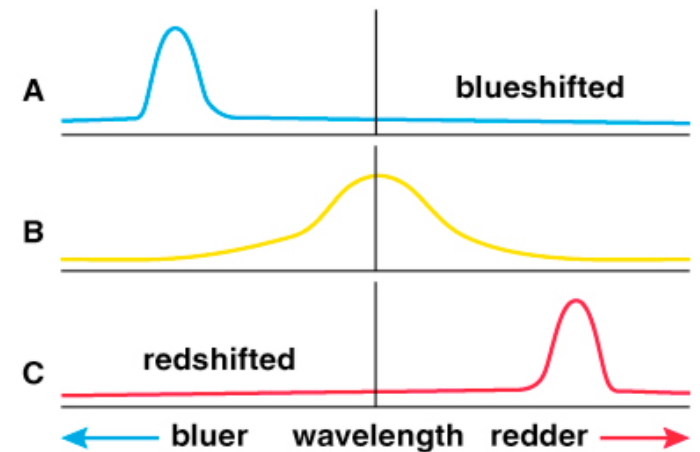
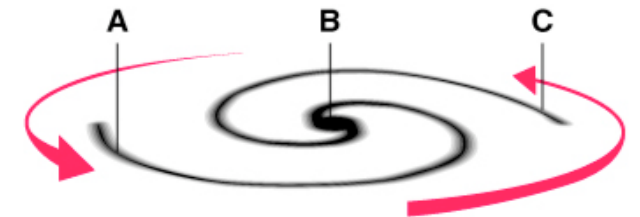
**Radial coordinate in units of  $R_D$**



Longer arrows represent larger orbital velocities.



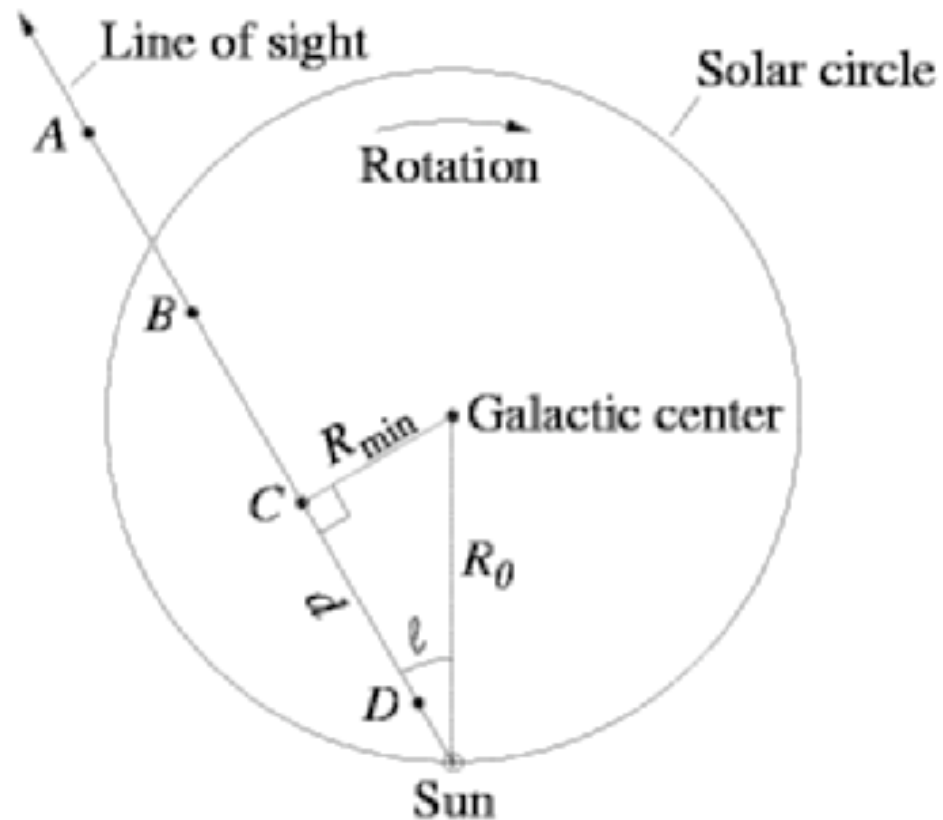
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# The Milky Way

Measure the « Terminal Velocity Curve » (TVC)



$$V_c(R_{min} = R_0 \sin l) = | V_t(l) + V_0 \sin(l) |$$

# Dissipating a misunderstanding

It is often argued that a ring of DM is present around  $R=13\text{kpc}$

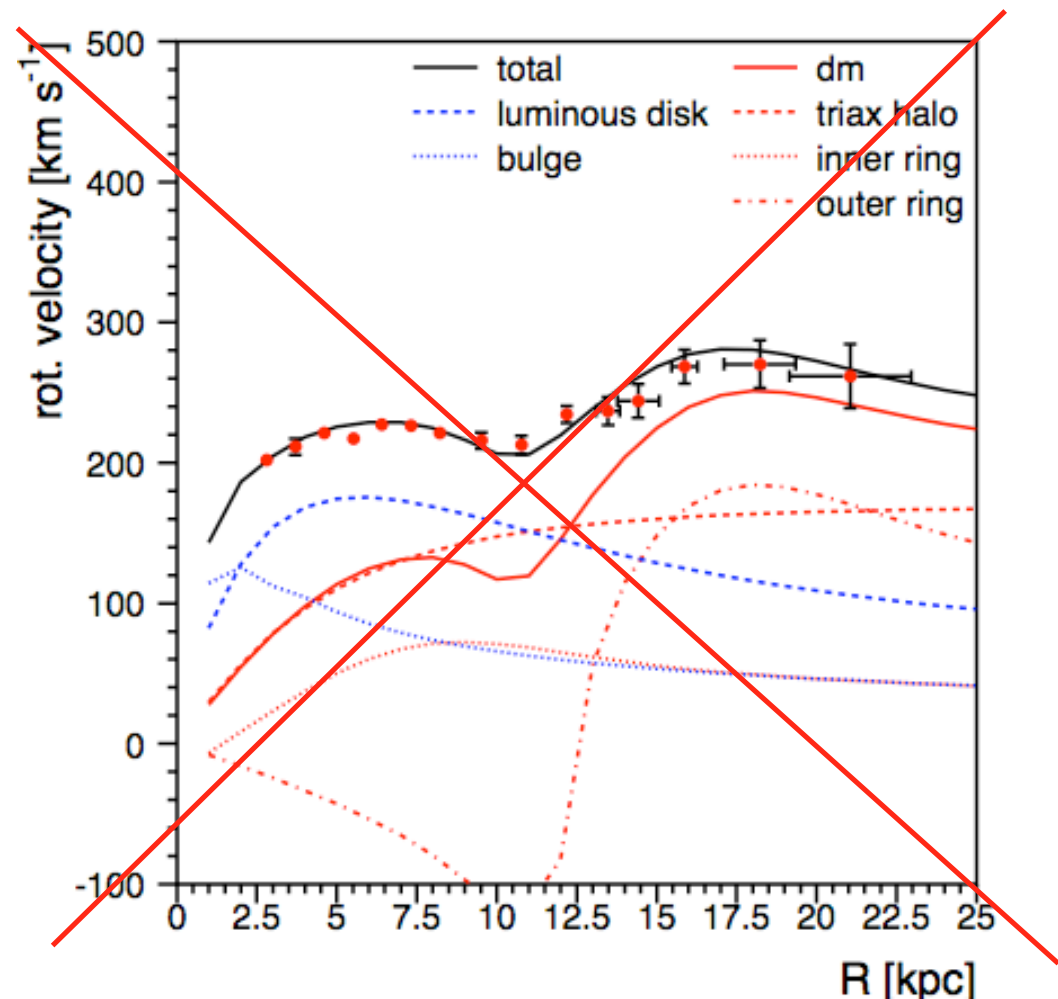
At  $R < R_0$ :

$$V_c(R_0 \sin l) = V_t + V_0 \sin l$$

**BUT** at  $R > R_0$ :

One needs the **distance** of tracers (cepheids P-L relation)

**Binney & Dehnen (1997):**  
data compatible with a gently declining RC if overdensity of TRACERS



Open question 1: the cusp problem

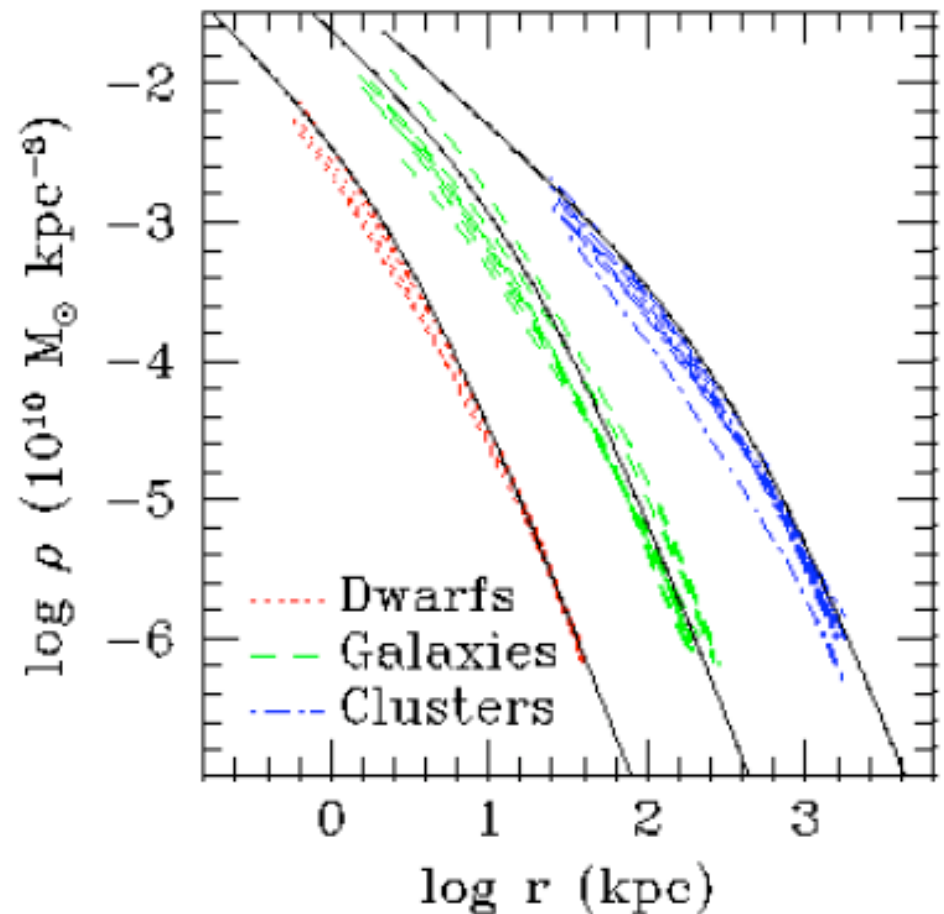


# NFW dark matter Profiles from N-body simulations

In  $\Lambda$ CDM scenario the density profile for virialized DM halos of all masses of all masses is empirically described at all times by the universal NFW formula (Navarro+96,97).

$$\begin{aligned}\rho(r)/\rho_{crit} &\approx \delta r_s / r(1 + r/r_s)^2 \\ &= \rho_s r_s^3 / r(r^2+r_s^2)\end{aligned}$$

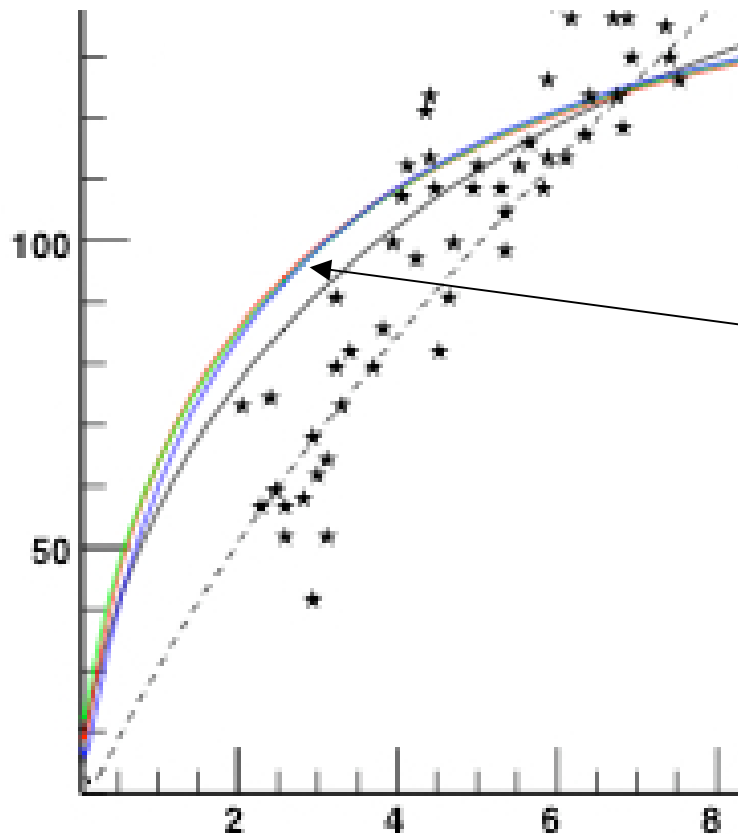
More massive halos  
have larger overdensities  $\delta$ .



# Inner rotation curve of the MW

$$V_c(R_0 \sin l) = V_t + V_0 \sin l$$

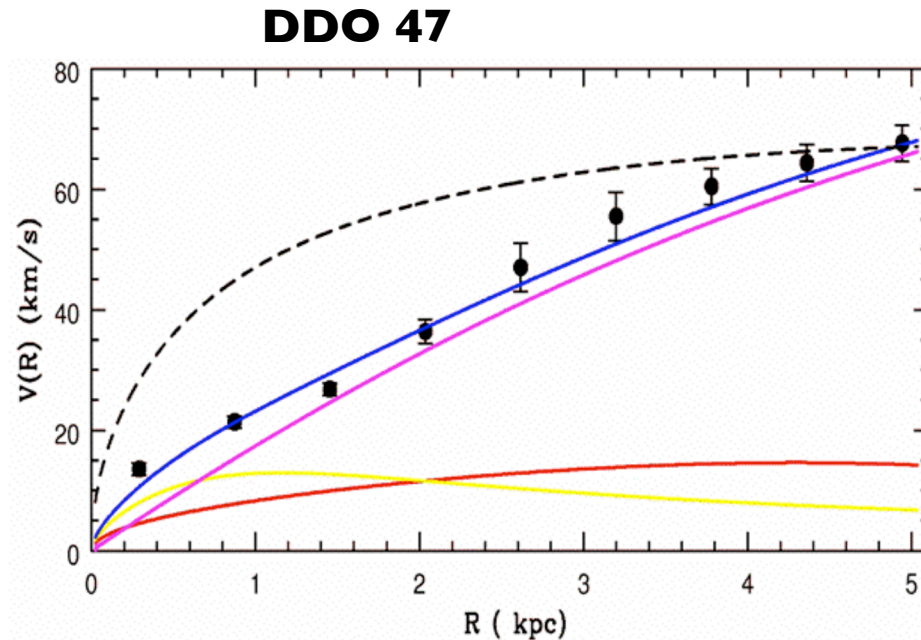
$$V_{\text{cDM}} = (V_c^2 - V_{\text{cbar}}^2)^{1/2}$$



NFW profile  
overpredicts DM  
density at the center

Confirmed by microlensing  
optical depth

In other galaxies too



General results from several samples including THINGS,  
HI survey of uniform and high quality data  
+ microlensing optical depth and gas flow in the MW

- No DM halo elongation
- Cored halos often preferred over NFW

**Tri-axiality and non-circular motions cannot explain the CDM/NFW cusp/core discrepancy. Including feedback from baryons (bar? No...)**

**Governato et al: best attempt but too high baryon fraction**

Aquarius simulations, highest resolutions to date.

Results: Einasto profiles (Navarro et al. 2010)

$$\ln \rho(r) / \rho_{r_2} = -2 / \alpha \left[ (r / r_2)^\alpha - 1 \right]$$

with  $r_2$  determining size and  $\alpha$  dependent slightly on mass  
( $\alpha = \mathbf{0.17}$  for MW-type halo from CDM simulations)

Slope  $d \ln \rho / d \ln r \propto -r^\alpha$  goes from -1.4 at  $r=1$  kpc to -0.8 at  $r=100$  pc

Only fits with  $\alpha \gg \alpha_{sim}$  OK

Open question 2: missing satellites?

# Mass function of luminous satellites

Many new ultra-faint dwarfs have been found (Segue1, Hercules...)

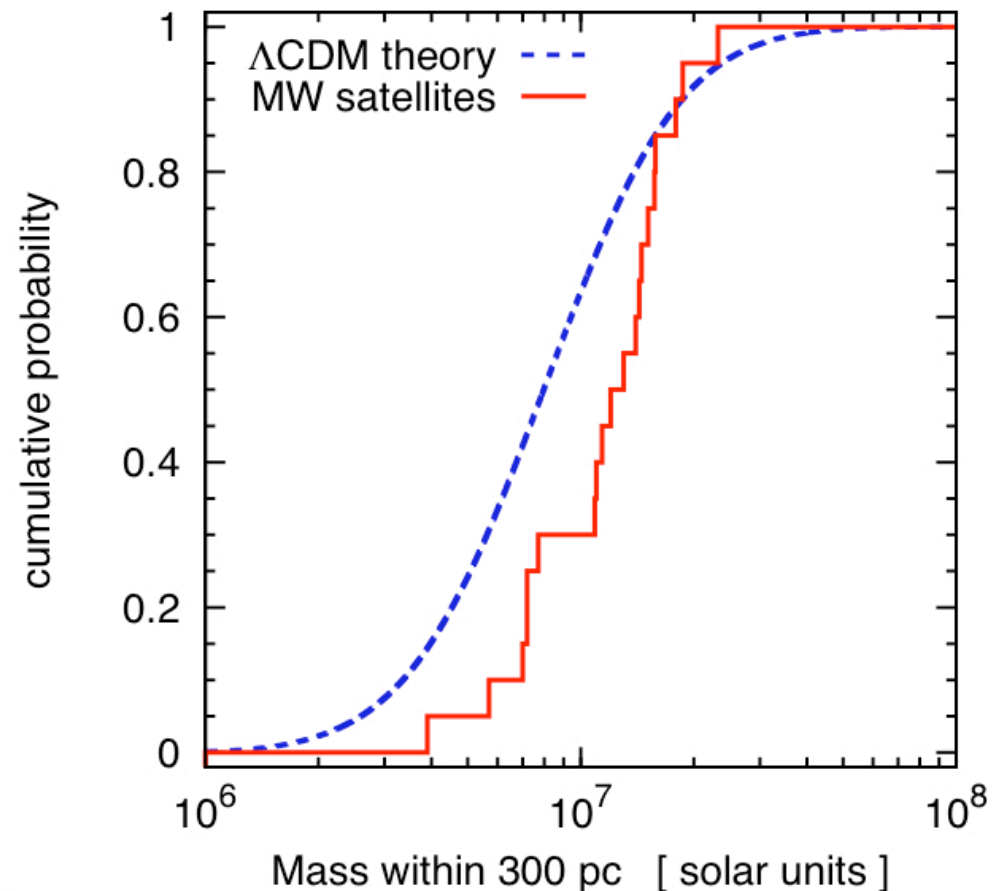
-> Is the missing satellite problem solved?

No: the mass function of **luminous** halos disagrees with the expectations from CDM

$$\xi_{\text{lum}}(M_{\text{vir}}) = k k_i M_{\text{vir}}^{-\alpha_i},$$

with

$$\alpha_1 = 0, \quad k_1 = 1, \quad 10^7 \leq \frac{M_{\text{vir}}}{M_{\odot}} < 10^9,$$
$$\alpha_2 = 1.9, \quad k_2 = k_1 (10^9)^{\alpha_2 - \alpha_1}, \quad 10^9 \leq \frac{M_{\text{vir}}}{M_{\odot}} \leq M_{\text{max}},$$



Kroupa et al. (2010)

Open question 3:  
phase-space correlation of satellites?

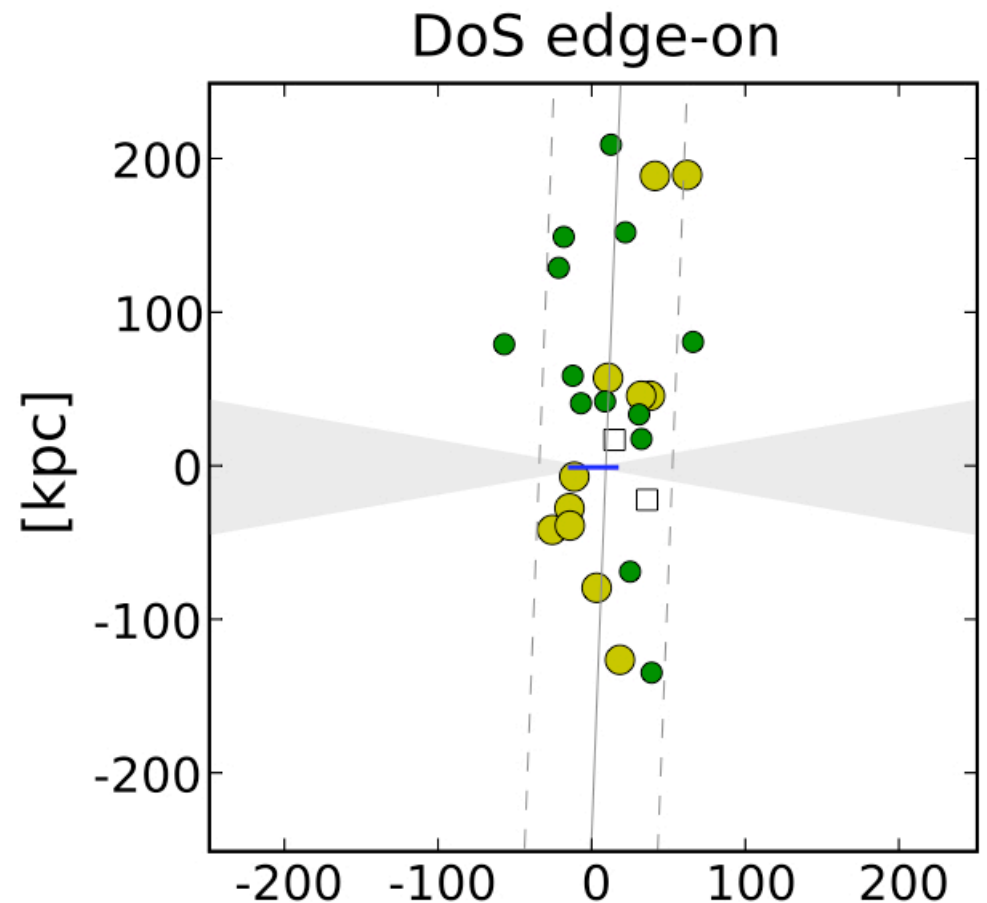
# The Holmberg plane of satellites

Seems not to be found in external galaxies (M31, SDSS) **but** still very much there in the Milky Way!

-> Wait for Pan-Starrs...

-> then, if it remains, what does it mean? Not expected in CDM simulations

-> TDGs ? But where are the primordial DM halos around the MW then?





Open question 4:  
reproducing the local void?

# Distribution of galaxies in the LV

562 galaxies with

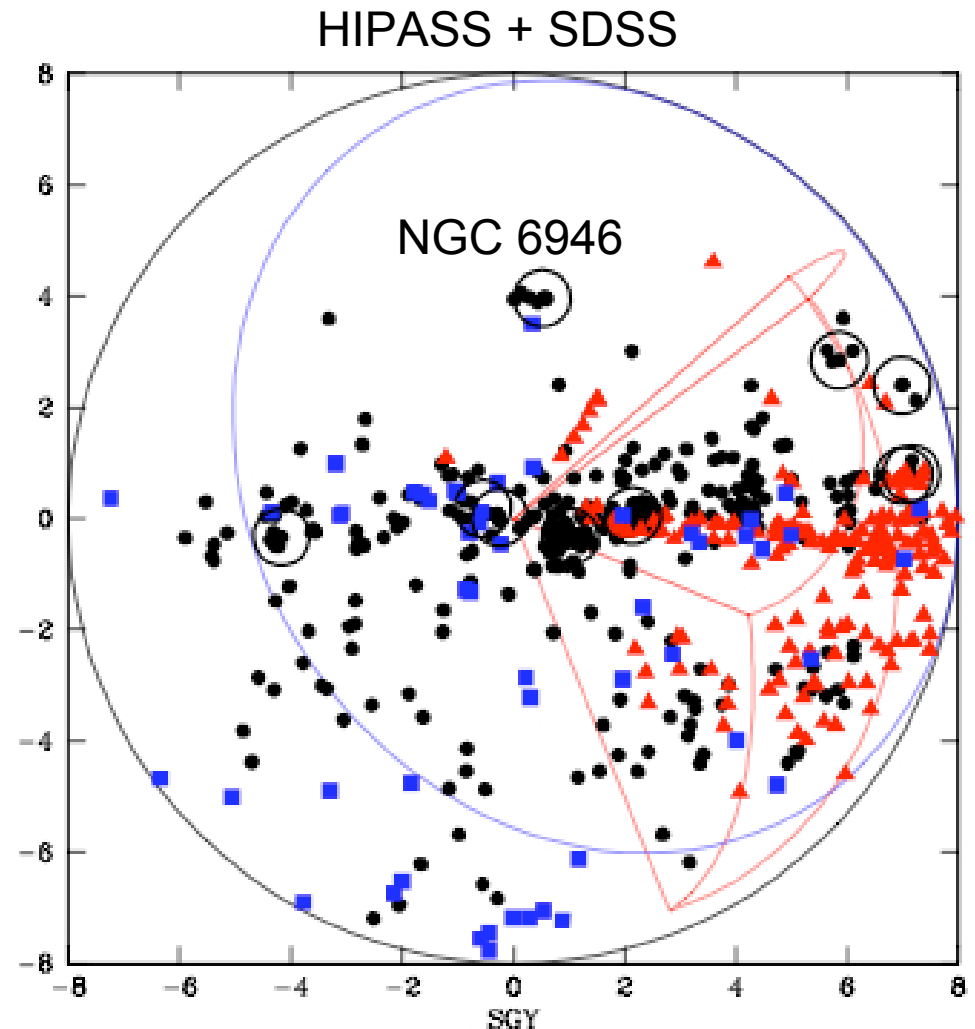
$1\text{Mpc} < d < 8\text{Mpc}$

5% are  $>2\text{Mpc}$  above the local sheet

Among the 10 most luminous ones (circles),

3 are  $>2\text{Mpc}$  above the local sheet

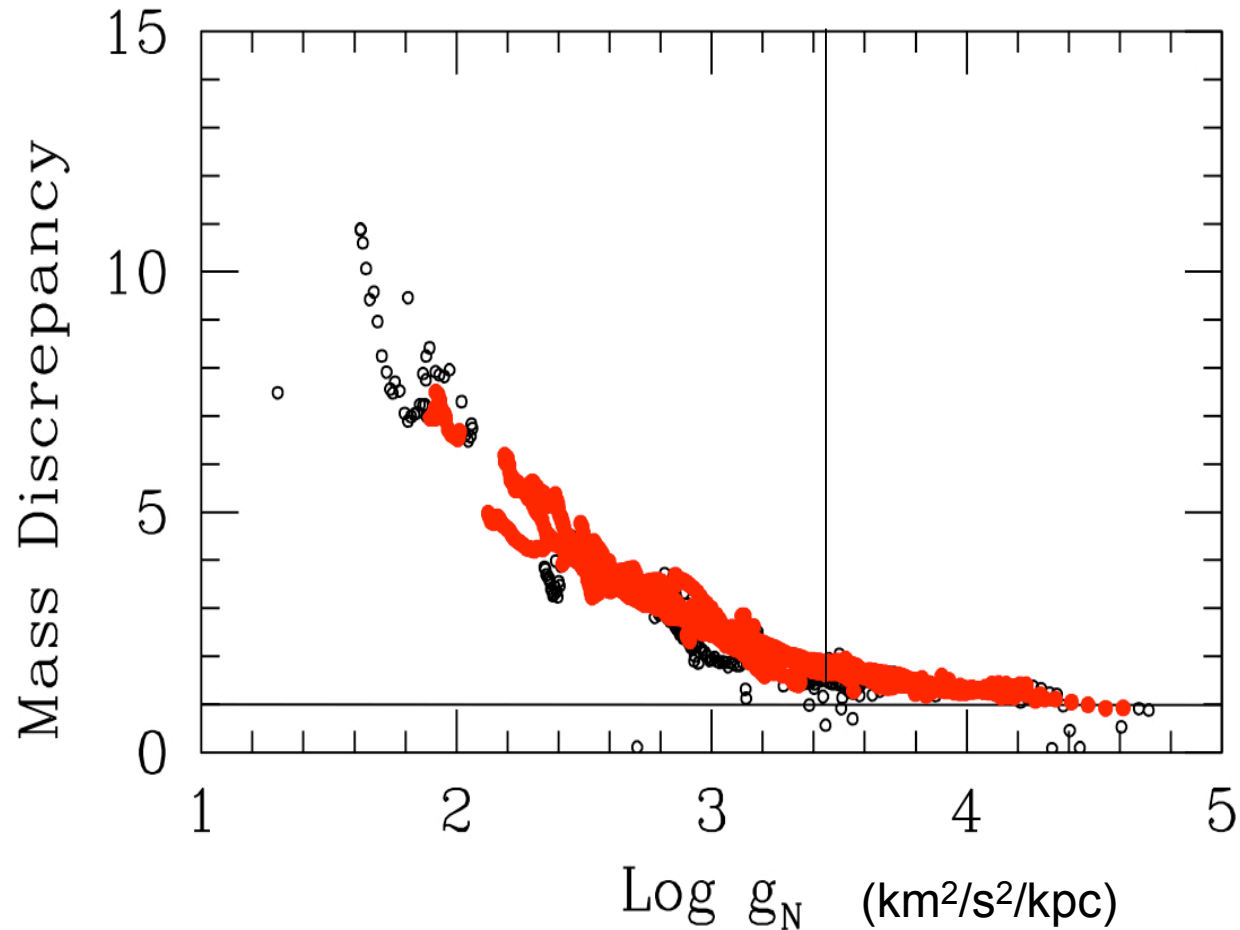
-> too few and too large galaxies in underdense regions (different from missing sat)



Peebles & Nusser (2010)

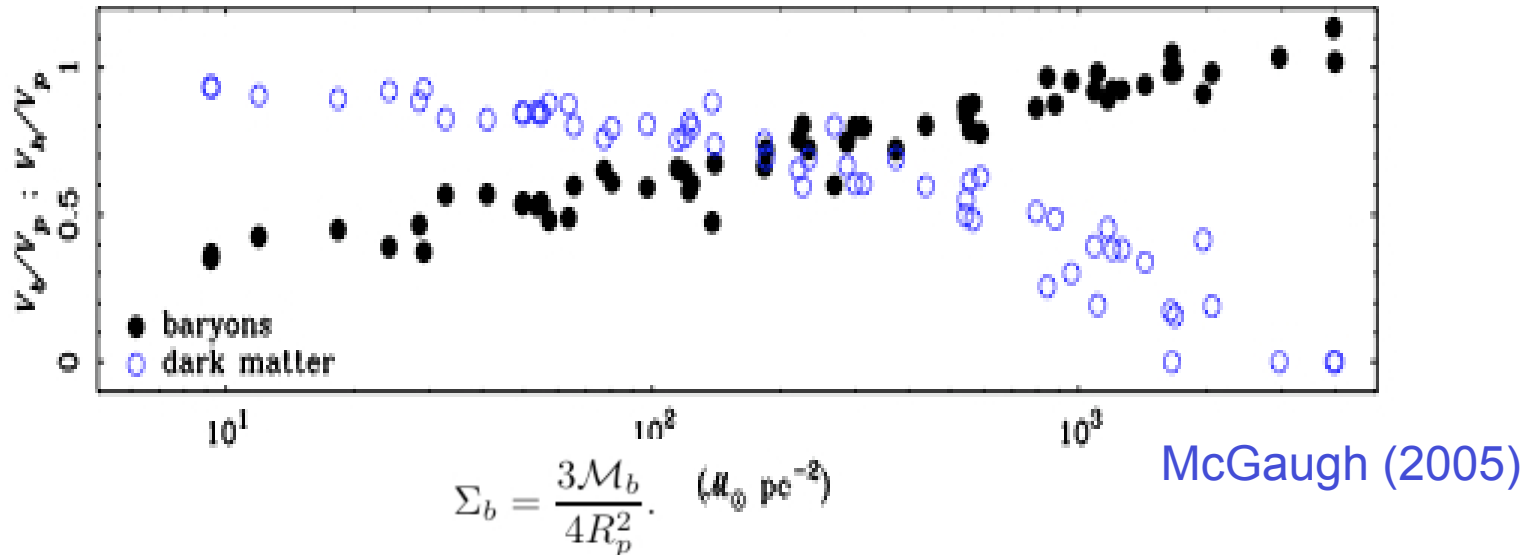
Open question 5:  
reproducing the mass discrepancy-  
acceleration relation?

# Mass Discrepancy vs Acceleration



McGaugh 2004; Gentile, Famaey & de Blok 2010

# A fine balance of DM and baryons



$R_p$  = radius of max contribution of both gas and stars to the RC

Comparing the contribution of baryons to the RC as a function of surface density (proxy for characteristic acceleration)

This could point at some sort of repulsion between surface densities of baryons and DM

**MDA (and this MDsurfdn) is *history-independent* !**

# Asymptotes to Baryonic Tully-Fisher

At small accelerations, the mass discrepancy is

$$\boxed{M_{\text{tot}}/M_{\text{bar}} = a_0/a} \quad \text{where } a_0 \approx 3600 \text{ km}^2/\text{s}^2/\text{kpc}$$

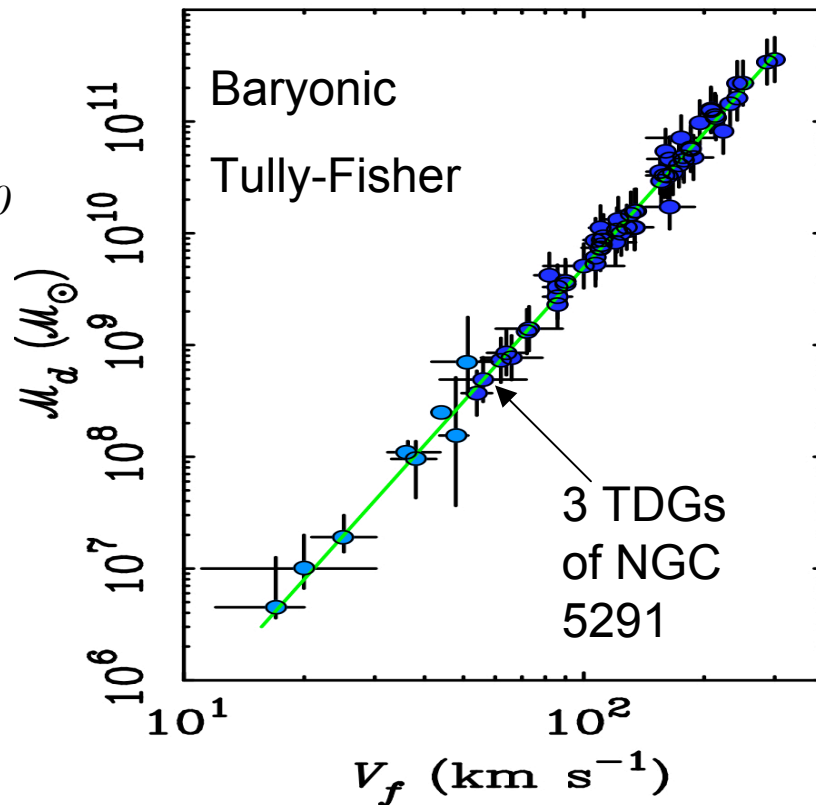
$$V_f^2 = GM_{\text{tot}}/r = GM_{\text{bar}} a_0/(ar) = GM_{\text{bar}} a_0/V_f^2$$

$$V_f^4 \propto M_{\text{bar}}$$

More precisely:

$$\log M_{\text{bar}} = 4 \log V_f - \log G a_0$$

reproduces slope, zero-point,  
and small (zero) scatter



e.g. Trachternach et al. 2009

# The MDA can be summarized by Milgrom's formula

Correlation summarized by this formula in galaxies (Milgrom 1983):

$$\mu (V^2/ra_0) V^2/r = g_{\text{N bar}} \quad \text{where } a_0 \sim cH_0 \sim c\Lambda^{1/2}$$

with  $\mu(x) = x$  for  $x \ll 1 \Rightarrow$  Tully-Fisher slope = 4

$$\mu(x) = 1 \text{ for } x \gg 1$$

This formula fits >2000 galaxy rotation curves data points!

Independent roles of  $a_0$  :

1) Zero-point of the Tully-Fisher relation (observed with small scatter):

$$4 \log V_f = \log M_{\text{bar}} + \log G a_0$$

2) Discrepancy always appear at  $V^2/r \sim a_0 \Rightarrow$  in LSB where  $\Sigma \ll a_0/G$

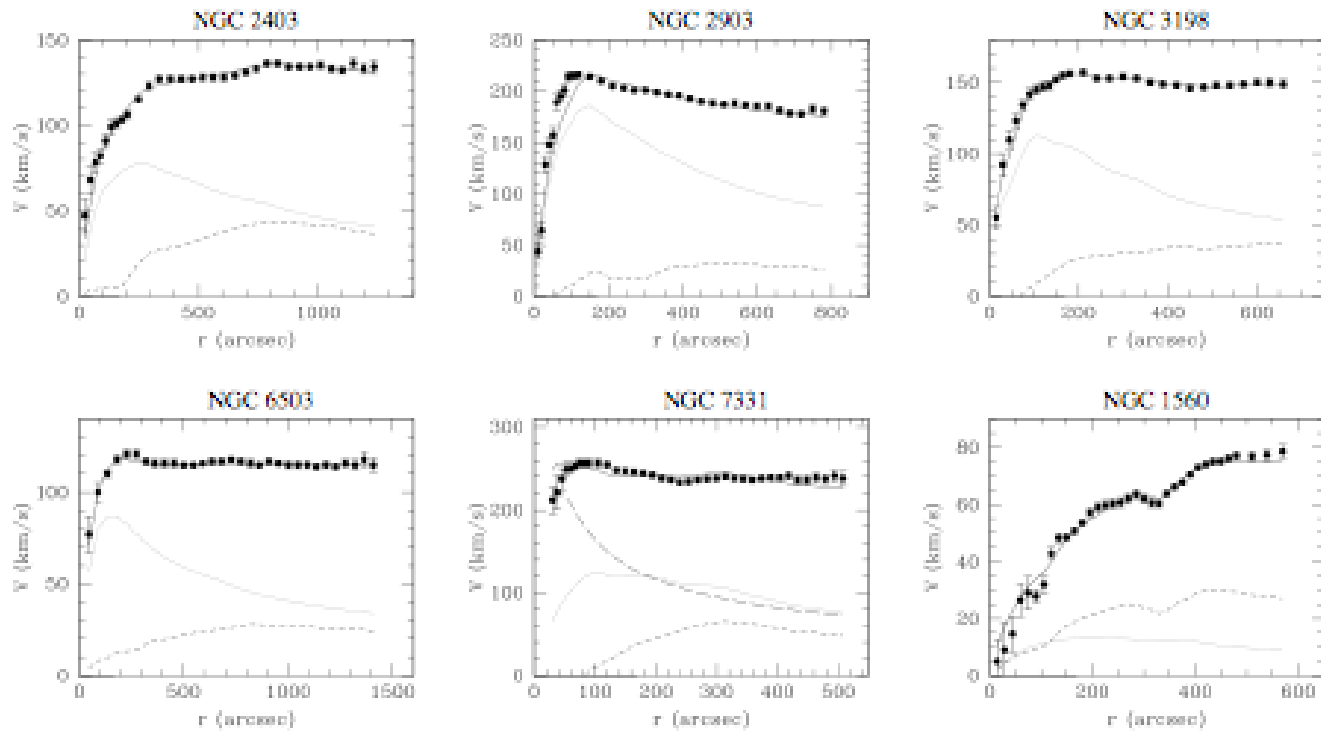
## Corresponding modification of **Newtonian** gravity (MOND):

$$\nabla \cdot [\mu(|\nabla\Phi|/a_0) \nabla\Phi] = 4\pi G \rho_{\text{bar}}$$

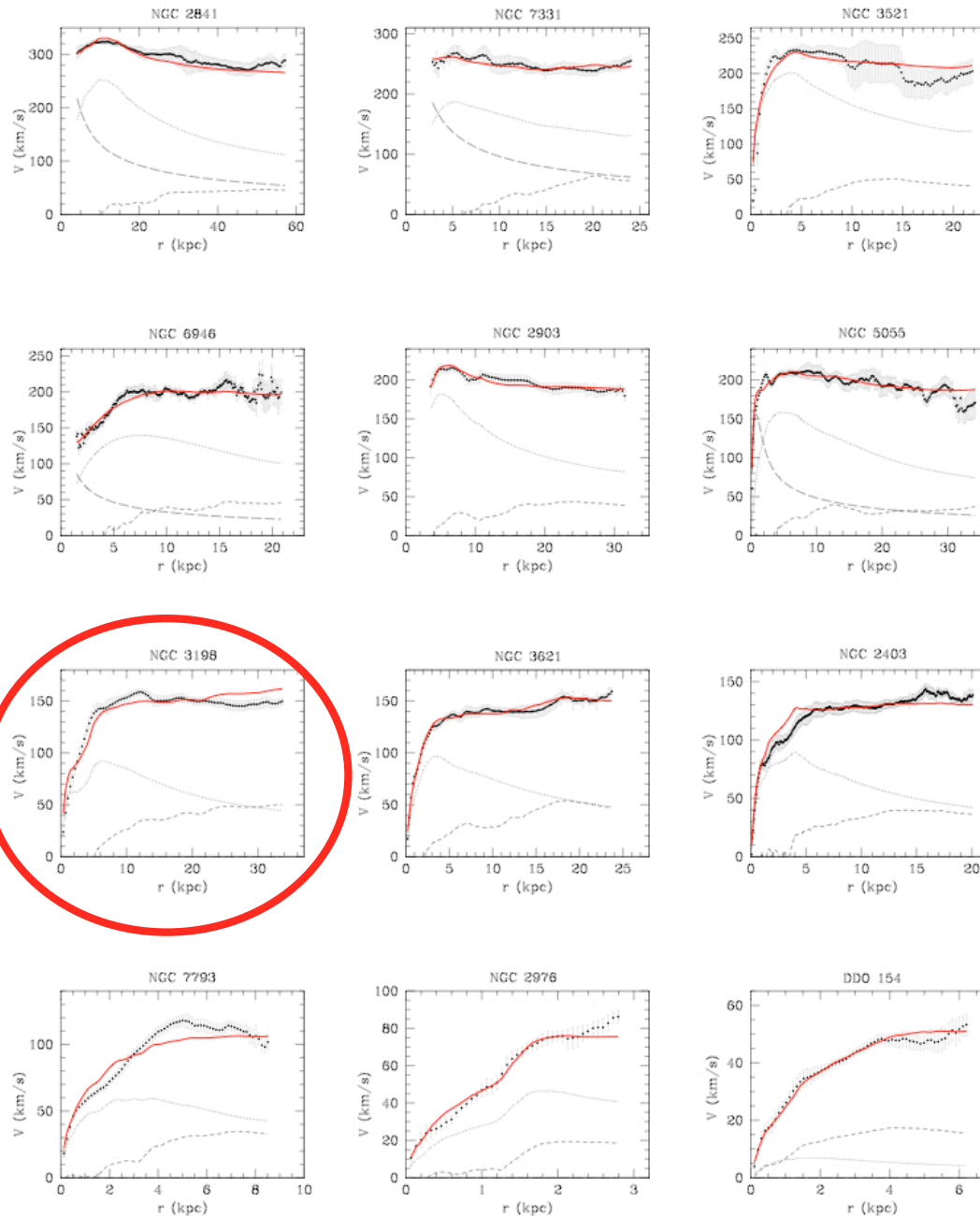
$$\Phi(r) \sim (GMa_0)^{1/2} \ln(r).$$



# MOND

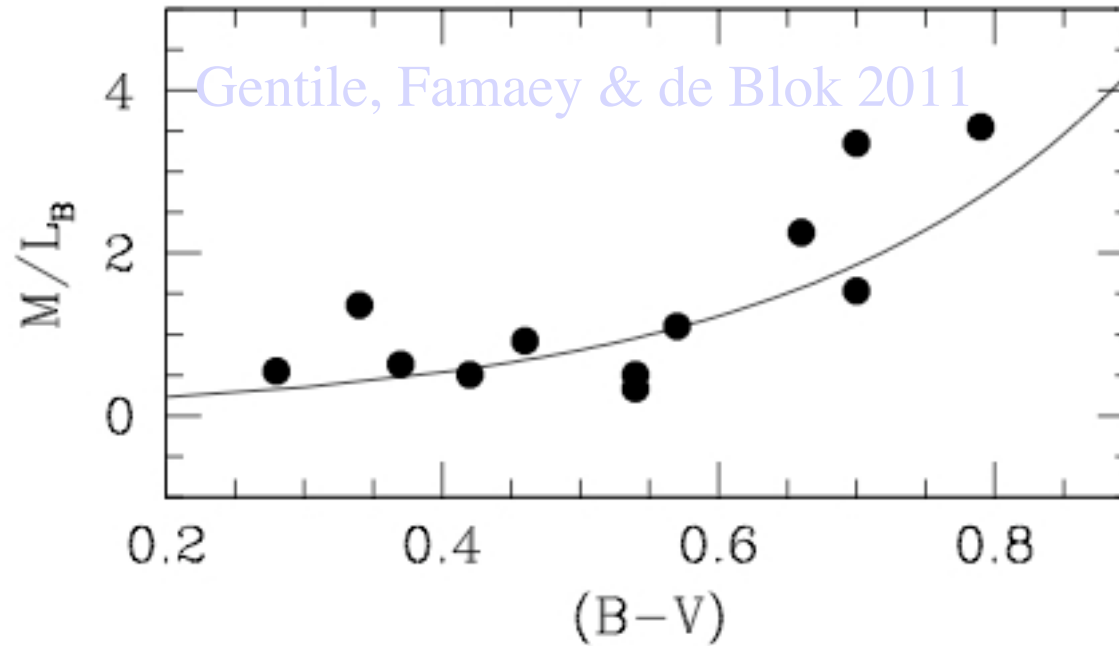


Famaey et al. (2007)



Might indicate a  
smaller  
 $a_0 = 0.9 \times 10^{-8} \text{ cm/s}^2$

THINGS (Gentile, Famaey & de Blok 2011)



M/L follows predictions of population synthesis models

# Non-isolated systems

In reality, **no** isolated systems: the external field in which an object is plunged influences the **internal** dynamics

For instance, Milky Way in the slowly varying Great Attractor gravitational field ( $0.01 a_0$ )

$$\nabla \cdot [ (\mathbf{g} + \mathbf{g}_e) \mu ( |\mathbf{g} + \mathbf{g}_e| / a_0 ) ] = \nabla \cdot ( \mathbf{g}_n + \mathbf{g}_{ne} )$$

In spherical symmetry:

$$\mathbf{g}_n = \mathbf{g} \mu ( |\mathbf{g} + \mathbf{g}_e| / a_0 ) + \mathbf{g}_e [ \mu ( |\mathbf{g} + \mathbf{g}_e| / a_0 ) - \mu ( |\mathbf{g}_e| / a_0 ) ]$$

When  $|\mathbf{g}| \rightarrow 0$  :  $\mathbf{g}_n = \mathbf{g} \mu ( |\mathbf{g}_e| / a_0 )$ ,  $r^{-2}$  force,  $r^{-1}$  potential !

# Escape speed

$$\frac{1}{2}v_{\text{esc}}^2(r) = \Phi(\infty) - \Phi(r)$$

Apply a  $0.01 a_0$  external field to the Milky Way, calculate the escape speed from the solar neighbourhood

->  $v_{\text{esc}} = 545 \text{ km/s}$  as observed !

Famaey, Bruneton & Zhao 2007

Wu et al. 2007

# Does MOND always work?

No: pressure-supported systems can be really problematic!

**Galaxy clusters**: lensing and dynamics require additional dark matter (about as much as baryonic matter, a factor of 10 in the central parts)

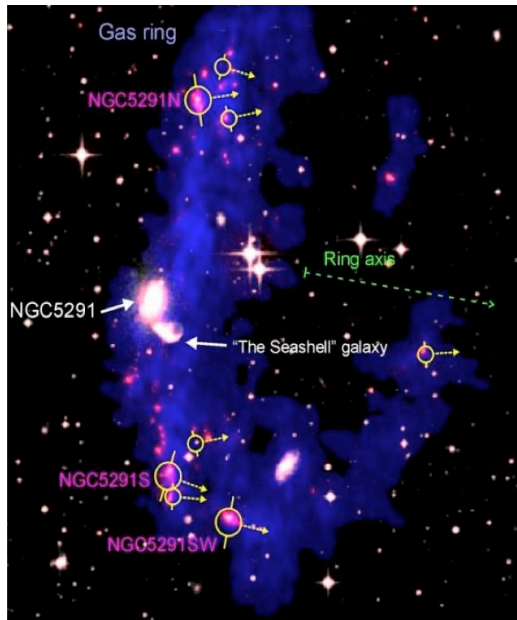
Velocity dispersion profiles and strong lensing of **elliptical galaxies**: generally **ok** in the field, but a few outliers inside groups and clusters

Velocity dispersion profiles of **dwarf spheroidals**: generally **ok** but not (yet) for Sextans and Draco, and stability must be checked. The new ultra-faint dwarfs cannot be in equilibrium (**old TDGs?**)

The total velocity dispersion in the **globular clusters** Pal 14 and Pal 4 (but not Pal 3) might be problematic for MOND (predicts 1 km/s instead of 0.5 km/s observed). But very few stars. NGC 2419 also problematic: orbit of the GC...?

# Two case studies

Rotationally supported gas-dense  
 ( $> 10^{-21} \text{ kg/m}^3$ )



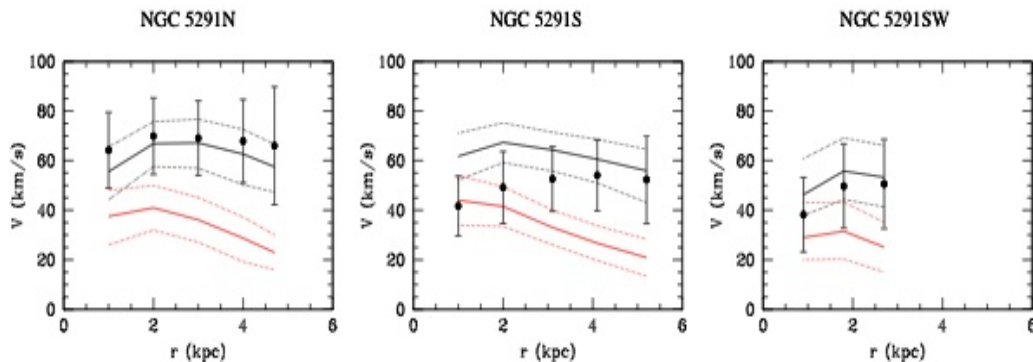
**Tidal dwarf galaxies  
 in NGC 5291**

Bournaud et al. (2007)

Gentile, Famaey et al. (2007)

~~CDM~~

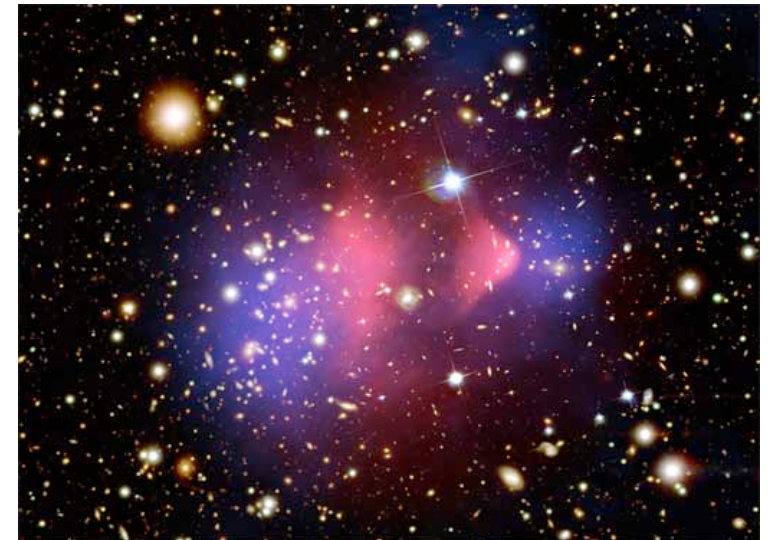
MOND



Pressure-supported not very gas-dense

CDM

~~MOND~~

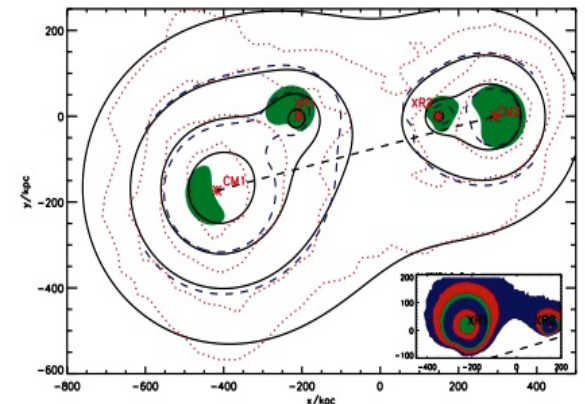


**The Bullet Cluster**

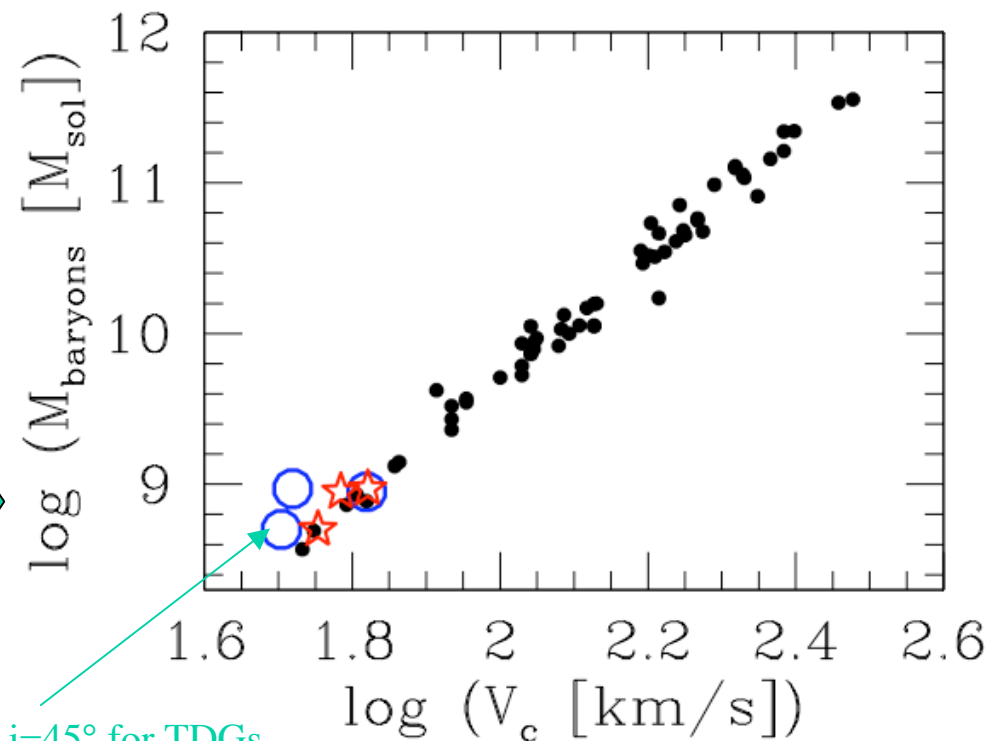
Clowe et al. (2006)

Angus, Shan, Zhao &  
 Famaey (2007)

But speed 4000 km/s?



# TDGs on the Tully-Fisher relation



$i=45^\circ$   
Newton

$i=45^\circ$  for TDGs  
of NGC 5291

Why does the MDA work in CDM  
and BDM galaxies???



# Model-independent statements

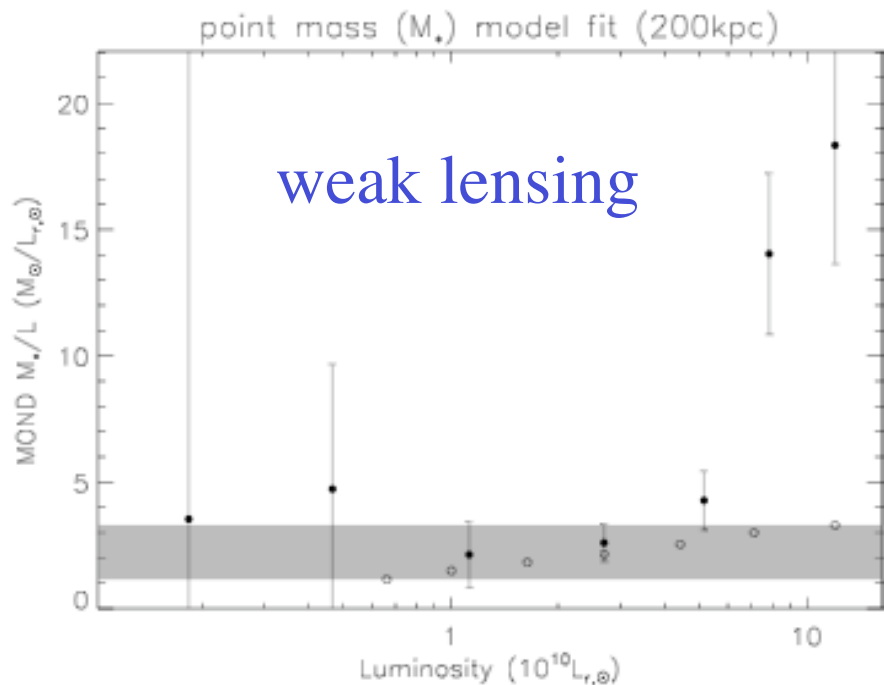
Independently from the theoretical framework, the MOND formula is an extremely efficient way of **predicting the gravitational field in rotationally supported galaxies** (with a relatively high gas density  $> \sim 10^{-21} \text{ kg/m}^3$ )

Any galaxy formation theory should be able to ultimately reproduce the MOND formula (or MDA) as a scaling relation for spirals (and TDGs)

What makes it difficult is that it is **history-independent!**

# Another model-independent statement

The MOND recipe breaks down in **some** pressure-supported systems with a low gas density (**especially in galaxy groups and clusters**)



Something breaks down at a baryonic mass of  $\sim 10^{12} M_{\text{sun}}$

(notice also that the mass is probed at very large radii)

# A modified gravity theory

There exists many relativistic theories reproducing MOND. Here is an example

The difficult thing is to have lensing and dynamics governed by the same potential

In GR, the geodesic equation is:

$$d^2x^\mu / d\tau^2 = - \Gamma^\mu_{\alpha\beta} (dx^\alpha/d\tau) (dx^\beta/d\tau)$$

reducing for timelike geodesics in weak-field to

$$d^2x^k / d\tau^2 = - \Gamma^k_{00} (dx^0/d\tau)^2 = - \Gamma^k_{00}$$

thus depending only on  $g_{00}$  (but not for null geodesics)

# TeVES

Einstein equations relate metric to stress-energy tensor just like Poisson equation relates potential to density. In weak-field:

$$g'_{00} = - e^{2\Phi_N} = - 1 - 2\Phi_N$$
$$g'_{ij} = e^{-2\Phi_N} \delta_{ij} = (1 - 2\Phi_N) \delta_{ij}$$

Idea: replace GR with a theory reducing to the SAME metric but replacing  $\Phi_N$  by  $\Phi$  obeying MOND

Add a scalar field and couple matter to

$$g'_{\alpha\beta} = e^{2\phi} g_{\alpha\beta}$$

... with action of  $\phi$  governed by a free function depending on  $(\text{grad } \phi)^2$ , works for dynamics, but *doesn't work for lensing*

# TeVes

Add a scalar field and a vector field and couple matter to

$$g'_{\alpha\beta} = e^{-2\phi}(g_{\alpha\beta} + U_{\alpha}U_{\beta}) - e^{2\phi}U_{\alpha}U_{\beta}$$

with  $g^{\alpha\beta} U_{\alpha}U_{\beta} = -1$ , timelike in static situations, and action  $S = S_g + S_s + S_v + S_m$ ,

with action  $S_s$  of  $\phi$  governed by a free function depending on  $(\text{grad } \phi)^2$

$\Rightarrow$   $\phi$  **obeys a B-M equation**, and plays the role of the dark matter potential (dynamics and lensing are governed by the **same** physical metric  $g'$ )

# Hot Dark Matter + relativistic MOND?

**Ordinary neutrinos** of 2 eV (experimental model-independent limit) are **not enough** to explain the MOND discrepancy in X-ray emitting groups (too high phase-space density needed)

=> Maybe another fermionic dark **HDM** particle? (hot light sterile neutrinos with  $m_\nu \sim 10\text{eV}$  ?)

=> plays the role of CDM in the early Universe, then MOND-like gravity boosts structure formation (**FASTER STRUCTURE FORMATION HELPS LOCAL VOID**) ... to be investigated until DM is detected directly

=> Maybe **CDM and no MOND**?... but then one must in any case understand why it does reproduce so precisely the **MOND** relation for all galaxies...

**EXCITING TIMES AHEAD**

