

European Summer Campus 2010



"Metamaterials" Strasbourg, France, June 27 – July 5, 2010



Auxetic Metamaterials

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http://www.auxetic.info



Acknowledgements

- Co-workers:
 - Brian Ellul
 - Daphne Attard
 - Ruben Gatt
- \$\$\$\$
 - University of Malta
 - Malta Council for Science & Technology
 - Malta Government Scholarship Scheme
- Organisers of Metamaterials European Summer School



The Maltese Islands

- 126 sq. miles
- ~400,000 people





Golden bay



History





University of Malta ... since 1592

- Founded as Collegium Melitense by Papal Decree in 1592
- Public university since 1768 by Grand Master Pinto de Fonseca





1780



The University now ...

- Msida
- ~10,000 students
- The 'home' of the auxetics group







Siggiewi – My home town



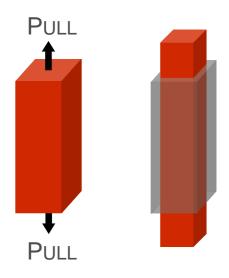
Introduction to auxetics

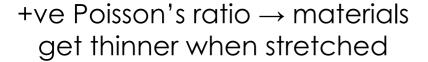


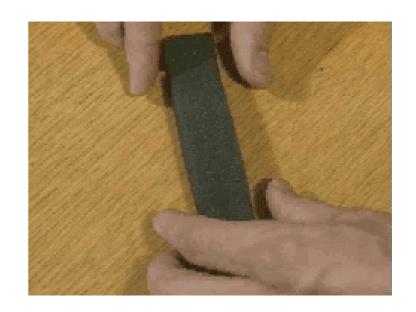
Poisson's ratios

Poisson's ratio,
$$v = -\frac{\text{lateral strain}}{\text{axial strain}}$$

strain =
$$\frac{\text{extension}}{\text{original length}}$$









Common values

Material	Poisson's ratio
Rubbers	0.5
Lead	0.45
Aluminium	0.33
Common steels	0.27
Cellular solids e.g polymer foams	0.1 - 0.4
Cork	0.0



But...

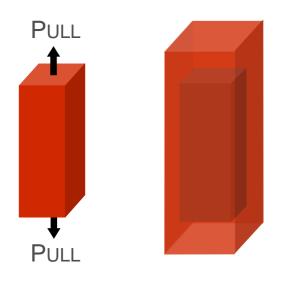
... Poisson's ratios can also be negative

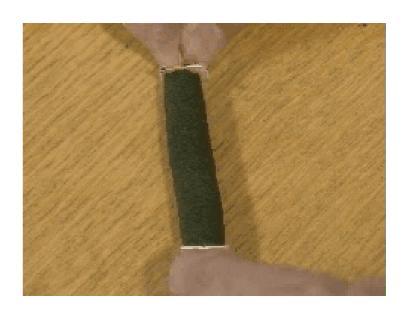
$$-1 \le \nu \le 0.5$$

... from the classical theory of elasticity (for isotropic materials)



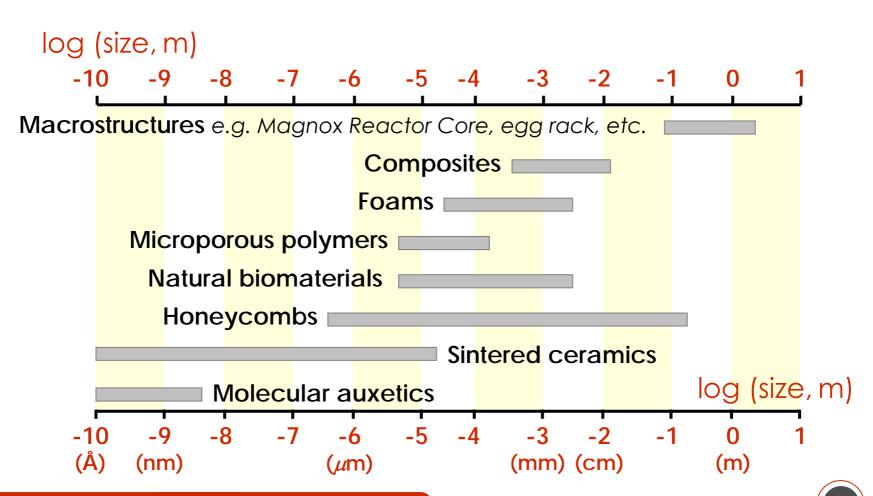
Auxetics



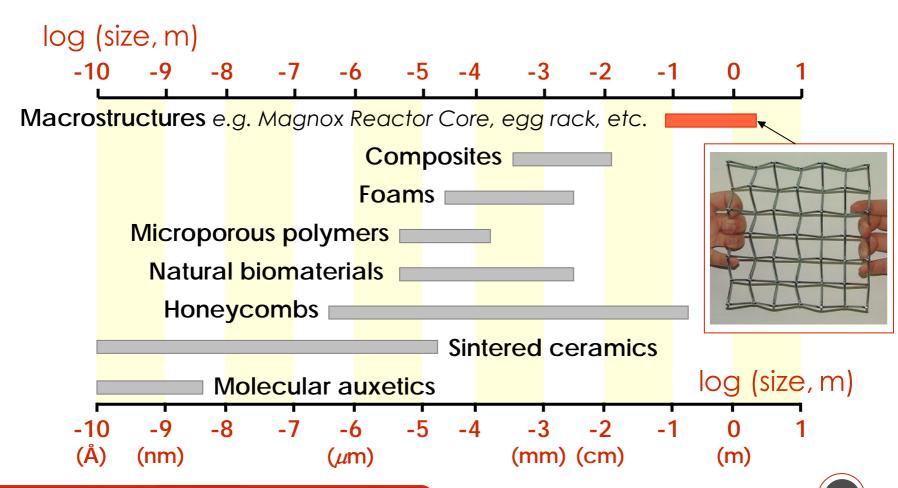


-ve Poisson's ratio → materials get fatter when stretched

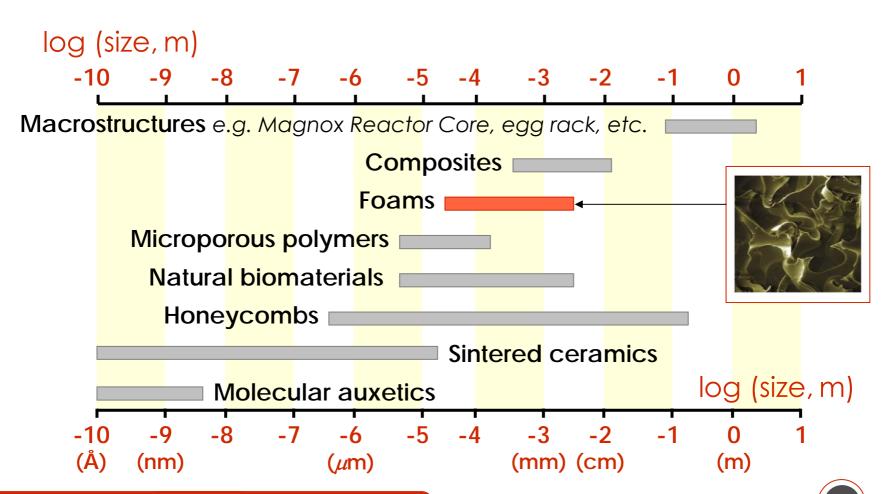




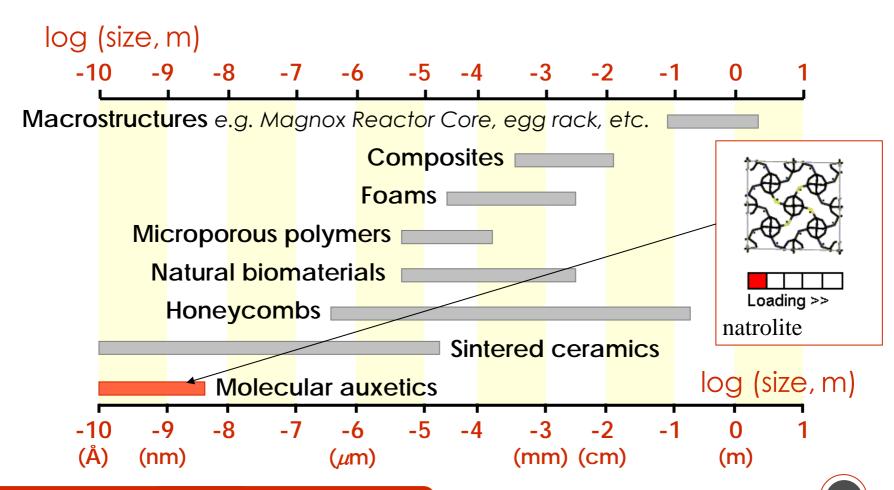














What gives rise to auxeticity

- Correct co-operation between:
 - -The material's internal structure (geometry)
 - -The way the internal structure deforms when loaded (deformation mechanism)



Auxetic mechanisms (1)

Re-entrant honeycombs

$$v_{12} = \frac{1}{v_{21}} = -\tan(\theta) \frac{X_1}{X_2}$$
$$= -\tan(\theta) \frac{l\sin(\theta)}{h - l\cos(\theta)}$$



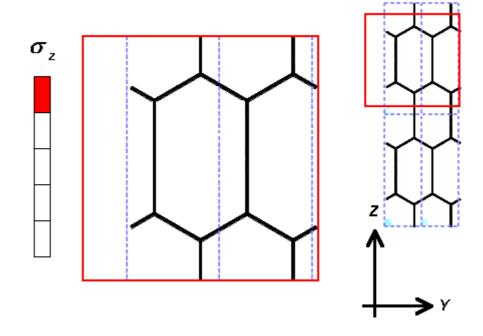
Conventional: $90^{\circ} < \theta < 180^{\circ}$





Auxetic mechanisms (2)

Dilating mechanisms



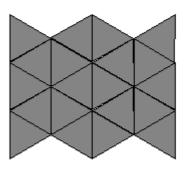


Auxetic mechanisms (3)

Rotating Rigid / Semi-Rigid Units

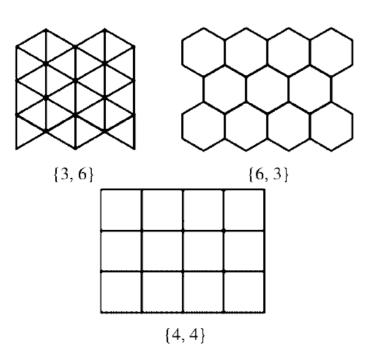
Poisson's ratio will depend on:

- (1) Shape of the rigid unit
- (2) Degree of aperture
- (3) Connectivity
- (4) Extent of rigidity of the unit

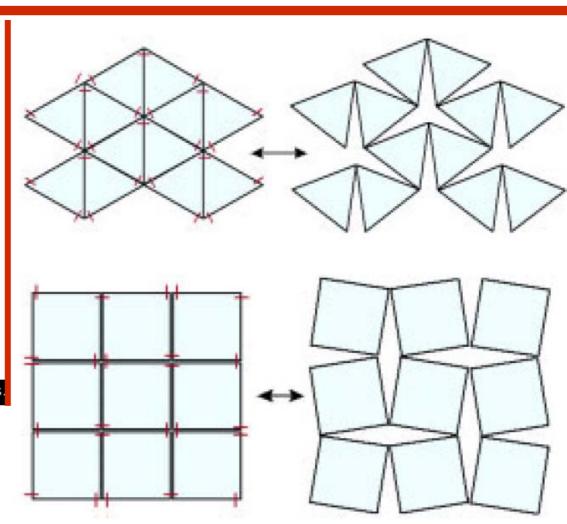




Rotating Quadrilaterals



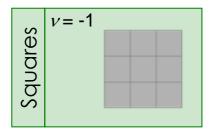
Regular $\{3, 6\}$, $\{4, 4\}$ and $\{6, 3\}$ tessellated structures.





...more examples

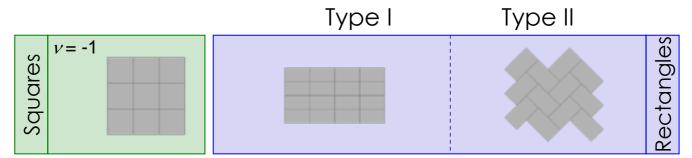
- Rotating rigid units
 - quadrilaterals





...more examples

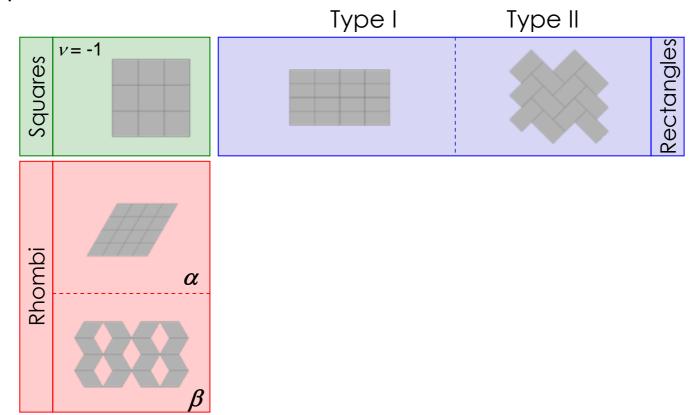
- Rotating rigid units
 - quadrilaterals





...more examples

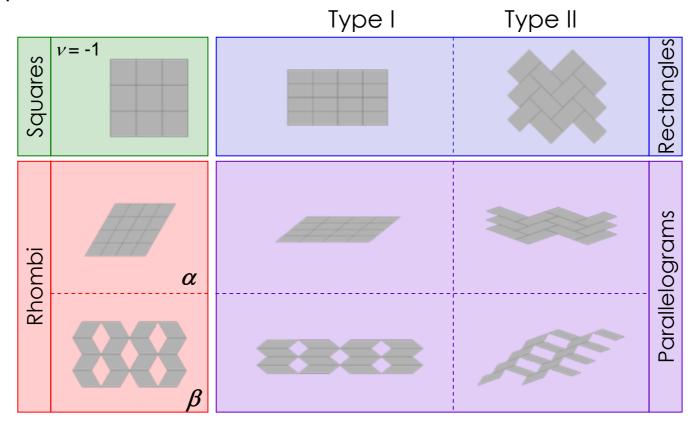
- Rotating rigid units
 - quadrilaterals





.. more examples

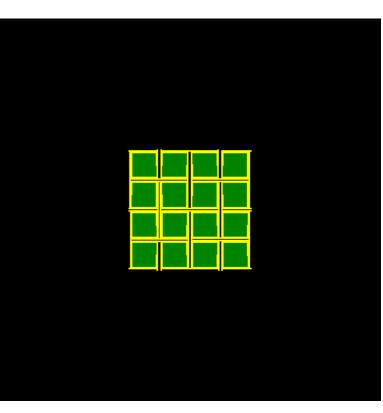
- Rotating rigid units
 - quadrilaterals





Others ... The Chirals, Anti-chirals

n	Chiral tessellations	Anti-chiral tessellations
3	2000	0000
4	555	900
6	200	SYSTEM CANNOT BE CONSTRUCTED

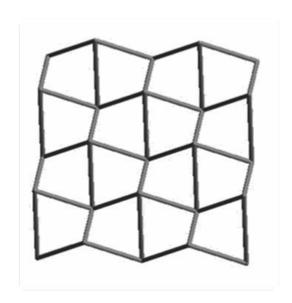


anti-tetrachiral



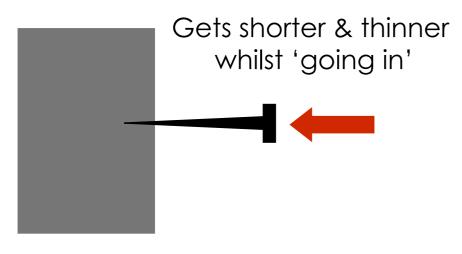
... and more

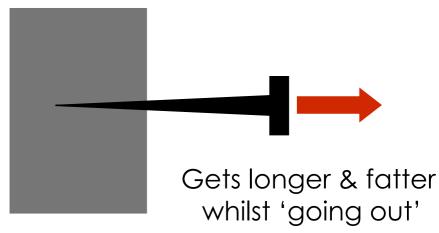
Egg-rack mechanism





Auxetic nails



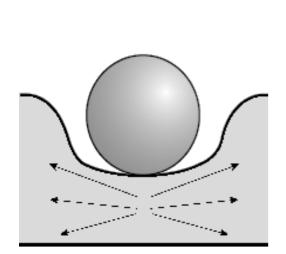


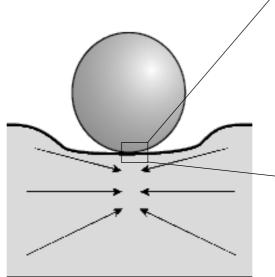


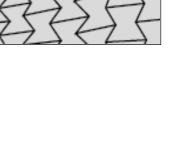
Auxetic materials are harder to indent...

...In auxetics, the material tends to go towards the point of impact to become



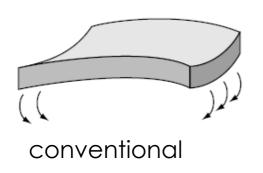


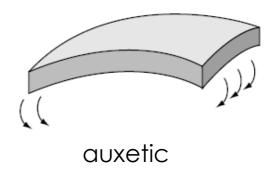






Synclastic behaviour...



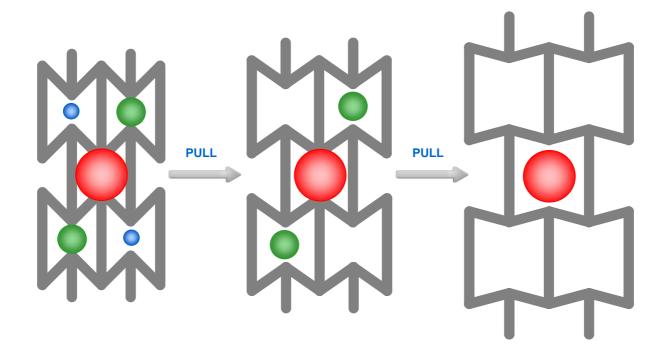


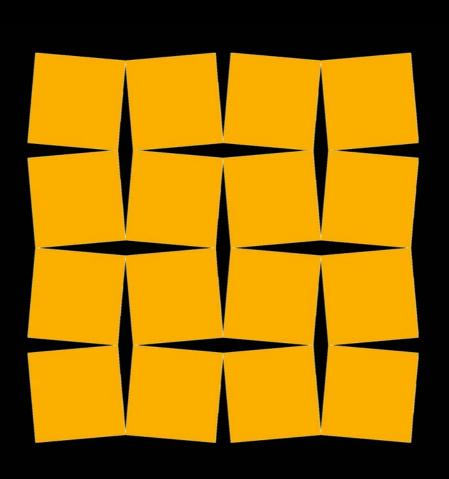
... ability to form dome shaped surfaces





Smart filters

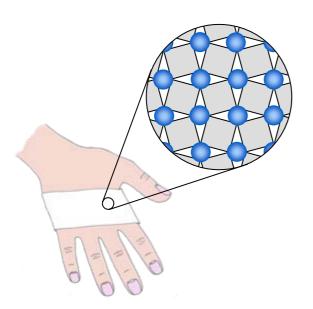


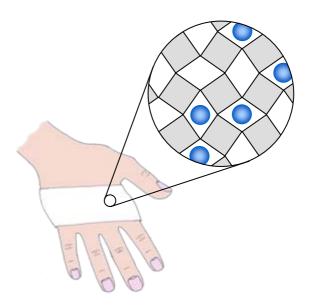




Properties and applications

Smart dressings







Other Properties

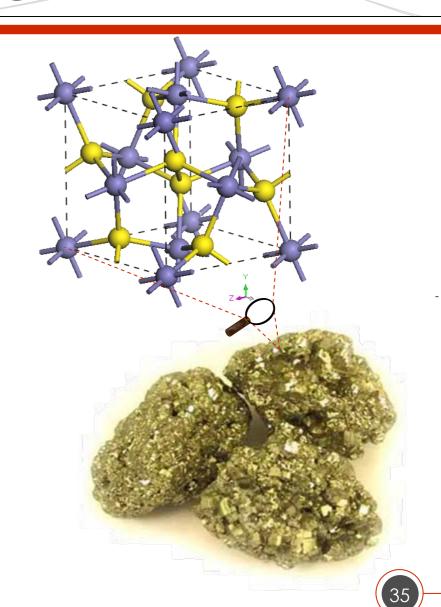
An increased shear stiffness

Higher plane fracture toughness



Historical note

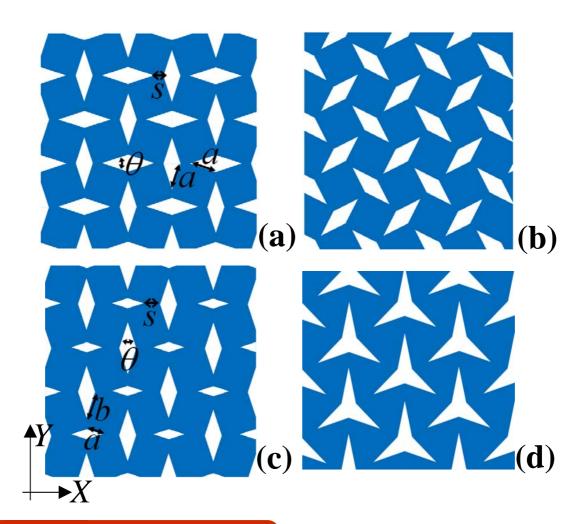
- First Report: A negative
 Poisson's ratio was first
 reported in single crystals
 of iron pyrites and was
 attributed to crystal
 twinning [Voigt, 1928].
- This was followed by some isolated reports mostly in the 1970s and 1980s



Macro auxetics ... an example

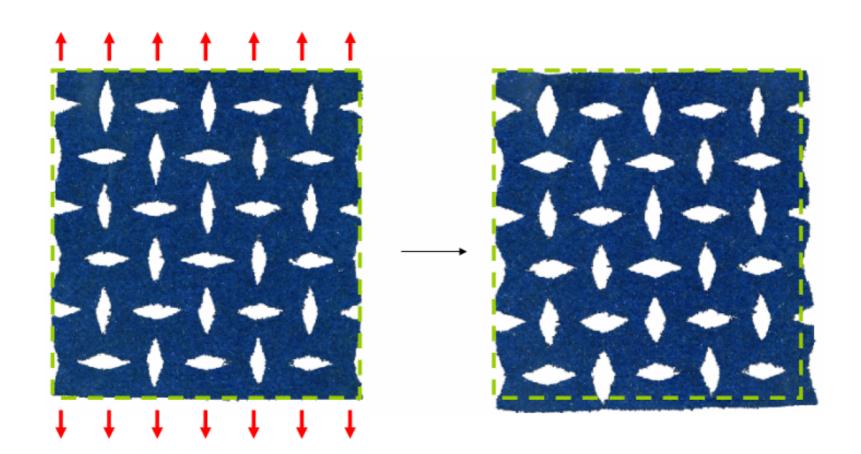


Perforated sheets





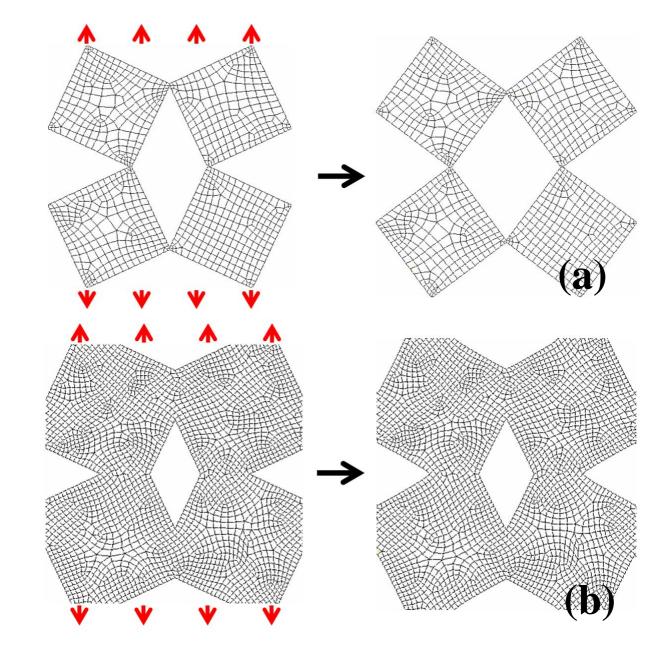
Experiment on Carpet Fabric

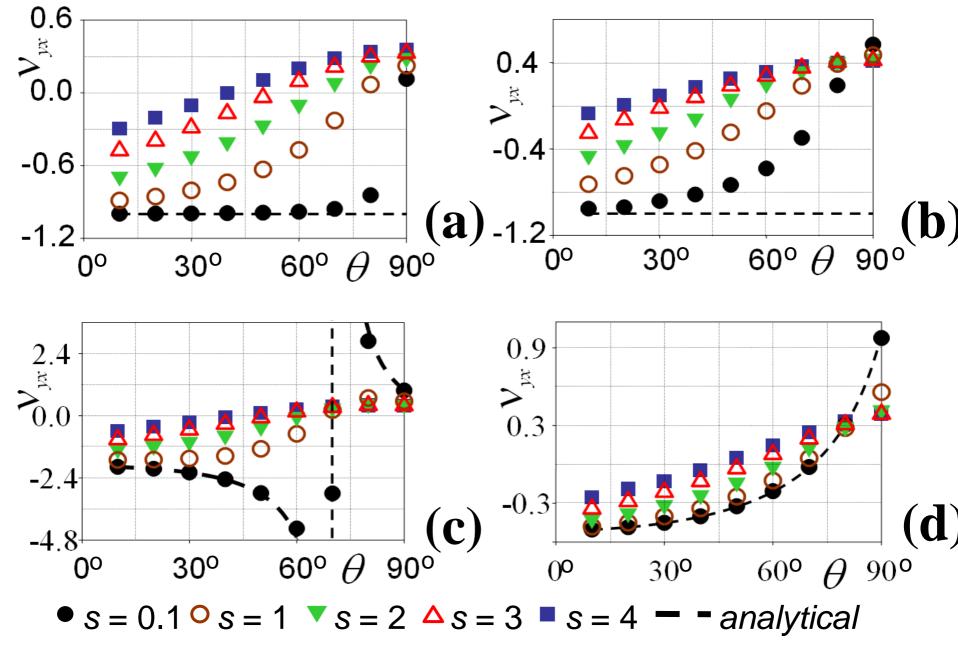




→X

→X

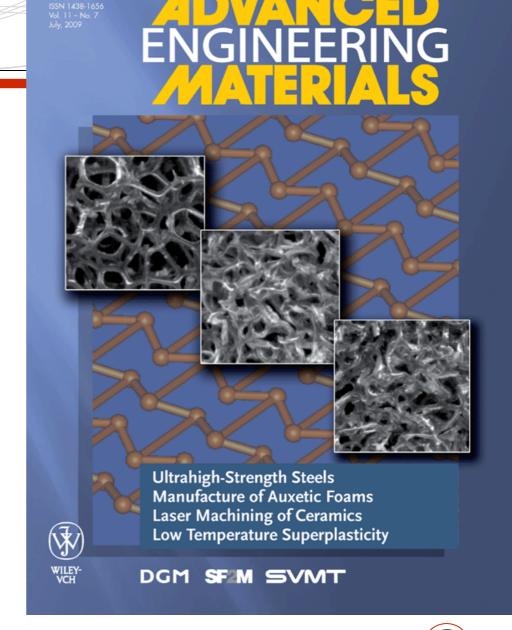






Microscale Auxetics

... FOAMS





Process

- First manufactured by Rod Lakes, University of Wisconsin, Madison, (R. Lakes, Science, 235 (1987) p. 1038-1040.)
- Produced from commercially available conventional foams through a process involving:
 - Volumetric compression of ~30% in volume
 - Heating to the polymer's softening temperature
 - Cooling whilst remaining under compression



Typical Procedure

Starting from: Reticulated 30 ppi polyester polyurethane

- Cut conventional foam in the shape of a cuboid of size 35 mm x 35 mm x 105 mm long;
- Press sample into a mould of dimensions 25 mm x 25 mm x 75 mm (28.6 % strain along each axis);

x 2

- Heat at 200 °C for 10 minutes,
 Remove from mould
 Stretch
 Replace in the mould.
- Cool to room temperature
- Heat for 1 hour at 100 °C

Taken from: Smith, Grima, Evans, Acta Mater. 48 (2000) p.4349-4356.

Technique adapted from: Chan and Evans, J. Mater. Sci., **32** (1997) p. 5945-5953.

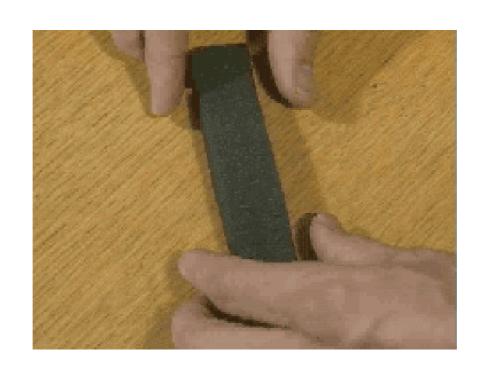
nro

http://www.auxetic.info

43



Before ...





... and after





New approach

Uses solvent instead of heat

- Process involves
 - Wetting foam with appropriate solvent
 - Compressing the foam volumetrically by 30%
 - Allowing the foam to dry well

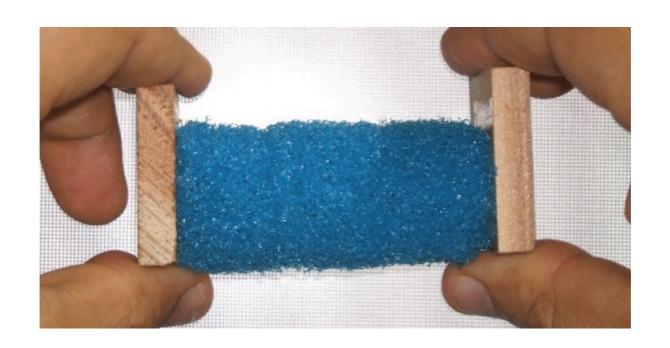


Typical Process

- Starting from: Reticulated 30 ppi polyurethane foam (Dongguan Dihui Foam Sponge, China)
- Cut conventional foam in the shape of a cylinder of diameter
 40mm and length 84mm
- Wet the foam with acetone
- Remove excess solvent
- Press sample into a mould of diameter 26 mm and length 55mm (~35 % strain along each axis);
- Allow the sample to dry completely before removing from mould



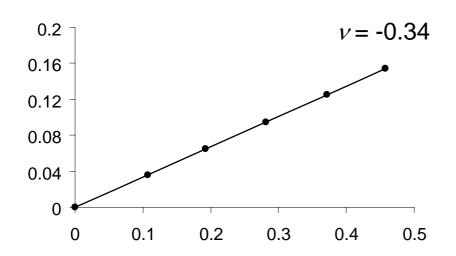
Result

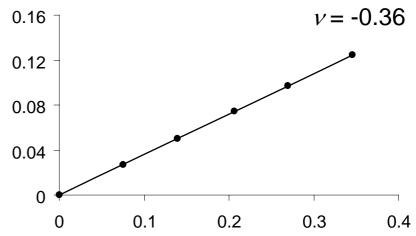


JN Grima, D Attard, R Gatt and RN Cassar, Adv. Eng. Mater., 21 (2009)

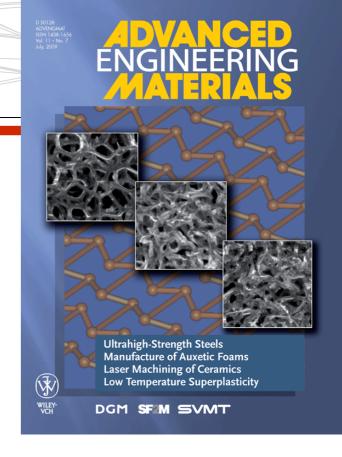


Measurements





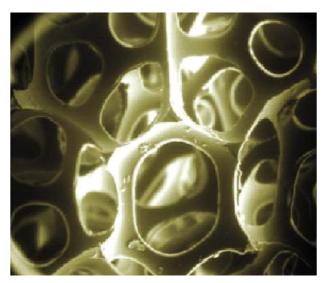




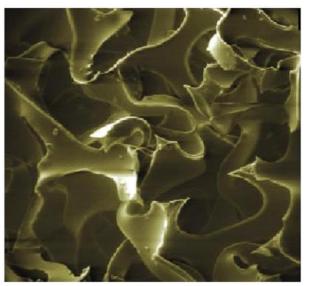
Foams - The Models



Microstructure in auxetic foams



Conventional foam

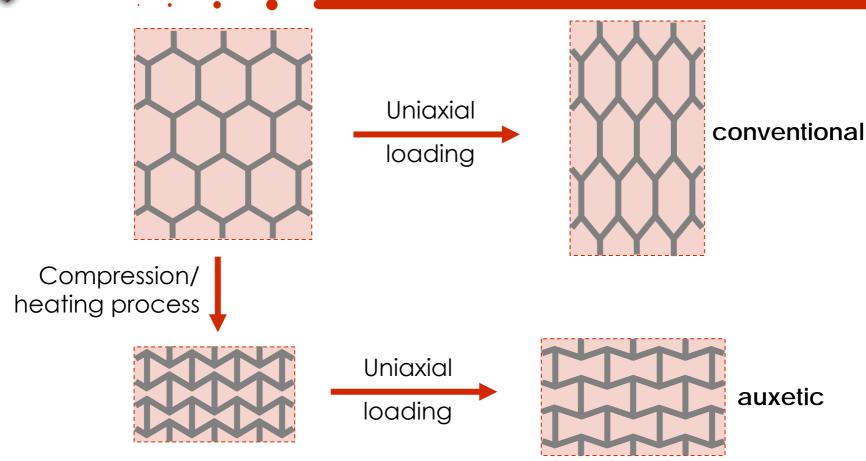


Auxetic foam

JN Grima, A Alderson and KE Evans, J. Phys. Soc. Jpn, 74 (2005) 1341.



Re-entrant structures



LJ Gibson and MF Ashby, Cellular Solids, Cambridge Uni. Press, 1997.

IG Masters and KE Evans, Composite Struct, 35 (1996) 403.

KE Evans, A Alderson and FR Christian, J. Chem. Soc. Faraday Trans., 91 (1995) 2671.

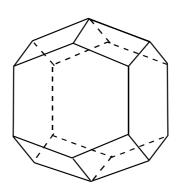


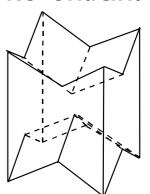
3D Re-entrant structures

conventional

Re-entrant

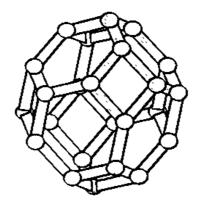
dodecahedron foam models

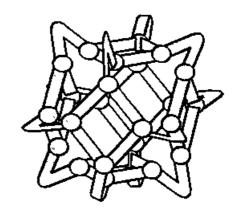




(KE Evans, MA Nkansah and IJ Hutchinson, Acta Metall. Mater., 2 (1994) 1289)

tetrakaidecahedron foam models

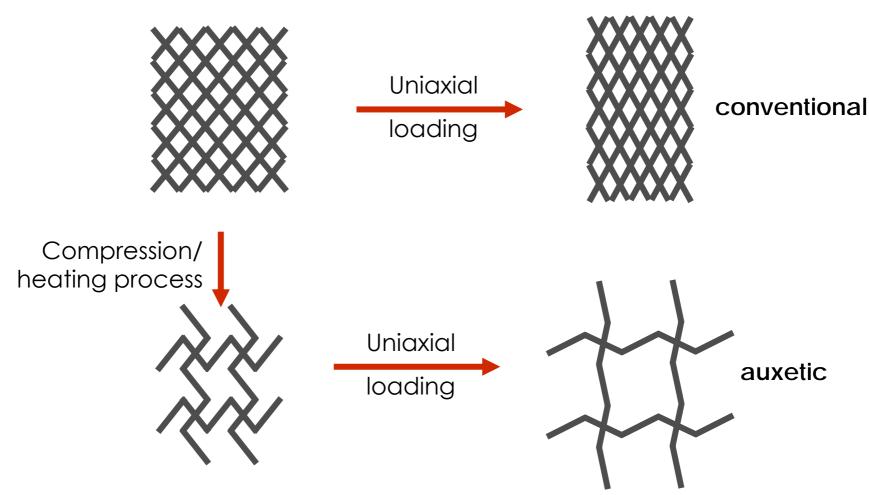




(JB Choi, RS Lakes, J Compos. Mater., **29** (1995) 113.)



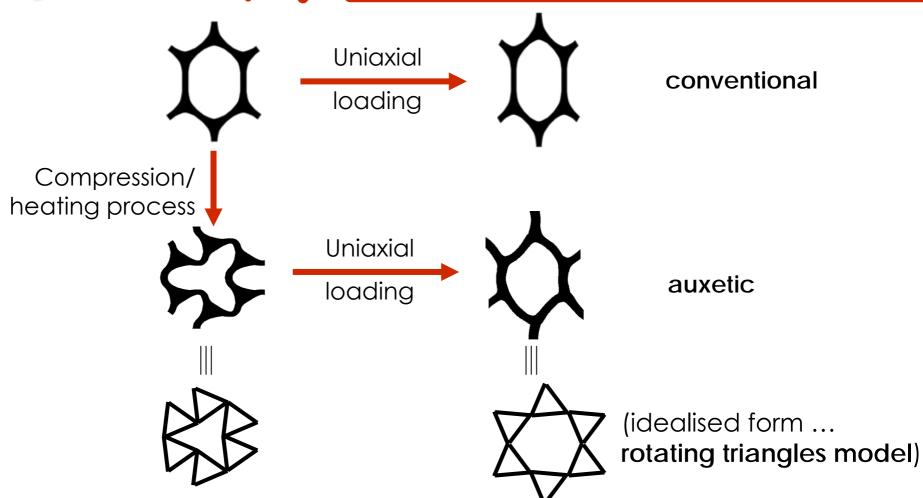
Missing rib model



CW Smith, JN Grima and KE Evans, Acta Mater., 48 (2000) 4349.



Rotating rigid units



JN Grima, A Alderson and KE Evans, J. Phys. Soc. Jpn, 74 (2005) 1341.



Later on ... The evidence

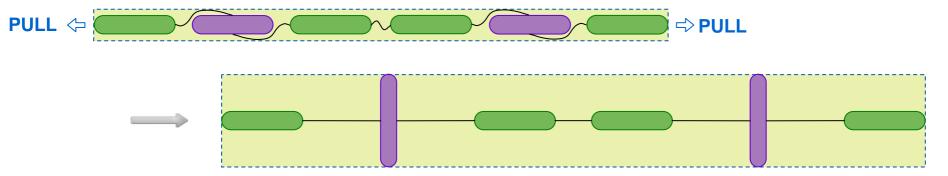
- In situ three-dimensional X-ray microtomography of an auxetic foam under tension, S.A. McDonald, N. Ravirala, P.J. Withers, A. Alderson, Scripta Mater. (2009) p. 232-235 which says:
 - X-ray microtomography has the potential to unambiguously identify the predominant deformation mechanisms responsible for the auxetic response of polymeric foams. It has been performed in situ on an auxetic polyurethane foam subjected to incremental uniaxial tensile loading. A Poisson's ratio of -0.20 measured from localized microstructural changes observed during the tomographic sequence compares well with the bulk value of -0.21 obtained by videoextensometry. Evidence obtained by digital image correlation for straightening of bent ribs and rotation of junctions connecting ribs during straining is presented.





Anselm C. Griffin's LCP

concept



molecular level equivalents

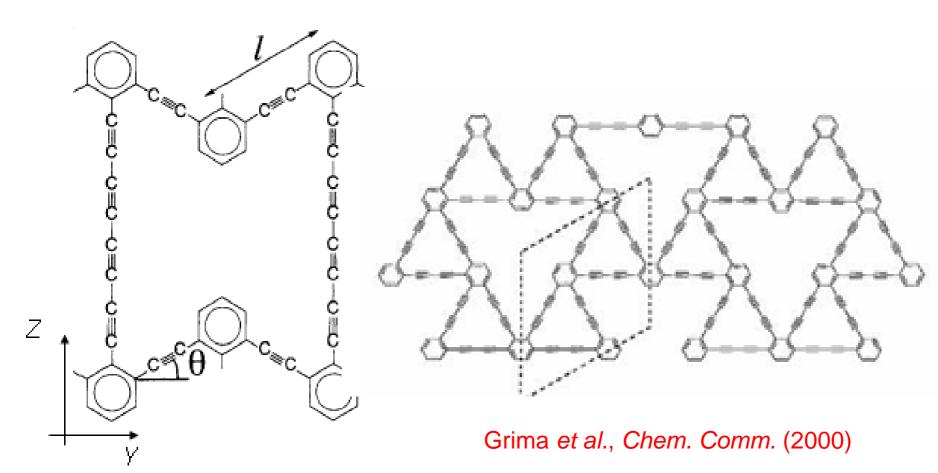
$$\begin{array}{c} C_3H_7 \\ O(CH_2)_{10}O \\ \hline \\ C_5H_{11}O \\ \hline \\ C_3H_7 \end{array}$$

$$O(H_2C)_{10}O-O(H_3C)_{10}O-O$$

http://www.auxetic.info



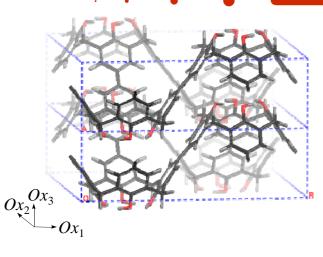
Other possible auxetic polymers

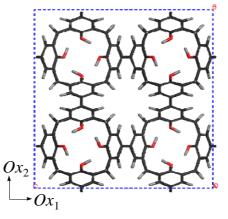


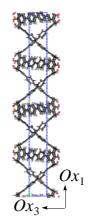
Evans et al., Nature (1991)



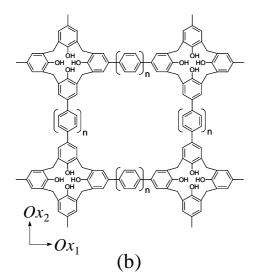
Other possible polymers ...

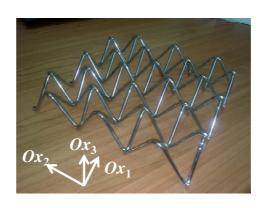






(a)



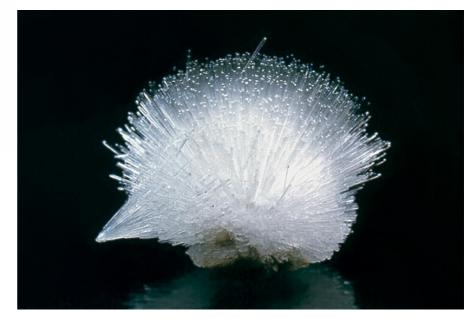


(c) Grima *et al.*, *Chem. Comm.* (2004)



Auxeticity in Naturally Occurring minerals







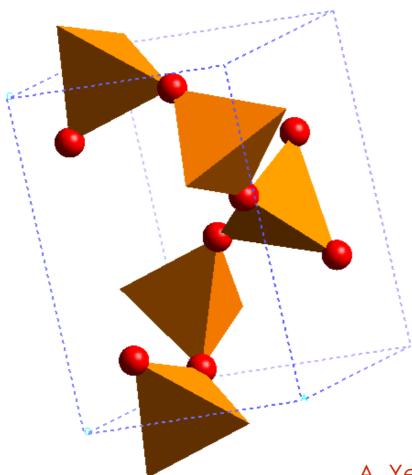
Case Study (i) - Cristobalite

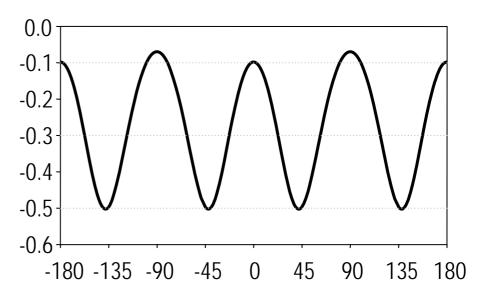
- Meta-stable, crystalline silica
- Has a low temperature phase (α-cristobalite) and a high temperature phase (β-cristobalite)





α-Cristobalite: mechanical properties





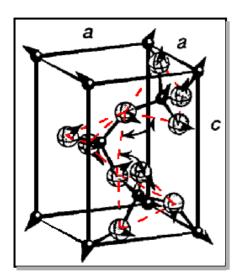
Maximum auxetic behaviour in the (1 0 0) and (0 1 0) planes (yz, xz) at **c. 45**° to the major axes.

A. Yeganeh-Haeri et al., Science, 257 (1992) 650



Deformation mechanisms: Rotating tetrahedra

Keskar & Chelikowsky

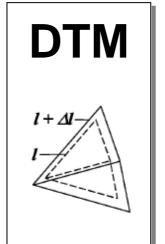


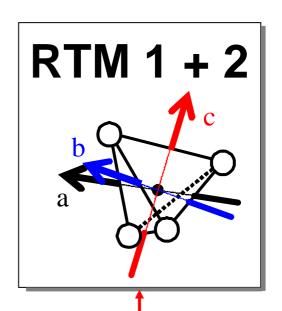
... rotation of SiO₄ tetrahydra

tetrahedra expand / shrink without changing relative orientation



Alderson et al.

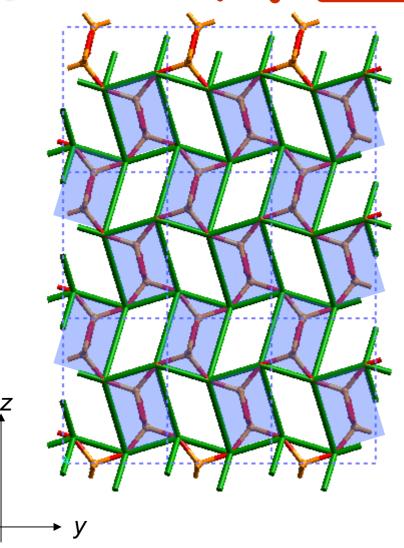




Tetrahedra rotate relative to each other @ two distinct local axis without changing shape



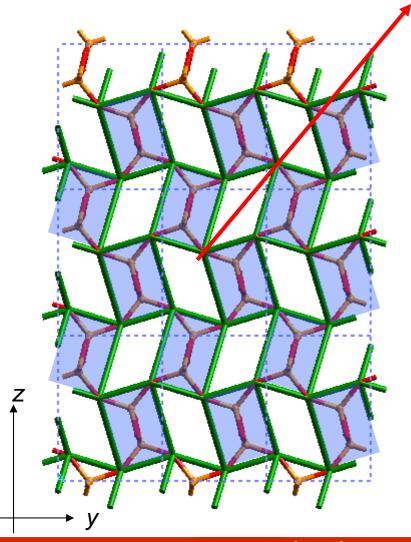
Deformation mechanisms – 2D model

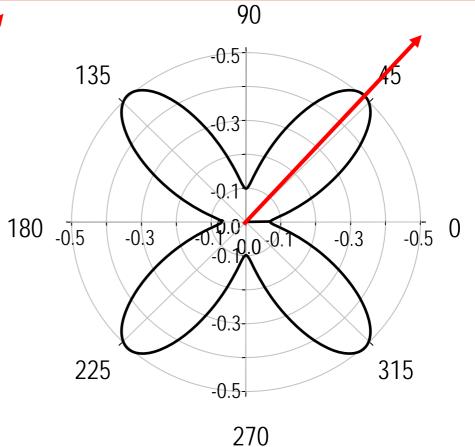


. . . Rotating rectangles as viewed in the (100) Plane (yz-plane)



Deformation mechanisms 2D model

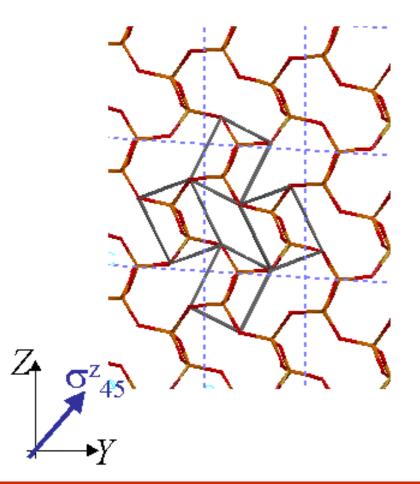




. . . Rotating rectangles as viewed in the (100) Plane (yz-plane)



Rotating rectangles model: Molecular Modelling





Load in σ^z₄₅ direction ... Rotating Rectangles mechanism taking place in the (100) plane

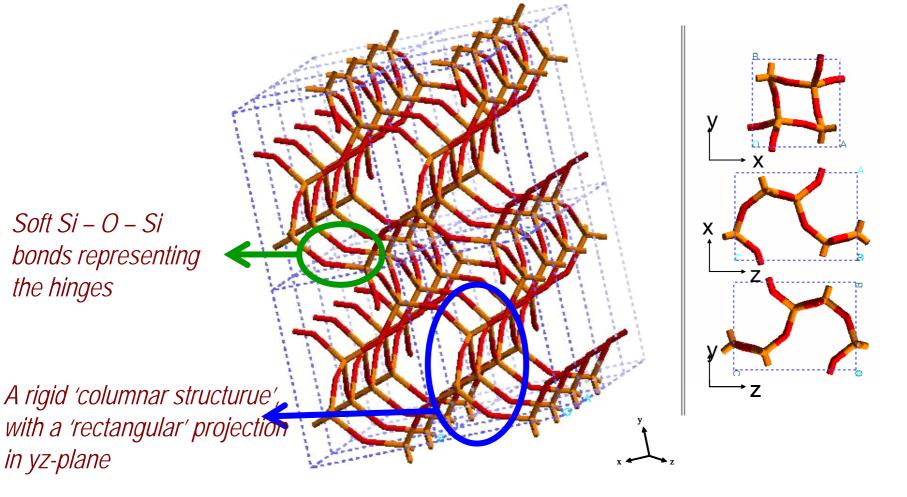


Soft Si – O – Si

the hinges

in yz-plane

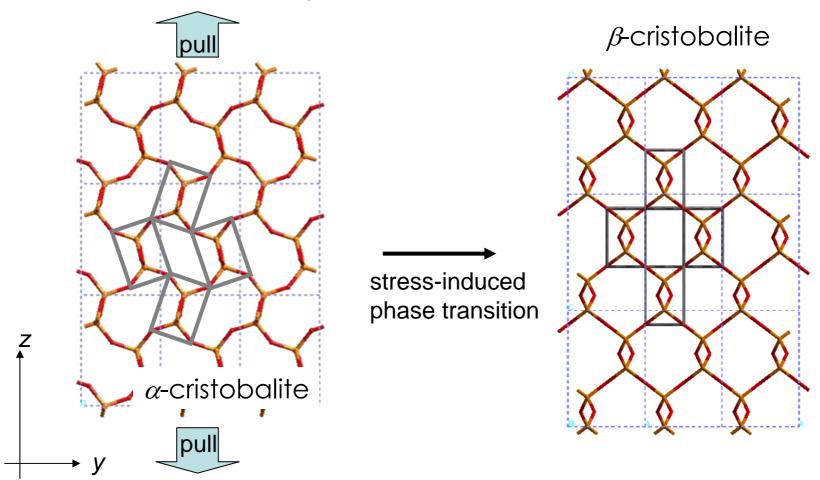
Rotating Rectangles model: Molecular Modelling



http://www.auxetic.info

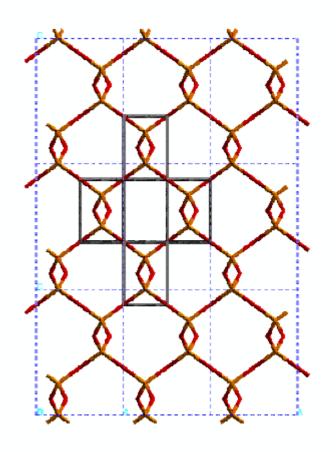


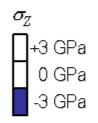
Loss of NPR for the $\alpha \rightarrow \beta$ transition: an explanation

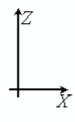




Loss of NPR for the $\alpha \rightarrow \beta$ transition: an explanation



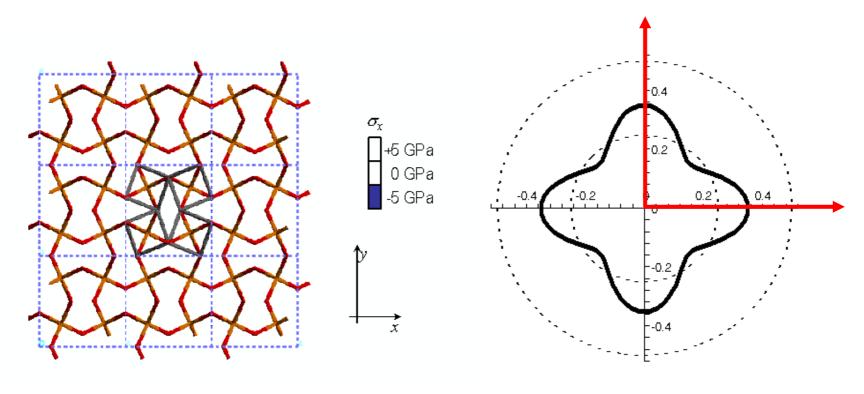




... Conventional behaviour in β -cristobalite in the (100) plane



NPR in 'ordered' β -cristobalite – an explanation



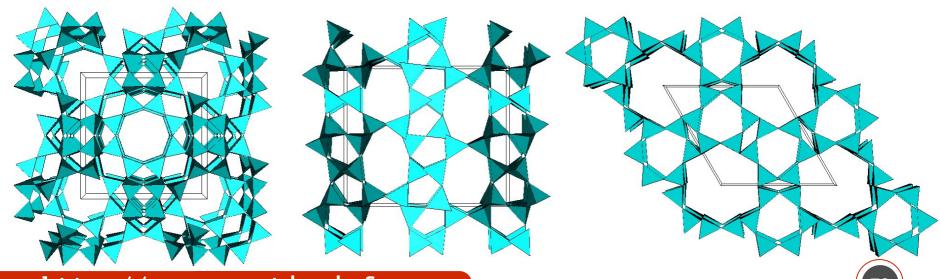
... Rotating squares mechanism taking place in the (001) plane



Case study (ii) - Zeolites

Why look at zeolites?

- Zeolites have highly geometric nanostructures, i.e.
 there is the possibility of auxetic behaviour
- Very little experimental data is available on the single crystalline mechanical properties of zeolites

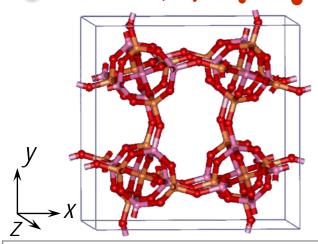


http://www.auxetic.info

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Zeolites ... early studies [1999]



THO (Thomsonite)

 $Na_4Ca_8[Al_{20}Si_{20}O_{80}]$. 24 H_2O

J.N. Grima et al., Adv. Mater, **12** (2000) p.1912

Force-field	$ u_{xy}$	\mathbf{v}_{yx}
Burchart ¹	-0.55	-0.55
BKS ²	-0.33	-0.53
Universal ³	-0.33	-0.40
CVFF ⁴	-0.46	-0.46

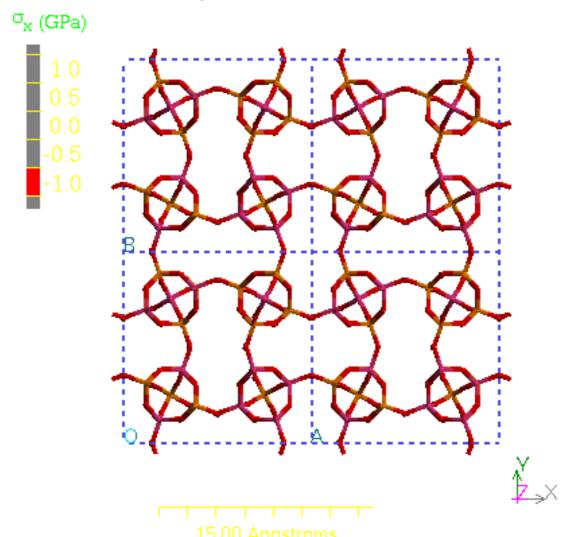
⁽¹⁾ Burchart, PhD. Thesis, Delft. Univ. Tech, (1992)

⁽³⁾ Rappe et al., J. Am. Chem. Soc. **114** (1992) 10046

⁽²⁾ Van Beest et. al., Phys. Rev. Lett., **64** (1990) 1955 (4) Cerius² User Guide, MSI Inc., San Diego, USA (1996)

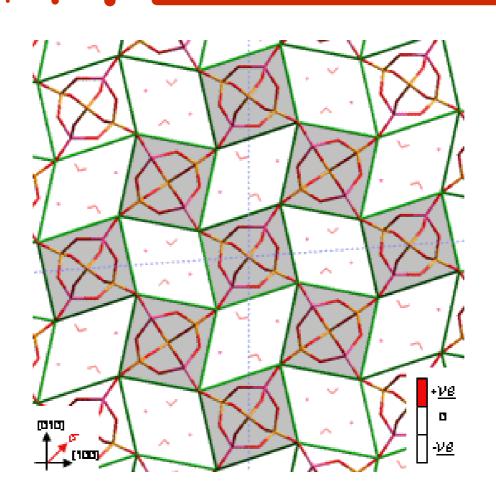


THO: deformations



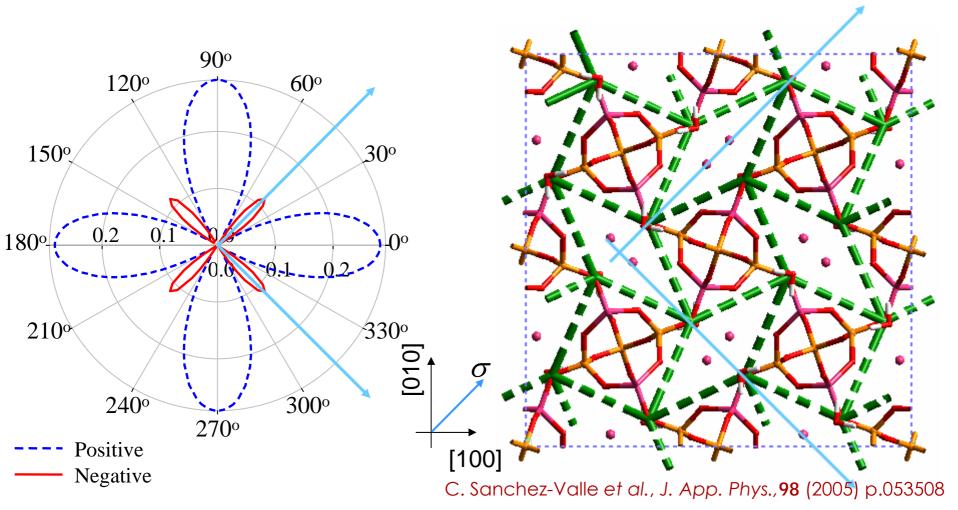


Natrolite (NAT): Deformation





NAT: deformation



J. N. Grima et al., J. App. Phys., 101 (2007) 086102.



Conclusions ..

Auxeticity is a very useful property;

 There are various types of auxetics ... model structures, polymers, foams, zeolites, etc. etc.

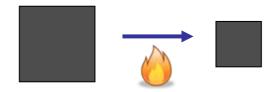
 Can be explained by 'geometry-deformation mechanism' based models;

Nature can teach us how to 'make' auxetics.

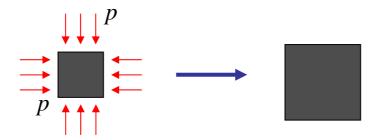


Other thermo-mechanical metamaterials

Negative Thermal Expansion



Negative compressibility





Negative Thermal Expansion: NTE

$$\alpha_{V} = \frac{1}{V} \frac{\partial V}{\partial T}$$

$$\alpha_{L} = \frac{1}{L} \frac{\partial L}{\partial T}$$

NTE

Cooling ... systems get larger

Heating ... systems get smaller

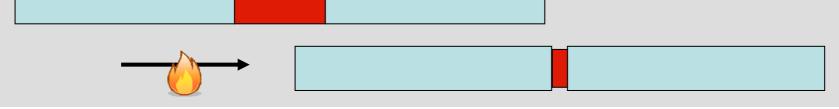


e.g. water near its freezing point

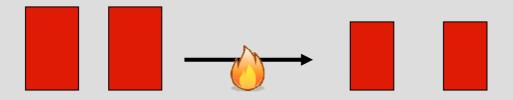


Applications

- Achieve any pre-desired thermal expansion
- Use as a 'filler' between two expanding strips



 Ensure that gap remains in diffraction gratings / sensors





Problem ...

 NTE materials are usually produced on a small scale and are very expensive

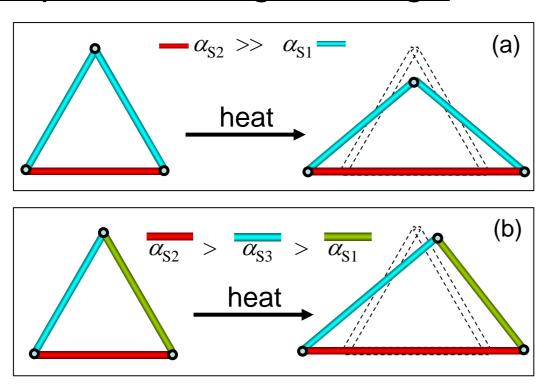
Solution ????

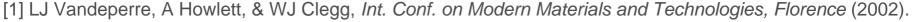


Case Study 1: NTE in triangular systems



Concept: the flattening of a triangle





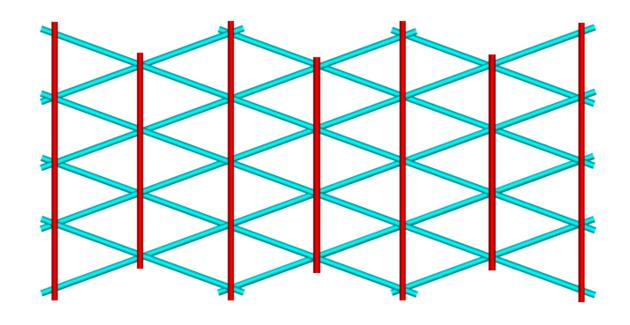
^[2] LJ Vandeperre & WJ Clegg, MRS Symposium Proceedings, 785 (2003) D11.4.

[4] CW Smith et al., Auxetic & Related Systems II & III, Poznan (2005); Exeter (2006)

^[3] D Cao, F Bridges, GR Kowah & AP Ramirez, *Phys. Bev. B*, **68** (2003) 014303.



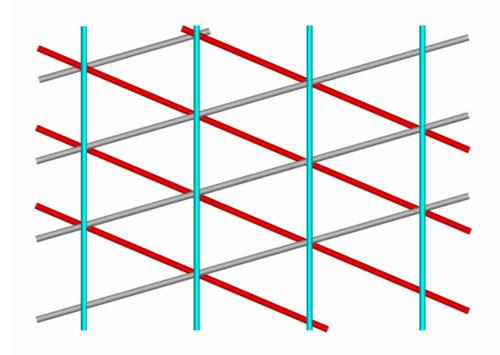
Implementations (1)...





Implementations (2)...

If three sides are made from different materials, the system may shear



J.N. Grima, Proc. Royal Soc. A, (2007)



Model for generalised form

$$\alpha_{11} = \frac{\mathcal{E}_{11}}{dT} = \left[l_1^2 \left(l_2^2 + l_3^2 \right) \alpha_{S1} + l_2^2 \left(l_1^2 + l_3^2 \right) \alpha_{S2} + l_3^2 \left(l_1^2 + l_2^2 \right) \alpha_{S3} \right] \frac{1}{2l_2^2 X_{11}^2}$$

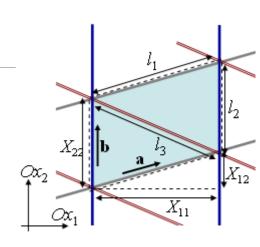
$$- \left[2l_2^2 X_{11}^2 \alpha_{S2} + l_1^4 \alpha_{S1} + l_2^4 \alpha_{S2} + l_3^4 \alpha_{S3} \right] \frac{1}{2l_2^2 X_{11}^2}$$

$$\alpha_{22} = \frac{\varepsilon_{22}}{dT} = \alpha_{S2}$$

$$\alpha_{12} = \alpha_{21} = \frac{\varepsilon_{12}}{dT} = \frac{1}{2} \frac{\gamma}{dT} = \frac{l_1^2 (\alpha_{S1} - \alpha_{S2}) - l_3^2 (\alpha_{S3} - \alpha_{S2})}{2X_{11}l_2}$$

$$\alpha(\zeta) = \alpha_{11}\cos^2(\zeta) + 2\alpha_{12}\sin(\zeta)\cos(\zeta) + \alpha_{22}\sin^2(\zeta)$$

$$\alpha (\zeta)_{\text{max/min}} = \frac{\alpha_{11} + \alpha_{22}}{2} \pm \sqrt{\left(\frac{\alpha_{11} - \alpha_{22}}{2}\right)^2 + \alpha_{12}^2}$$





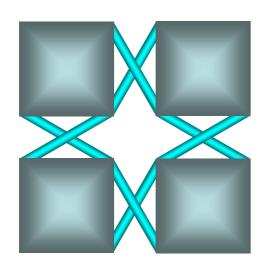
Implementation (3) ...

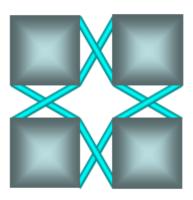
Maximizing the effect Gas ... use of gases



Implementation (4)...

Clegg & Vandeperre



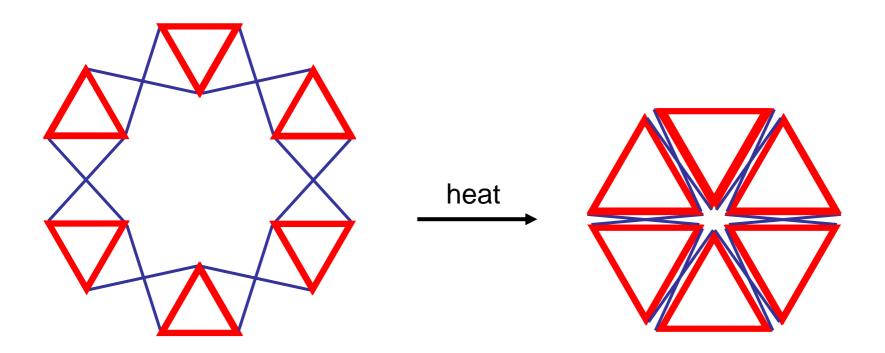


A 2D network which can generate isothermal NTE (squares can be hexagons or triangles)



Implementation

Also possible with triangles & hexagons ...





Is this important???? ... New Scientist









Bill Clegg, University of Cambridge ... A mathematical tool that makes designing the strut-based structures easier could be useful in a variety of engineering situations, he adds: "Thermal expansion is an enormous problem, particularly when you have layers of different material that expand differently, or when the gaps between electrodes are important, like in fuel cells or oxygen sensors."

...CORDIS focus Newsletter



In this issue

- Biotechnology integral part of EU economy, finds report, page 6
- ICT investment paying off, says (2010 report, page 8)
- Electronic health services without borders, page 12
- EU protect launches clinical trials In HIV prevention, page 15
- Keeping Germany competit R & D investment, lifelong learning and SMEs, page 19



CORDIS

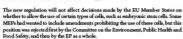


MEPs approve regulation for innovative therapies

A proposed regulation on marketing innovative therapies and on monitoring patients and products post-authorisation, was approved by the European Parliament (EP) on 25 April 2007.

The regulation provides for a compulsory centralised procedure to authorise the marketing of innovative products, and also for post-authorisation monitoring of patients and products. In the compromise package reached between Members of the European Parliament (MEPs) and the Council of the EU, amendments were included to enhance product safety and make the process easier for small and medium-sized enter-





AROUND EUROPE

Groundbreaking research by Maltese academics hits the headlines

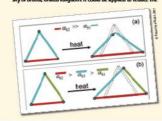
Maltese scientists are calebrating as their groundbreaking work on developing a way of reducing the impact of thermal expansion attracted the interest of the international scientific press.

scientific discoveries likely to impact society, took up the story as one of its breaking news items on its website, following the publi cation of the research results in Proceedings of the Royal Society A.

This was a cause to celebrate for the smallest EU Member State in terms of both population and area.

The team of scientists from the University of Malta had worked on negative thermal expansion, successfully developing a way of designing structures of any size that shrink when heated. This work follows from earlier resarch by Drs Bill Clegg and Luc Vandeperre from the University of Cambridge, United Kingdom, and by Professor Ken Evans and Dr Chris Smith from the University of Exeter, United Kingdom.

Their work was funded by the Malta Council for Science and Technology (MCST) and the EU-funded 'Chiral smart honeycomb' (Chismacomb) project, led by Dr Fabrizio Scarpa of the Univer-sity of Bristol, United Kingdom. It could be applied to reduce the



impact of thermal expansion on anything ranging from bridges to microscopic systems.

The University of Malta is gradually building an infrastructure to conduct world-class research in niche areas of engineering, science and medicine? said Professor Juanito Camilleri, the rector at the University of Malta.

Though we do not have a long-standing tradition of institutional research, and despite the very modest funds to sustain such endeavours, our up and-coming researchers have shown, time and again, through their publications, that they can put us on the interonal map of scientific and technological innovation, he added

The team of scientists studied triangles with at least one side made from a different material to the others, connected by rotating joints. They found that the diverse materials would change volume in response to temperature in a different way. The trian gles would actually shrink in one direction when heated.

The researchers then derived equations that describe the behaviour of their triangle-framework system as these are essential to predicting the response to temperature of their structure. So the mathematical model makes it possible to choose exactly how such a structure behaves.

The coordinator of the project, Dr Joseph N. Grima, and his colleagues believe the lattices of the triangles could have all kinds of applications. We have shown that it is possible to easily design systems that exhibit a tailor-made response to temperature, he said. 'These systems could be constructed very cheaply and could be as big as a bridge or on a microscopic scale, he concluded.

Result on information families links either? Matte

Austrian budget places research in 'best hands'

Research is in the best hands, a sufficient budget is there, said Austrian Science Minister Johannes Hahn in response to a preser of the 2007 budget by Finance Minister Wilhelm Molterer.

by EUR 420.8 million in 2007 — a rise of more than 13.7 % - to FUR 3.501 billion. In 2008 a further increase of EUR 457 million is planned, taking funding up to EUR 3.538 billion. This is the biggest increase since 1991, and was welcomed by Mr Hahn, the Science Council, the Association of Professors, and the Rectors'

Mr Hahn described the budget speech as 'a true declaration about the future of our society. 'And what is more the future than science and research? he asked.

Universities are also set to benefit from the new budget _ to the tune of over FUR 500 million over the coming three years. This equates to a 10 % funding increase

The minister pledged that more money will be made available to support students at a later stage — time constraints had meant that only an across-the-board increase in funding was possible for this budget. Mr Hahn indicated that more targeted funding will be made available at a later stage, once discussions on objectives have taken place.

Based on Information from the Austrian Government



CORDIS focus Newsletter - No 278 - May 2007



Can a system exhibit both NPR and NTE?

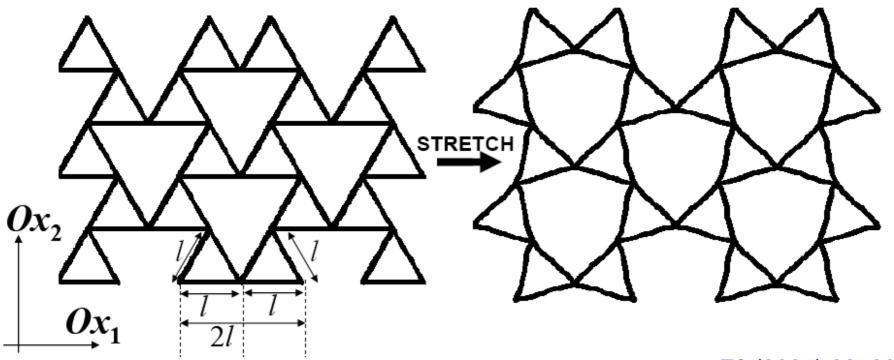


... For example the rotating triangles system



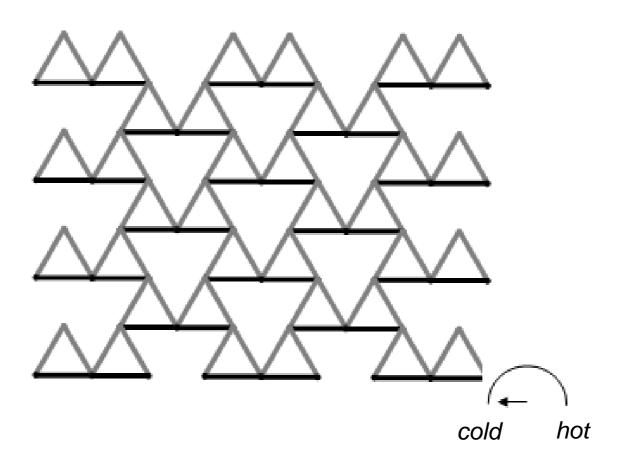
Auxeticity from 'Rotating Triangles' geometry

Negative Poisson's ratio



J.N. Grima, et al., J. Phys. Soc. Jpn., 76 (2007) 025001





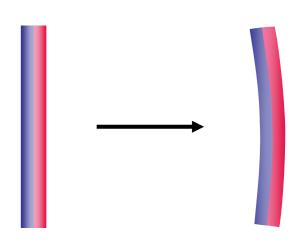
J.N. Grima, et al., J. Phys. Soc. Jpn., 76 (2007) 025001



Case Study 2: Bi-materials

Heating a bi-material with components having different thermal expansion coefficients will cause a curvature

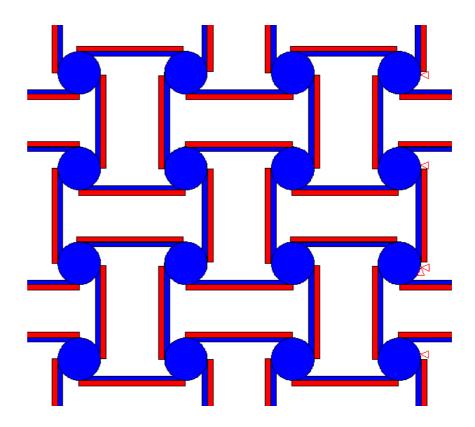
Same thing will apply if they have different moduli, etc.





Implementation ...

Use with anti-tetrachiral (of other similar systems)

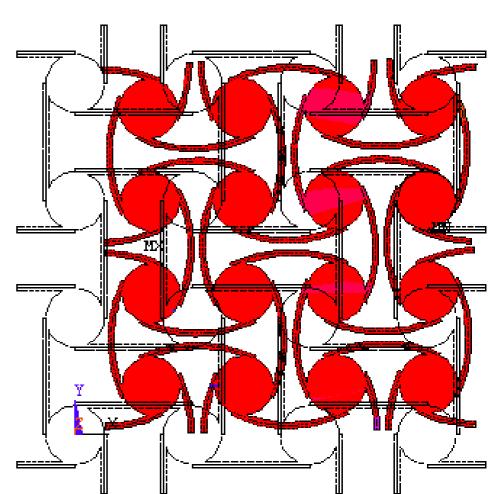




Result ... NTE / NPR

e.g.: NTE (verified with ANSYS)

	<u>Material 1</u>	<u>Material 2</u>
Young's modulus (psi):	1.20 x 10 ⁵	1.20 x 10 ⁵
Poisson's ratio:	0.3	0.3
Coefficient of Thermal Expansion:	5 x 10 ⁻⁷	0.00011





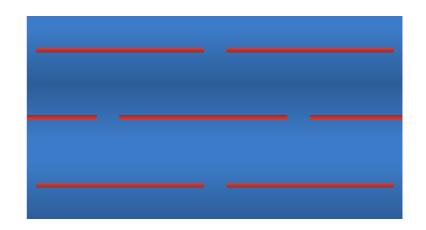
Case Study 3: NTE in composites with Needle-Like inclusions

i MA

engineering & research

(Ing. Michael Attard)



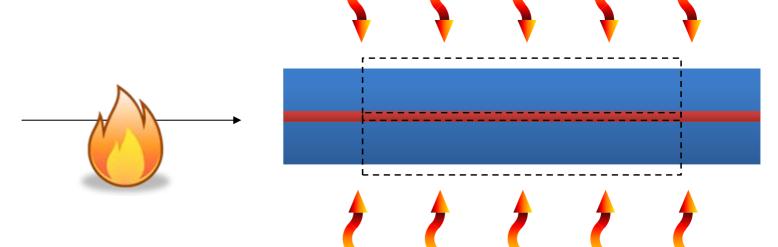




Case Study 3: NTE in composites with Needle-Like inclusions



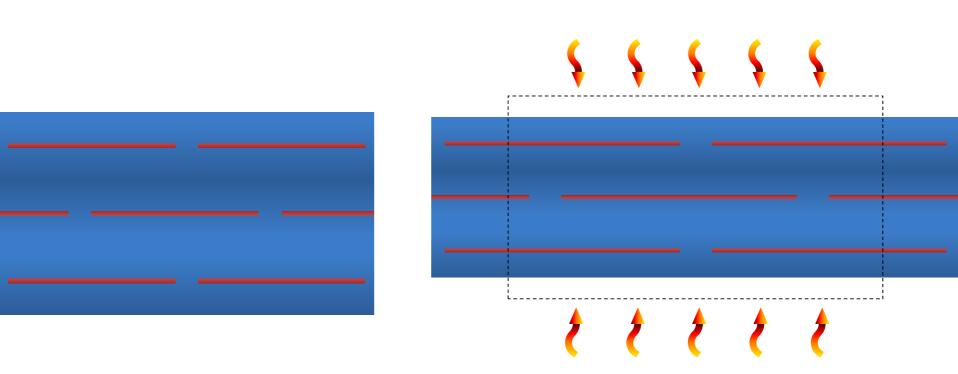
i MA engineering & research



J.N. Grima et al., Comp. Sci. Tech. (2010)

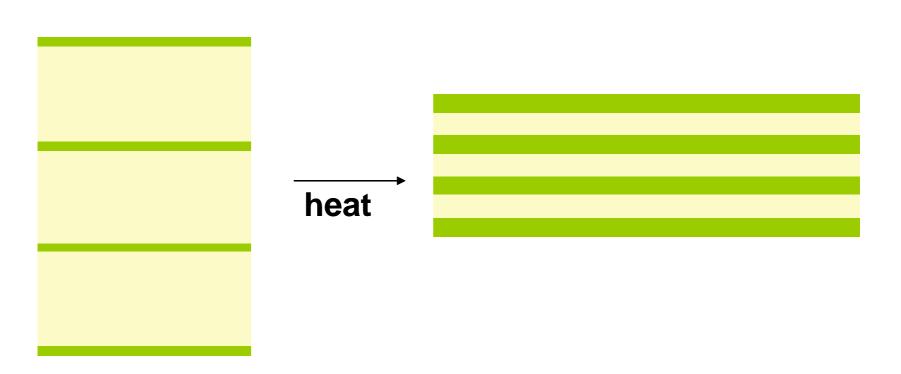


Case Study 3: NTE in composites with Needle-Like inclusions

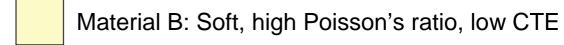




Alternative 'multi-layered' systems



Material A: Stiff, high CTE



J.N. Grima et al., Phys. Stat. Sol. RRL (2010)



Negative compressibility, NC

 Compressibility is a measure of the relative volume change of a fluid or solid as a response to a pressure (or mean stress) change.

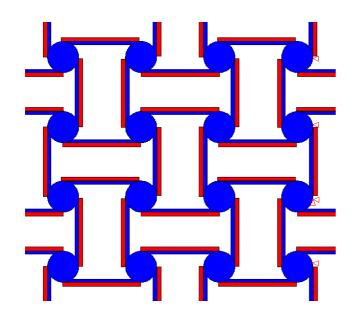
$$\beta = \frac{1}{K} = -\frac{1}{V} \frac{\partial p}{\partial V} \longrightarrow \text{Normally negative}$$

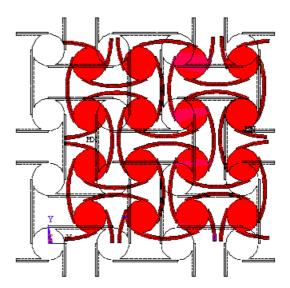
- Normally: System gets larger under negative pressure (partial vacuum)
- Negative compressibility: systems get smaller under negative pressure



Negative Compressibility

 Bimaterials also bend when subjected to a change in pressure if constituent materials have different Young's moduli and/or Poisson's ratio



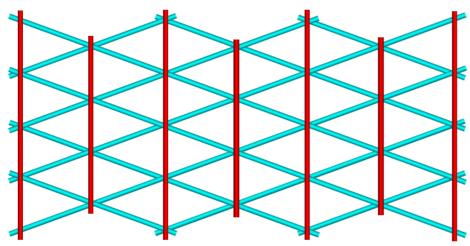


R. Gatt & JN Grima, Scripta Mater. (2007)

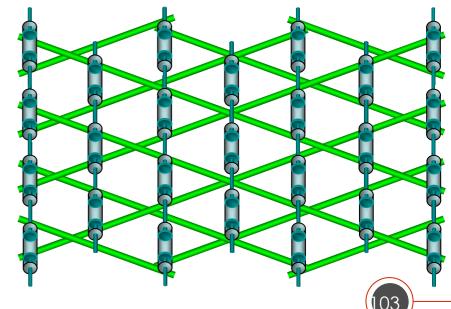
R. Gatt & JN Grima, Phys. Stat. Sol RRL. (2007)



Also in triangular systems ...



D. Attard et al. Phys. Stat. Sol. B (2008)



http://www.auxetic.info



Conclusions

- There are various thermo-mechanical metamaterials, including auxetic metamaterials, NTE and NC systems
- Some of these systems can be 'constructed; based on very simple models and concepts;
- Thermo-mechanical metamaterials can have some very interesting applications;
- NPR / NTE / NC can co-exist, and when they do, results are very interesting.

Thank you!

www.auxetic.info

