

Exotic Nuclear Geometries, Symmetries and Quantum Numbers

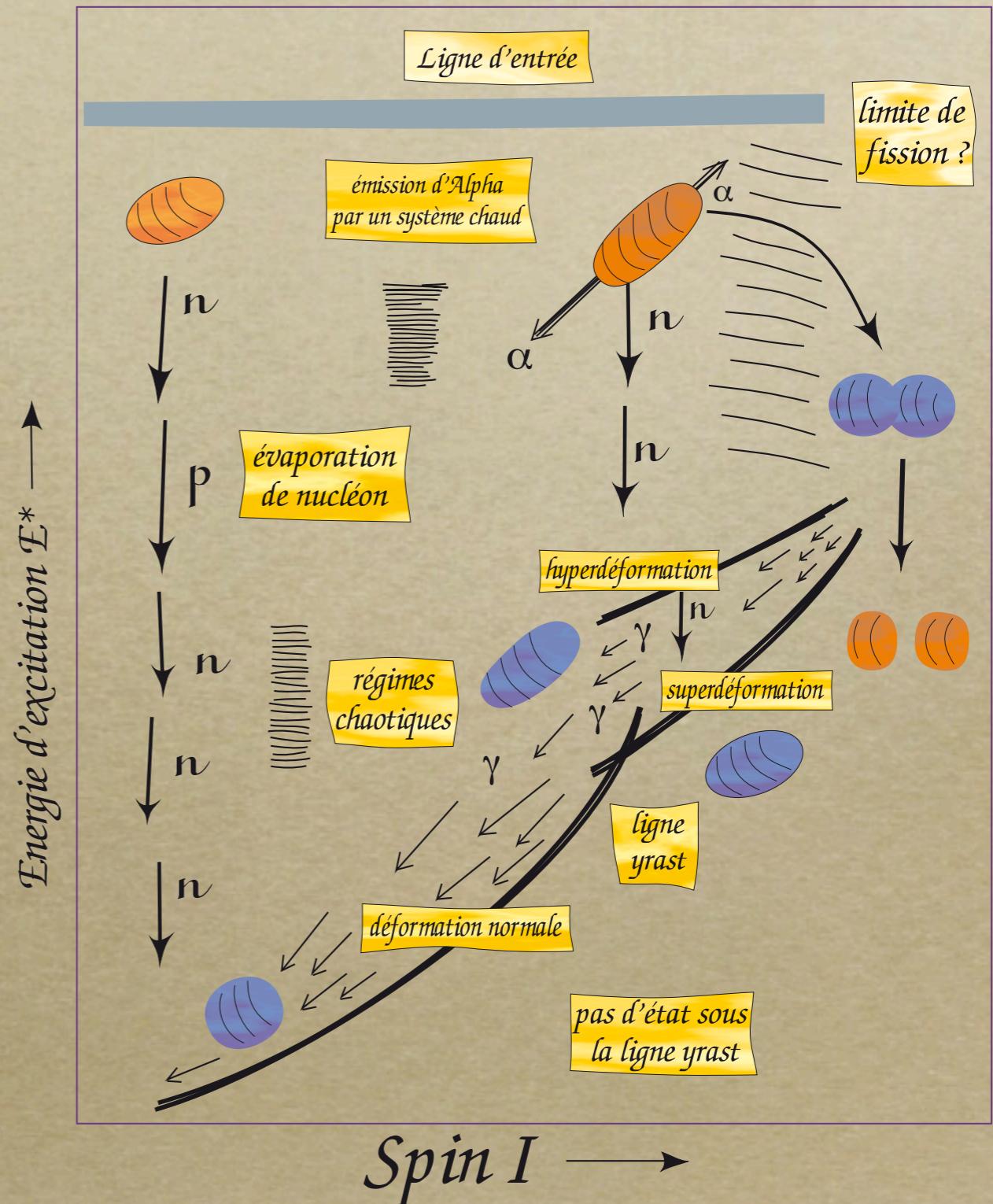
Benoît GALL

IPHC - Strasbourg University

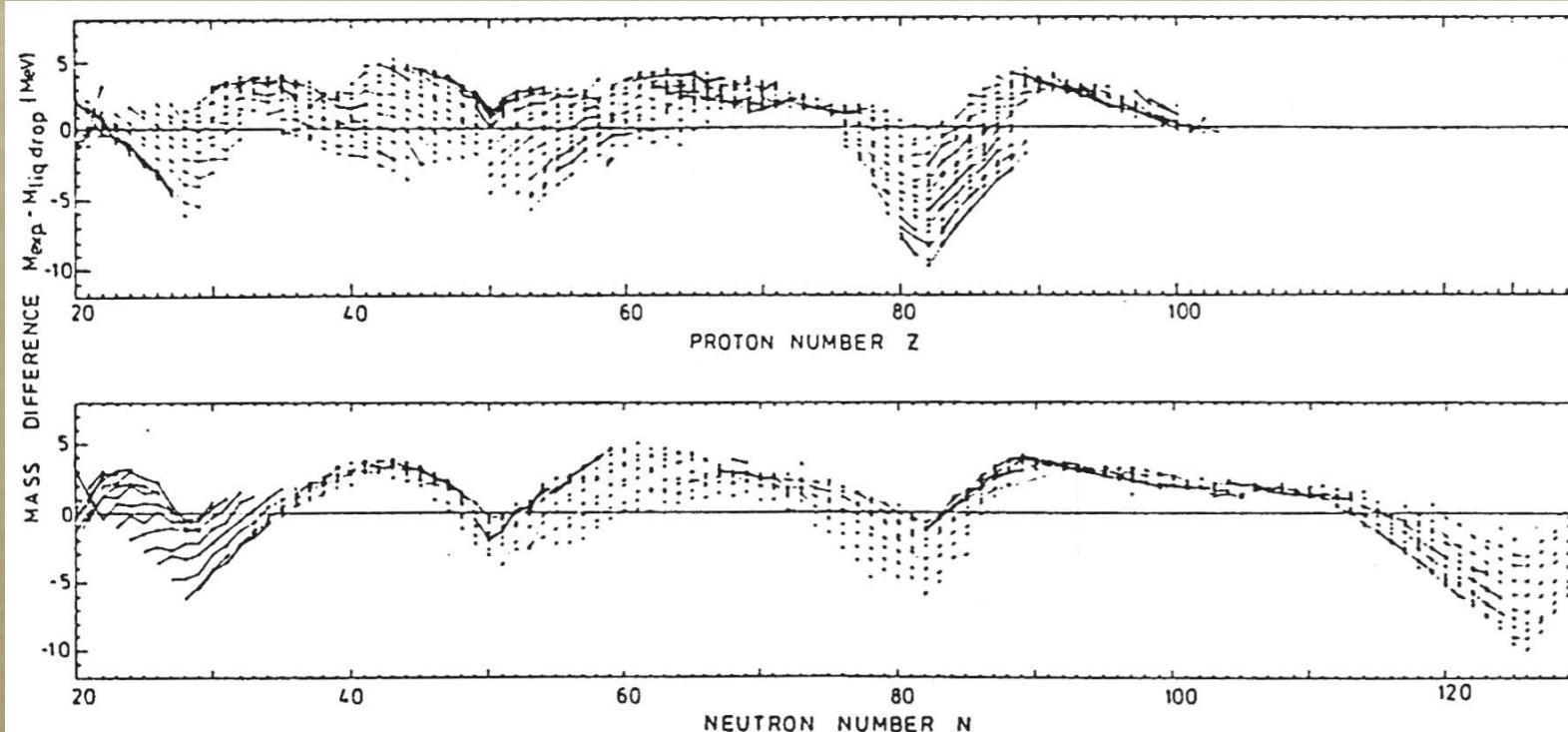
UEE- July 3 2009

Outline

- Preliminary considerations
- Excitations of the nuclei; case of rotationnal bands
- Effect of Nuclear deformation
- Experimental toolboxes & selected cases



Magic Numbers and Shell Model.



Same Magic numbers for neutrons & protons

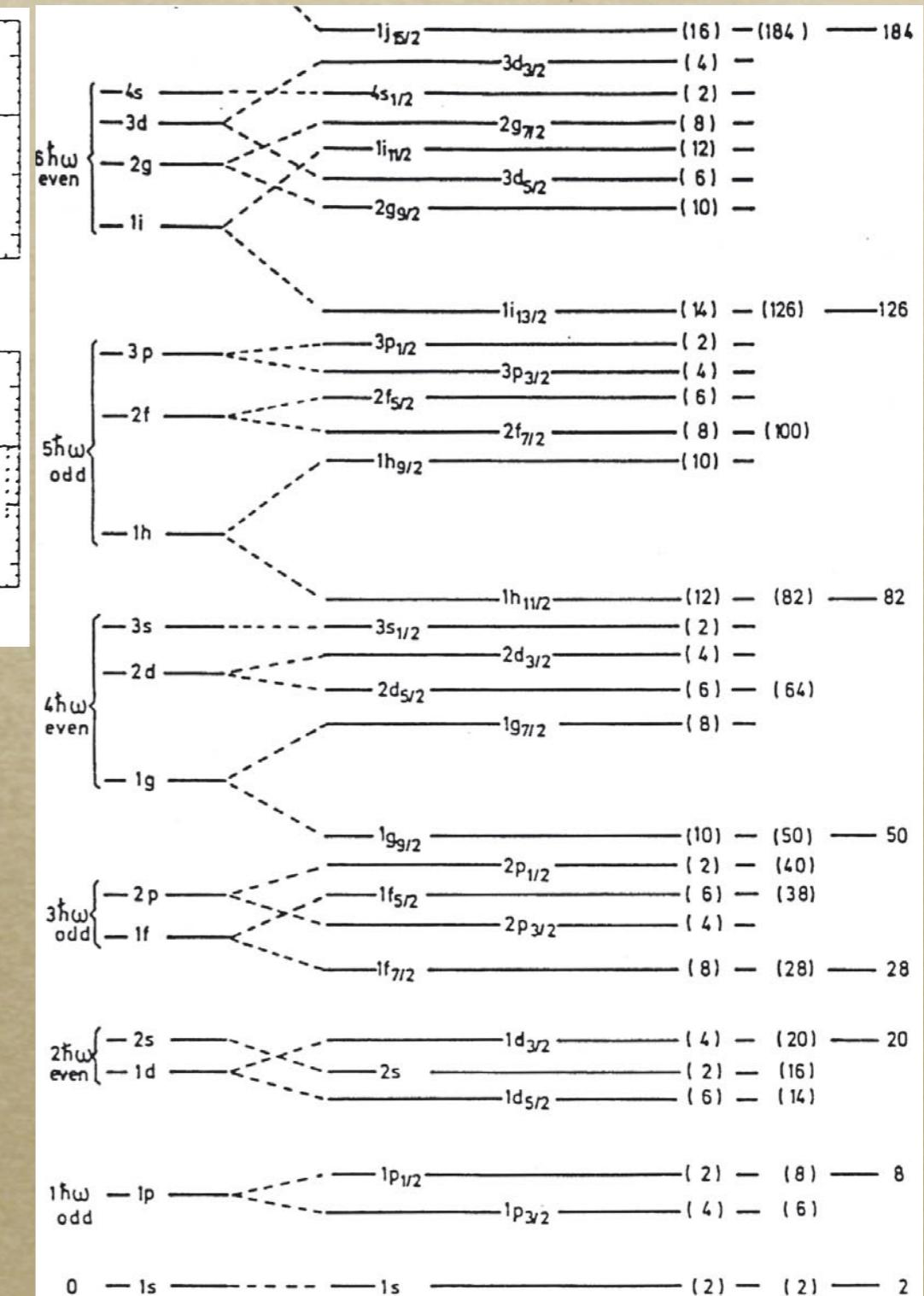
=> related to Gaps in a quantum system

... need right orbital ordering in models

Harm. Osc => not good gaps

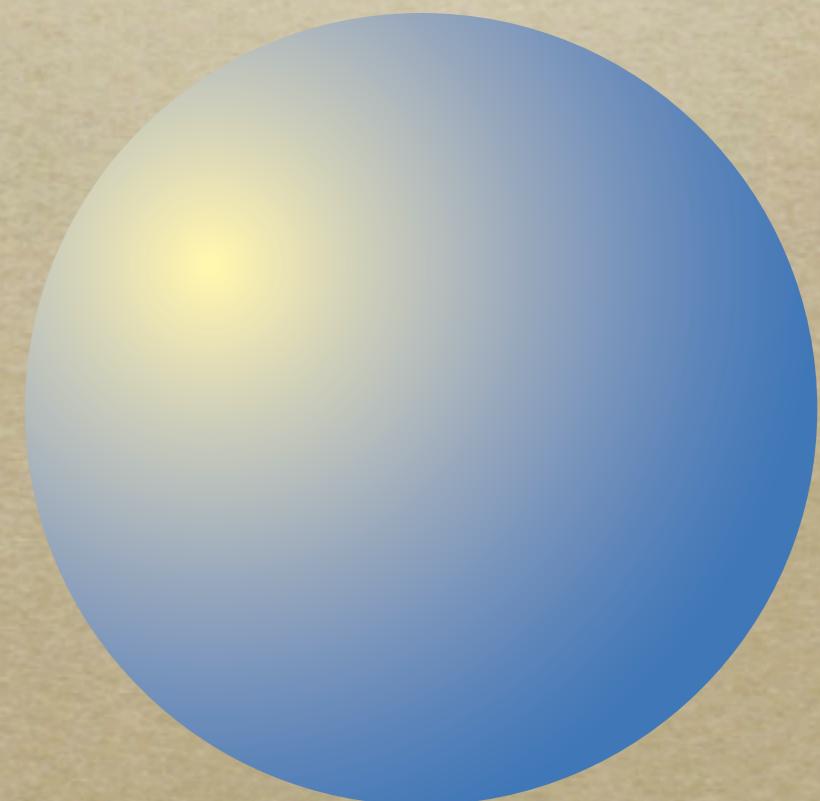
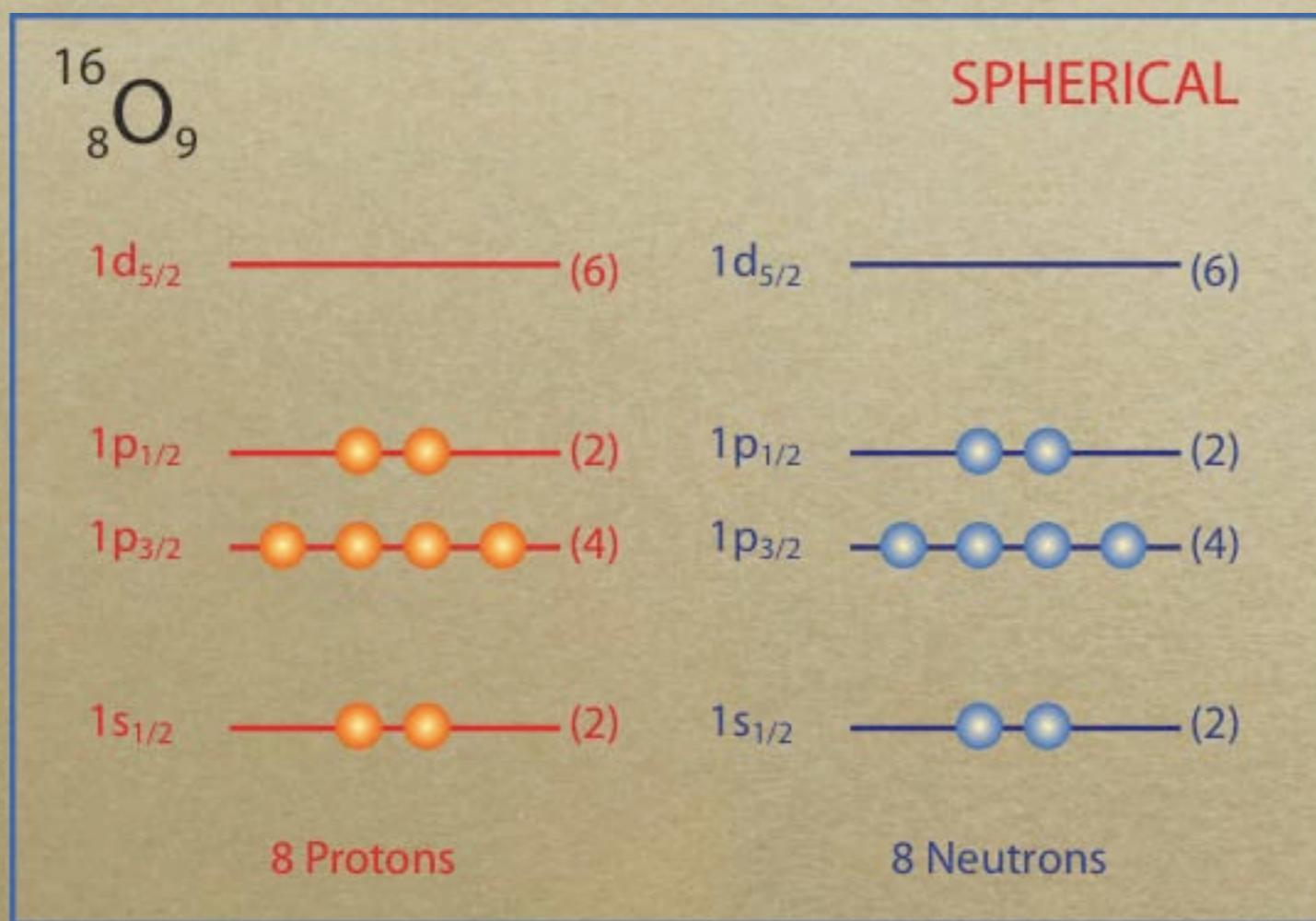
=> add a β^2 term and a λs term

=> new magic numbers (the right ones)



Fill the levels and get a Spherical nuclei ...

Single particle Energies



Fermi levels, Occupancy ...

How to learn more about the properties due to symmetry ?



How to learn more about the
properties due to symmetry ?

Break

it



To break the Symmetries we can act on:

Isospin Content ...

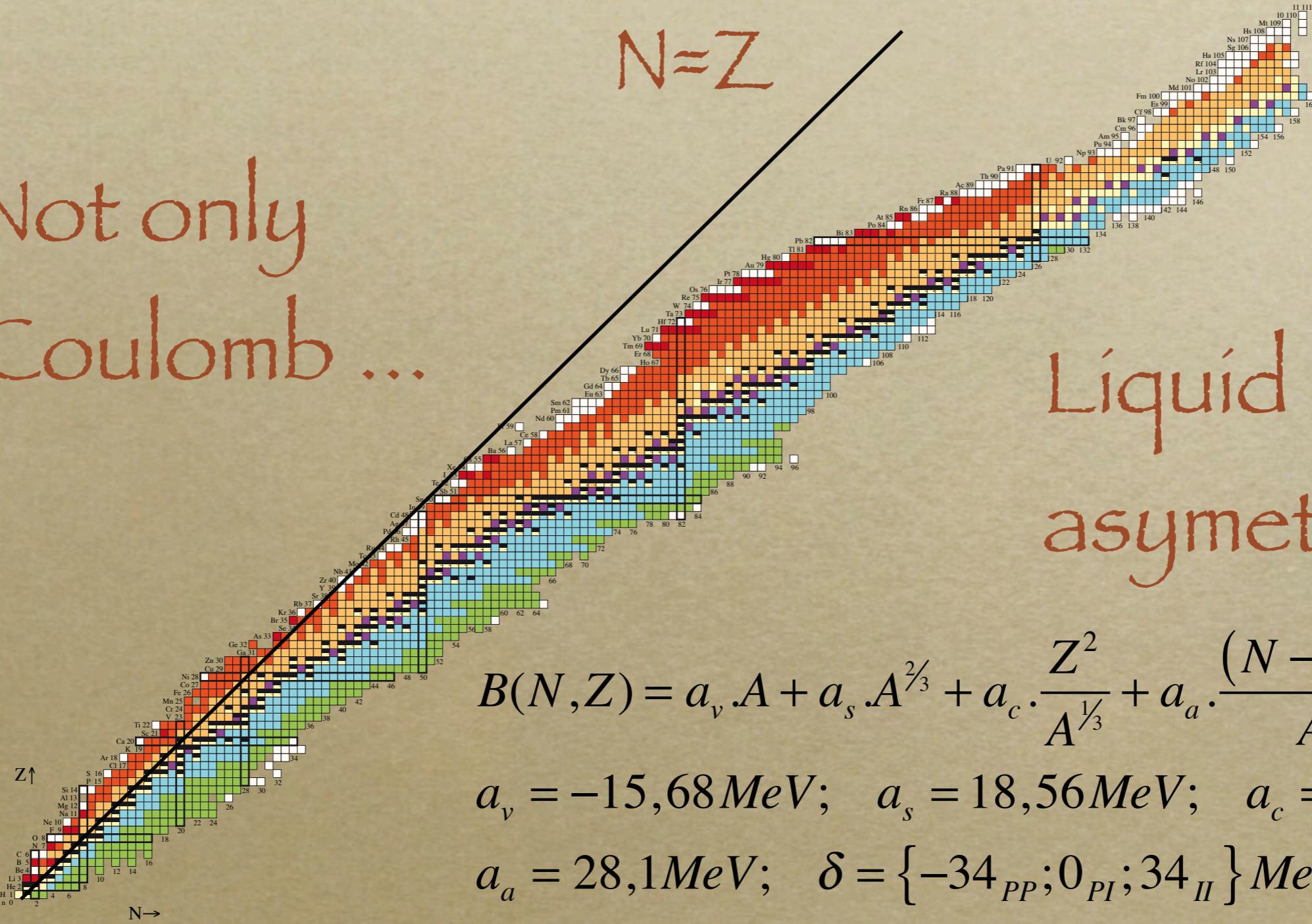
time-reversal ...

deformation ...

Nucleonic content ... Isospin ...

Not only
Coulomb ...

$N = Z$



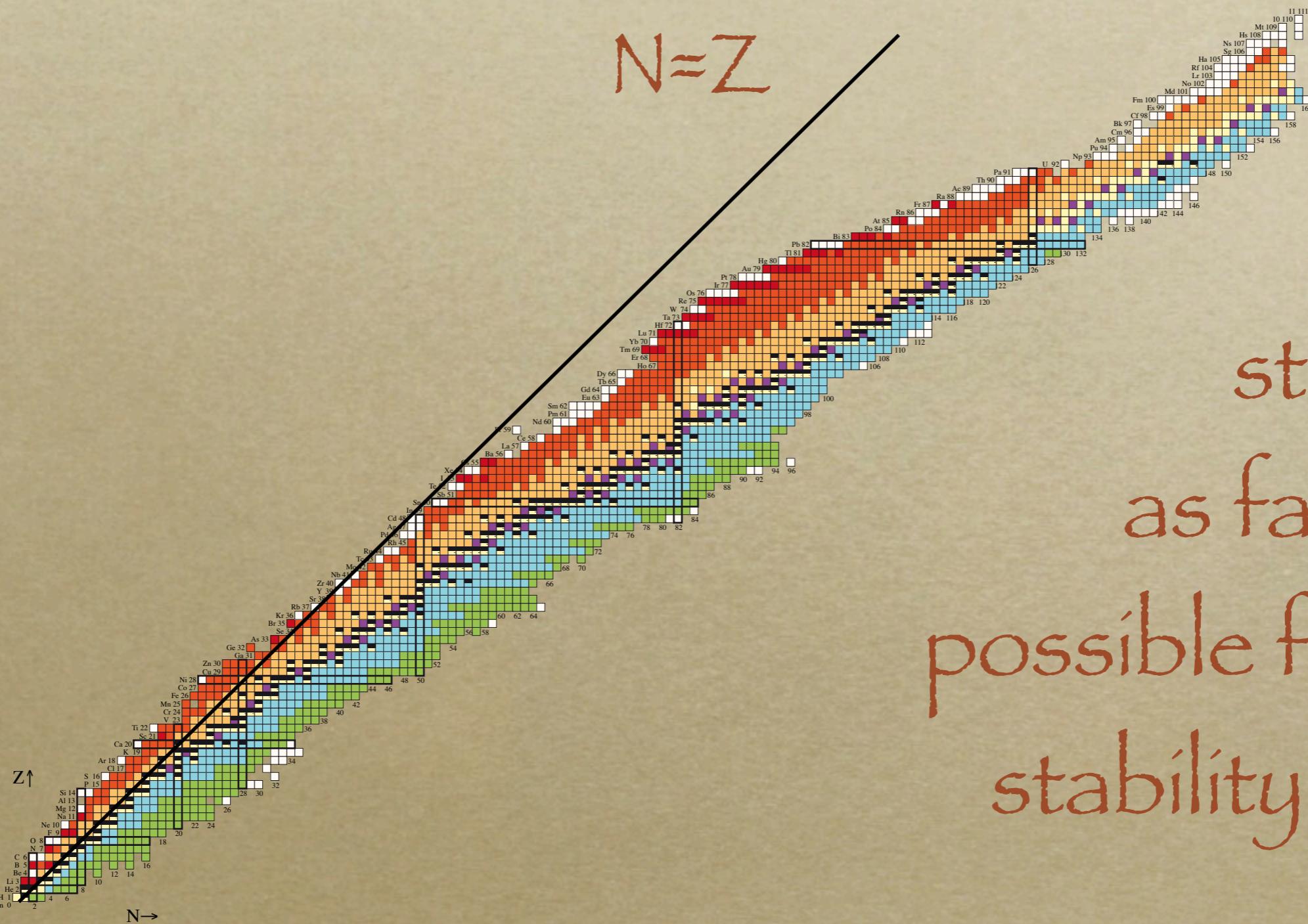
Liquid drop
asymmetry ...

$$B(N, Z) = a_v \cdot A + a_s \cdot A^{\frac{2}{3}} + a_c \cdot \frac{Z^2}{A^{\frac{1}{3}}} + a_a \cdot \frac{(N - Z)^2}{A} + \delta \cdot A^{-\frac{3}{4}}$$

$$a_v = -15,68 \text{ MeV}; \quad a_s = 18,56 \text{ MeV}; \quad a_c = 0,717 \text{ MeV};$$

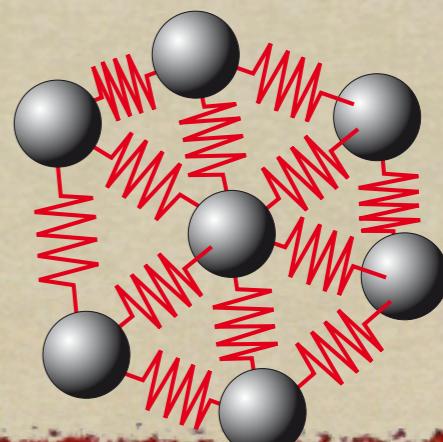
$$a_a = 28,1 \text{ MeV}; \quad \delta = \{-34_{PP}; 0_{PI}; 34_{II}\} \text{ MeV}$$

Far far away ...

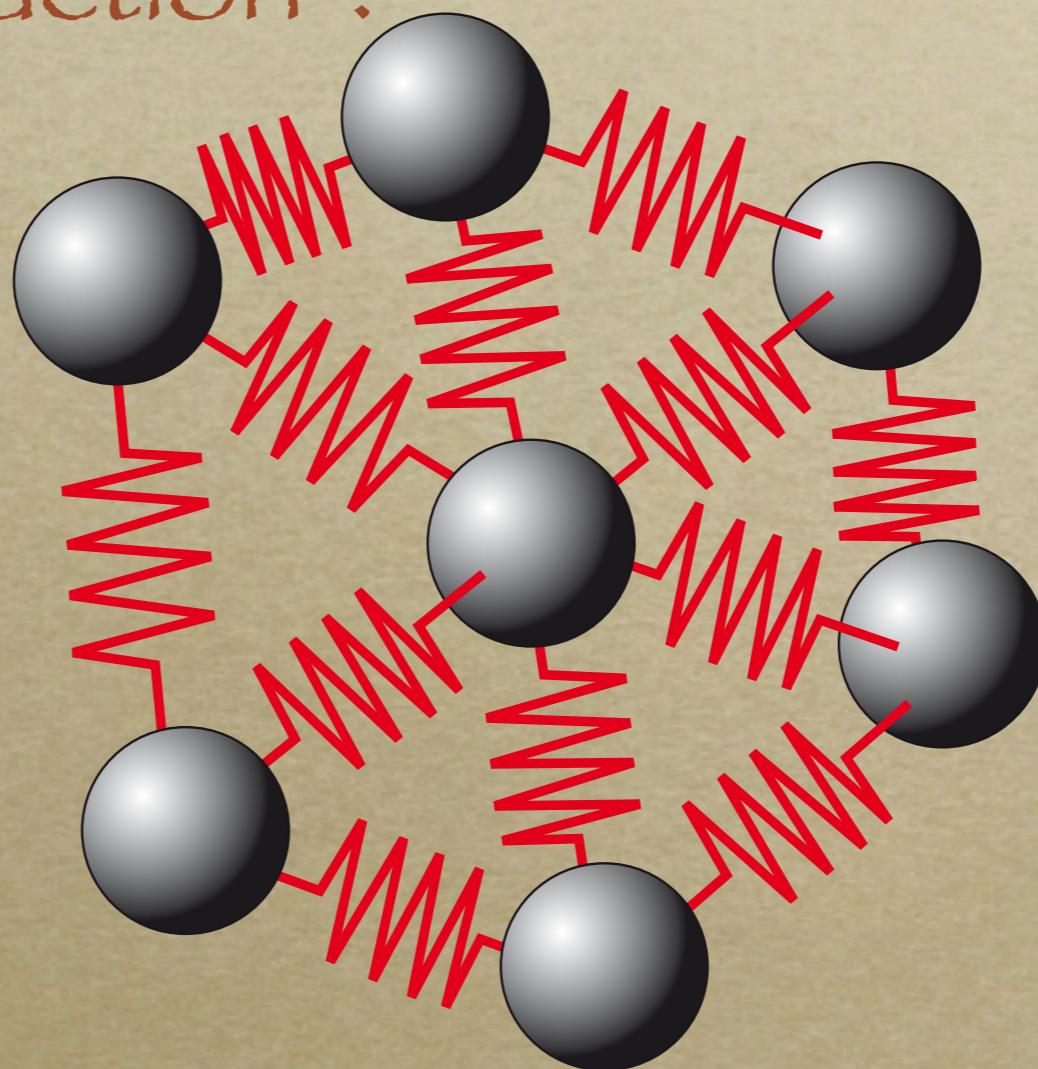


study
as far as
possible from
stability line

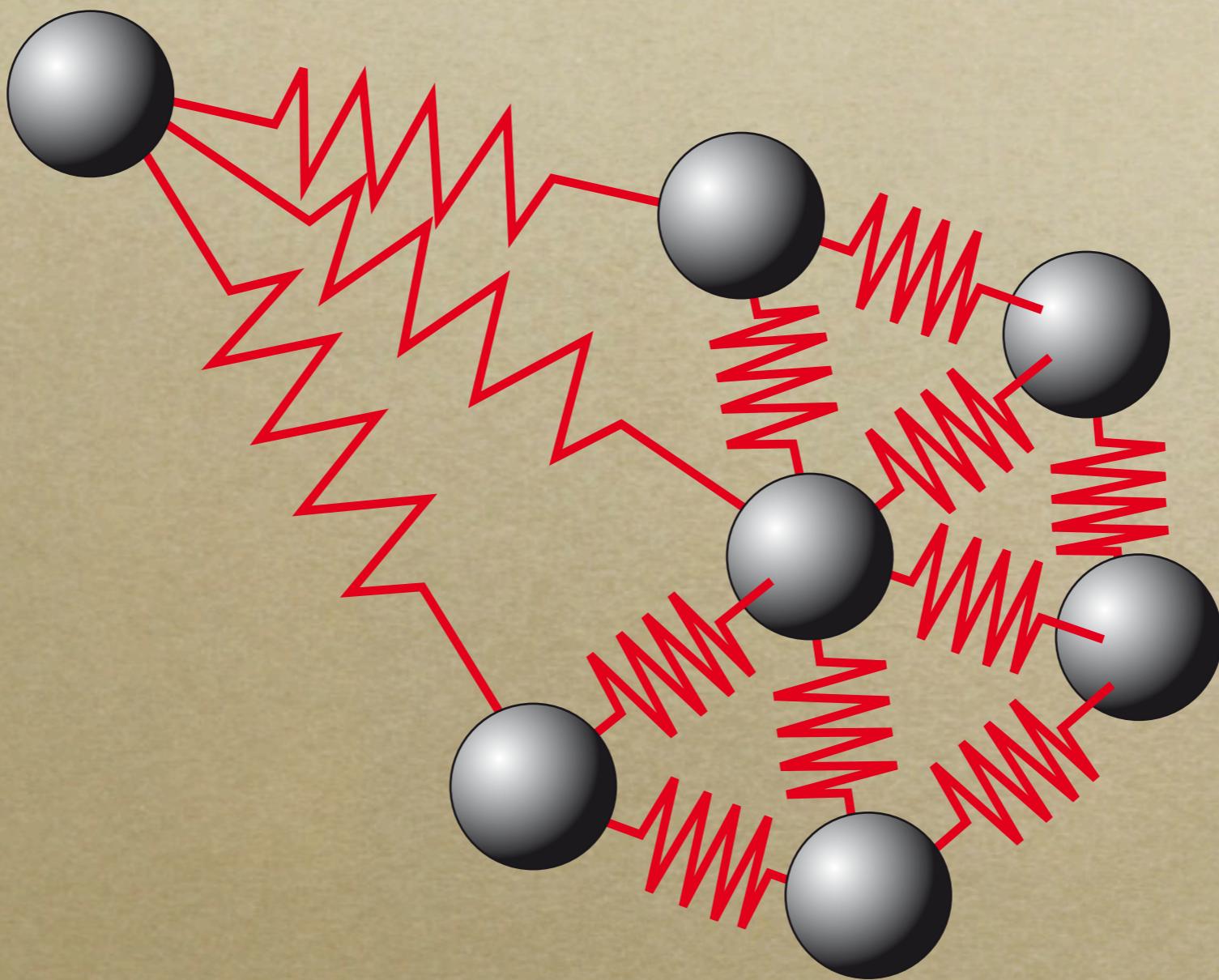
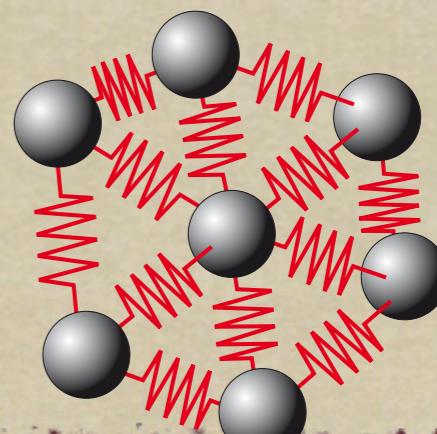
Self Consistency



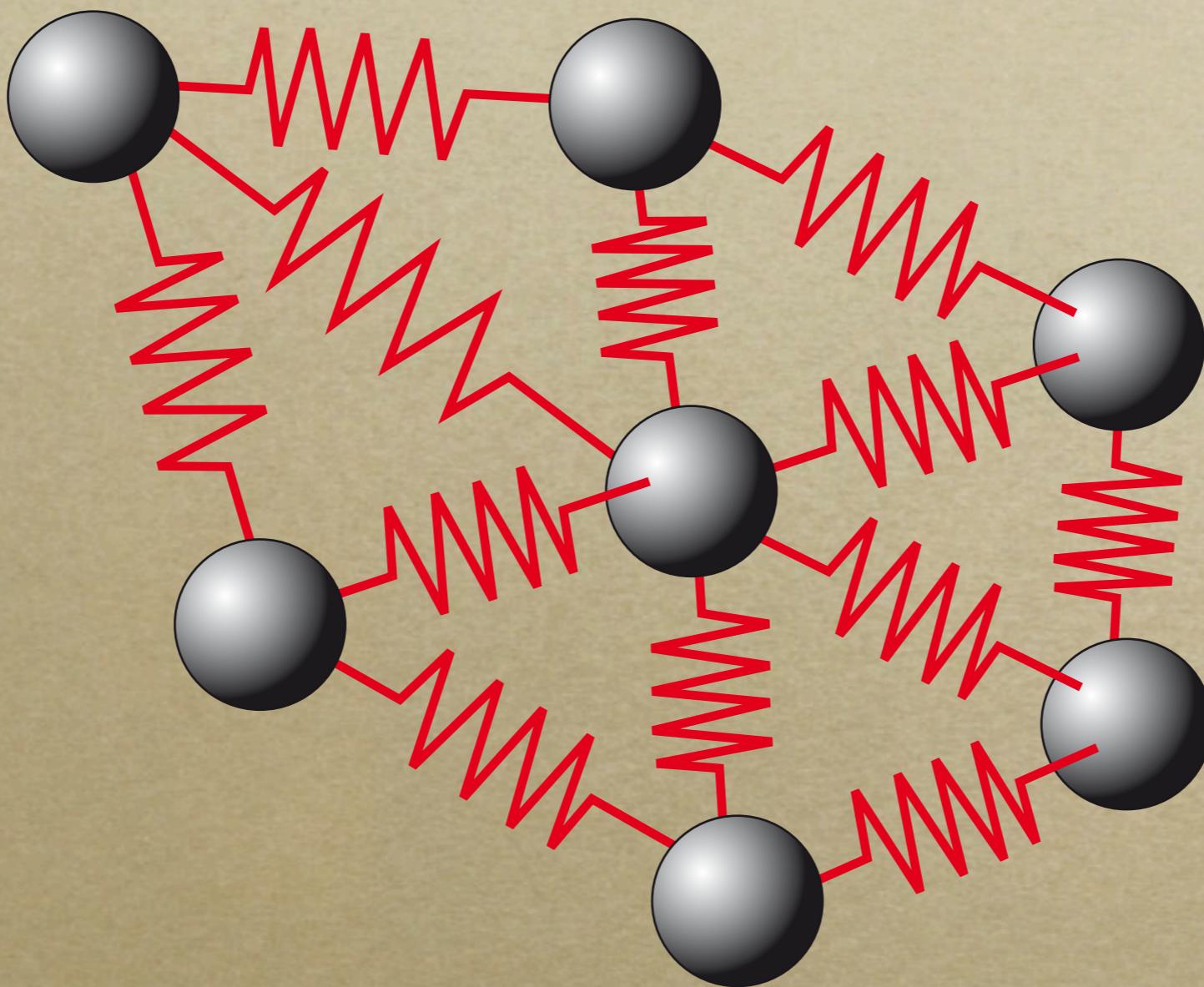
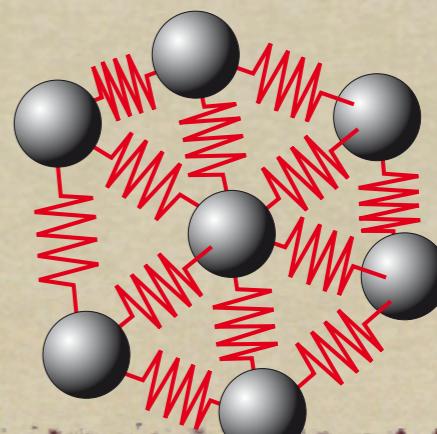
If I act on a single nucleon
What is the core reaction ?



Self Consistency



Self Consistency



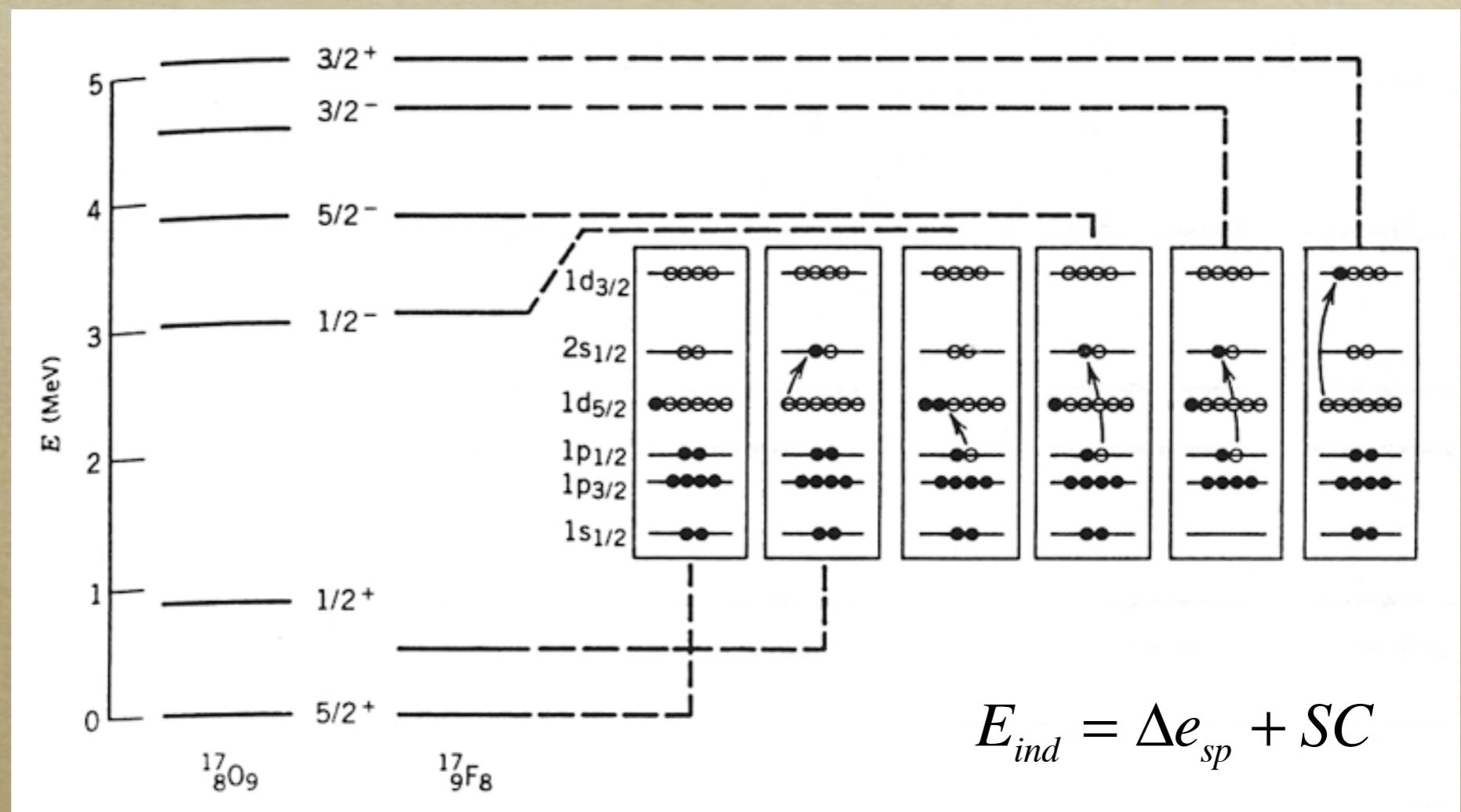
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- ⦿ Effect of Nuclear deformation
- ⦿ Experimental toolboxes & selected cases

Excitations of nucleus

Individual Excitations

single particle
excitations



Collective Excitations

Rotation

$$E_{rot} = \frac{\hbar^2}{2\mathfrak{J}} J(J+1)$$

Vibration

$$E_{vibr} = (N + \frac{3}{2})\hbar\omega$$

Excitations of nucleus

¹⁵²Dy case :
shape coexistence

Collective
Excitations
Vibration

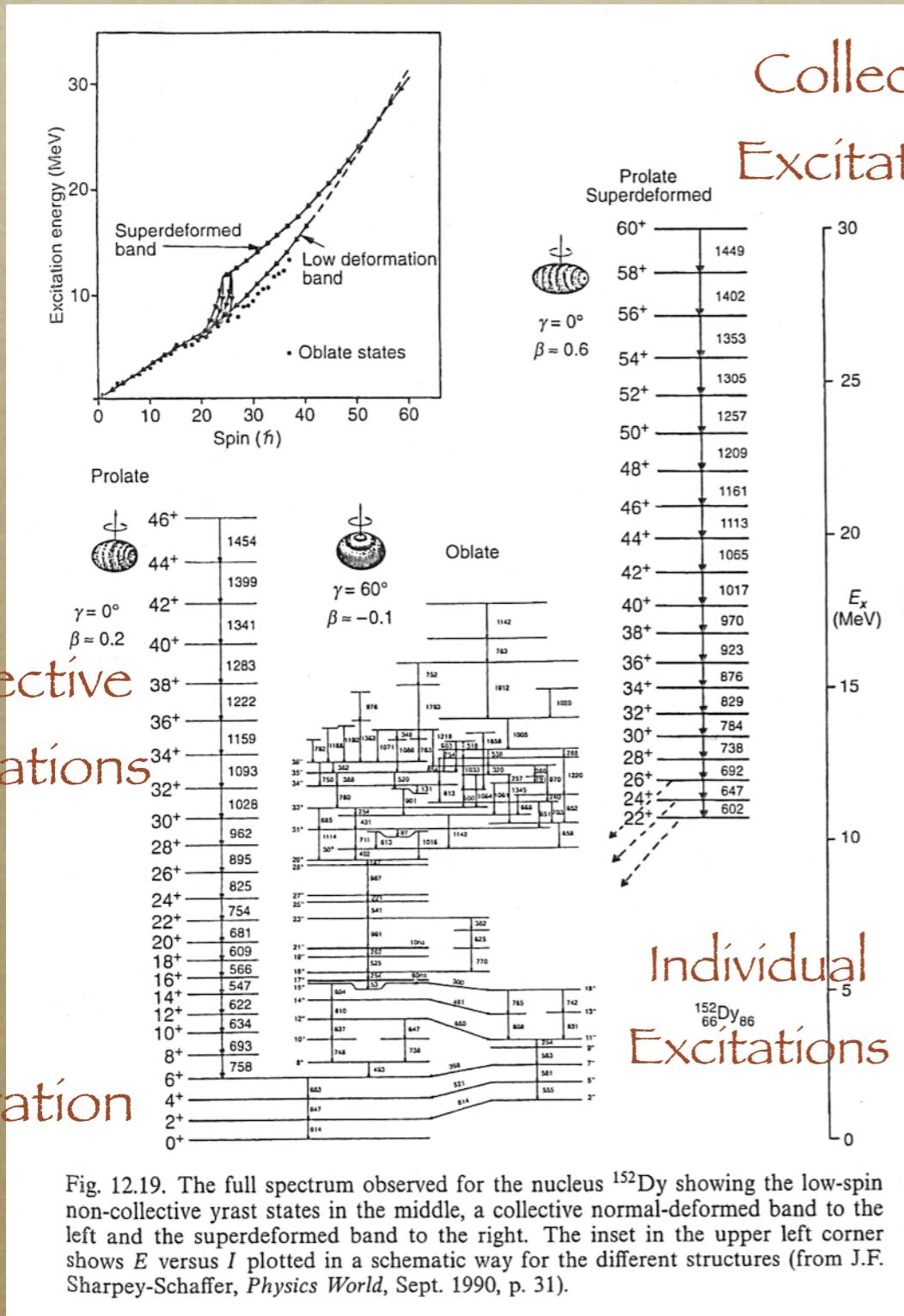


Fig. 12.19. The full spectrum observed for the nucleus ^{152}Dy showing the low-spin non-collective yrast states in the middle, a collective normal-deformed band to the left and the superdeformed band to the right. The inset in the upper left corner shows E versus I plotted in a schematic way for the different structures (from J.F. Sharpey-Schaffer, *Physics World*, Sept. 1990, p. 31).

Collective
Excitations

Individual
Excitations

Rotationnal band

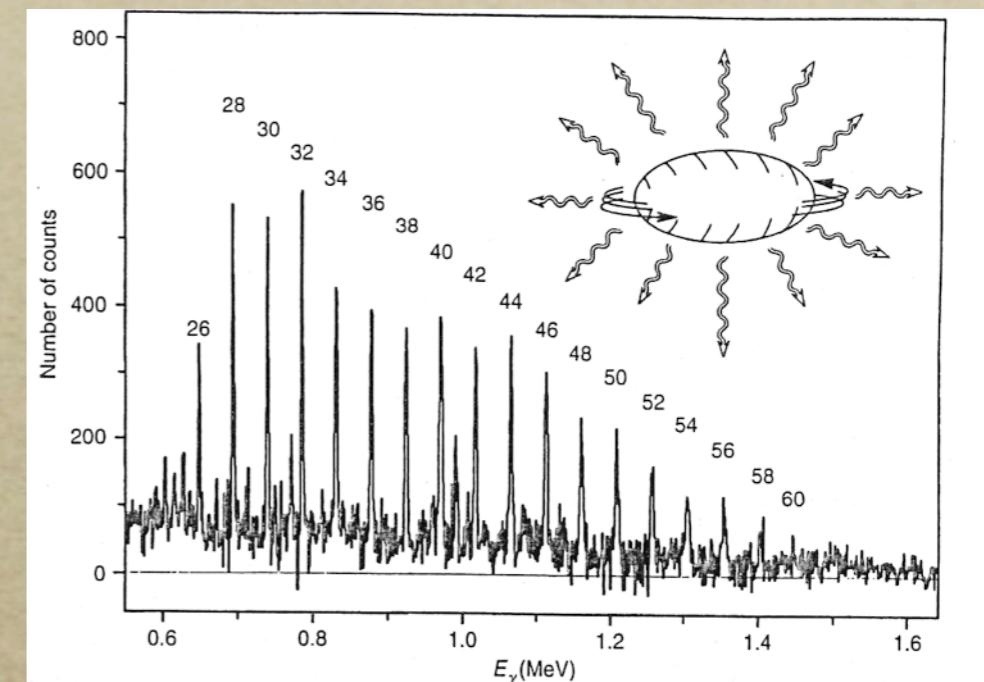


Fig. 12.18. The gamma-ray spectrum of the superdeformed band in ^{152}Dy as originally identified in the 1986 Daresbury experiment (from Twin *et al.*, 1986).

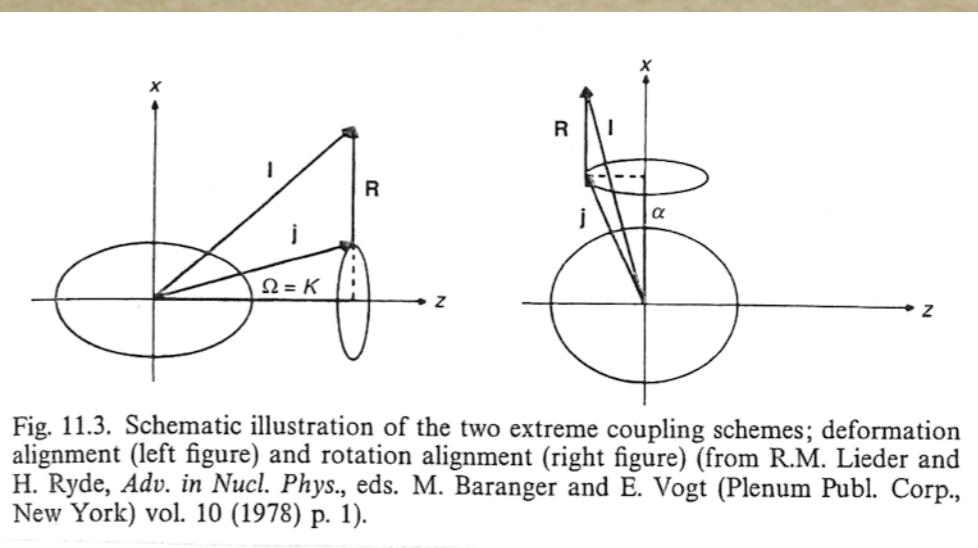
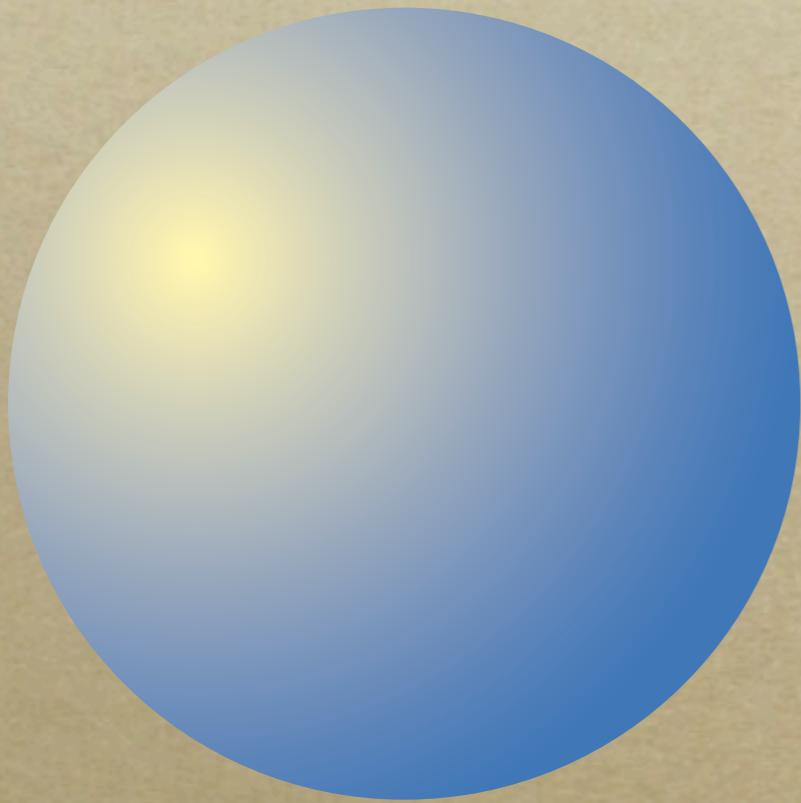


Fig. 11.3. Schematic illustration of the two extreme coupling schemes; deformation alignment (left figure) and rotation alignment (right figure) (from R.M. Lieder and H. Ryde, *Adv. in Nucl. Phys.*, eds. M. Baranger and E. Vogt (Plenum Publ. Corp., New York) vol. 10 (1978) p. 1).

Nuclear Rotation



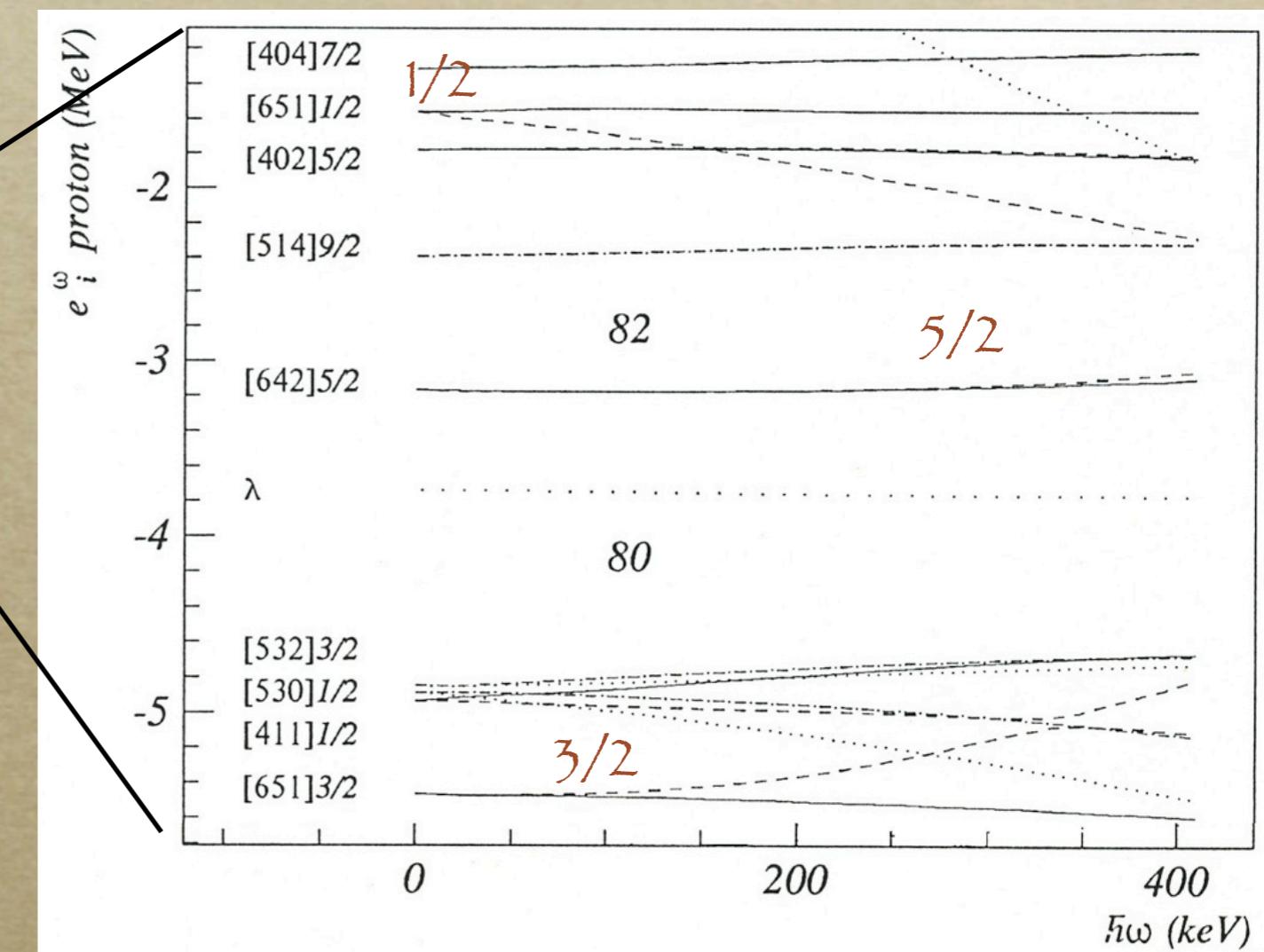
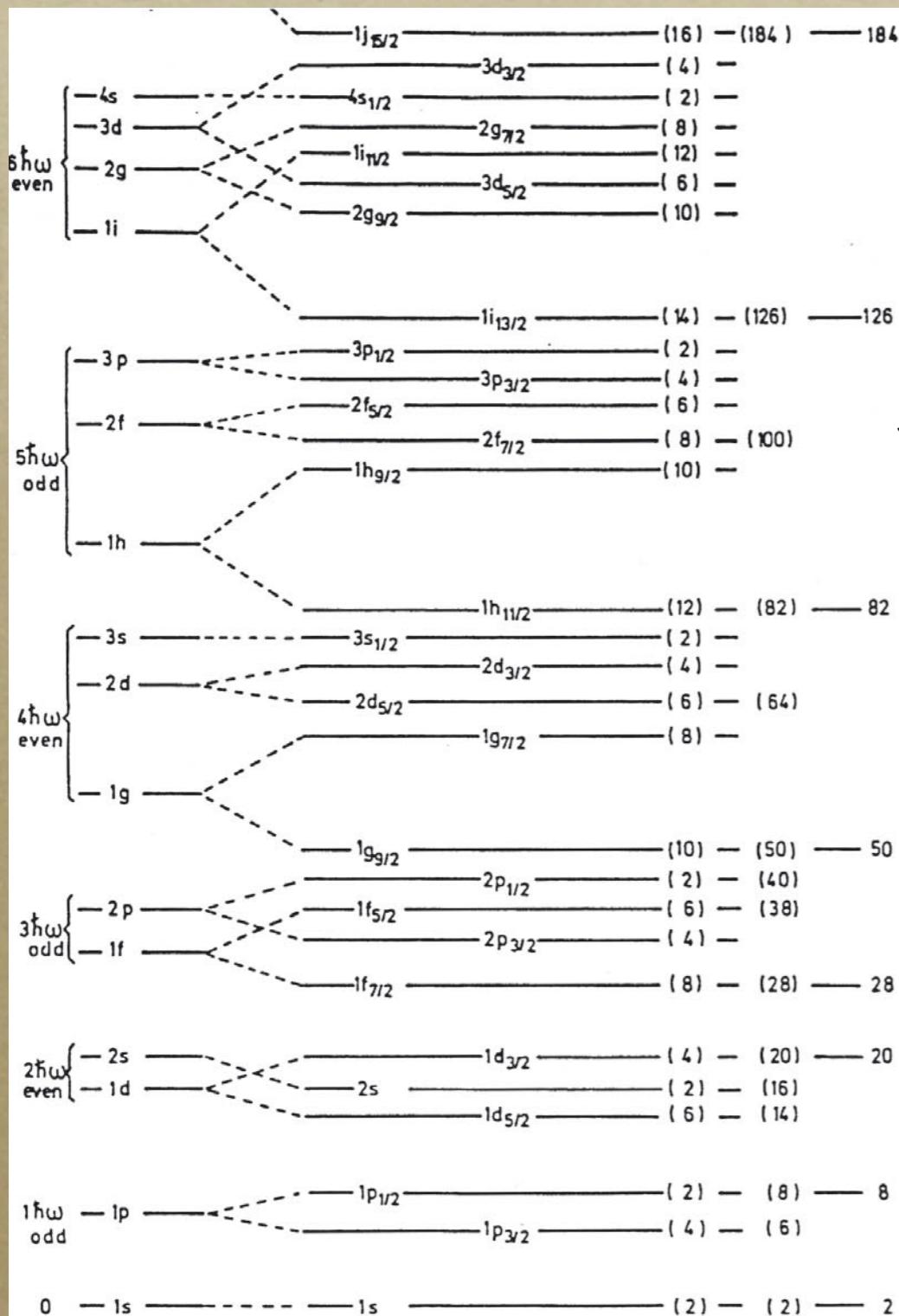
<= perfect sphere

What are the symmetry axes ?
Can we see rotation ?

NO ... because it is

Forbidden by Quantum Mechanics ! ...

Effect of rotation on e_{sp}



Breaks the time-reversal symmetry ...

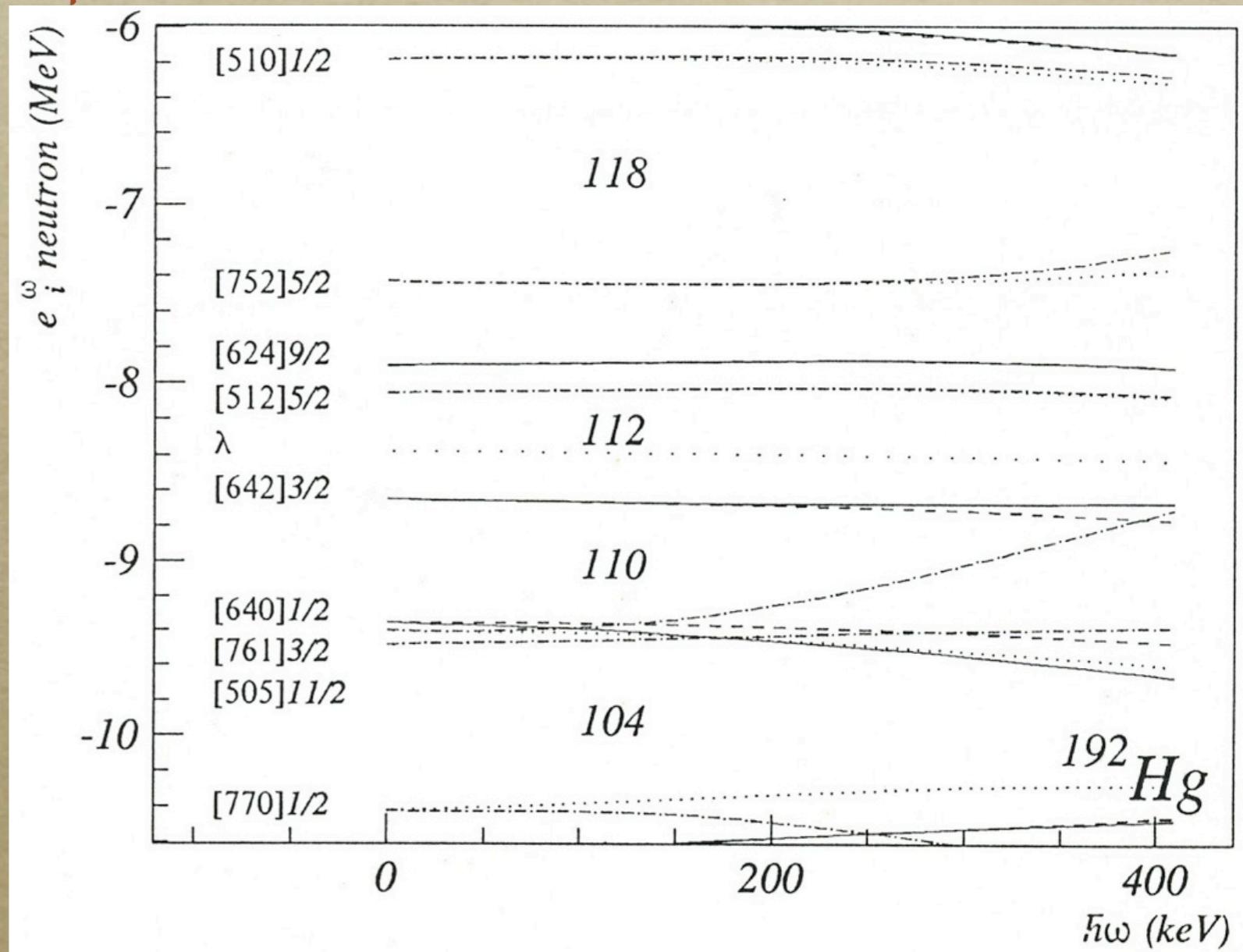
Theoretical Routhians e_{qp}

Due to pairing correlations, each sp level has a given occupancy
You can empty or fill each sp level around Fermi

keep track of
the origin of the
orbital through a
labelling:

- p “particle state”
- h “hole state”

Pairing GAP is
reduced by Coriolis
Anti-Pairing effect



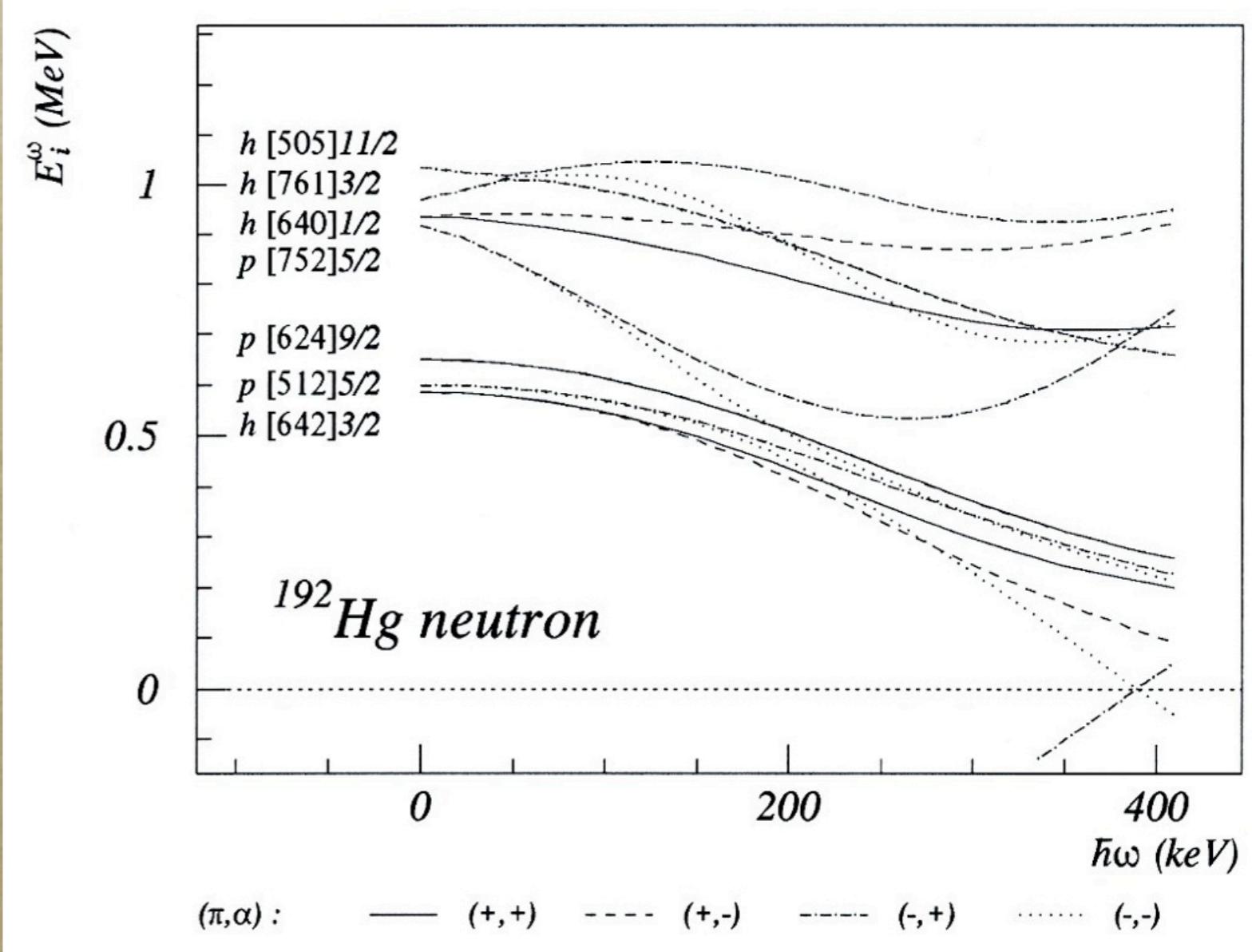
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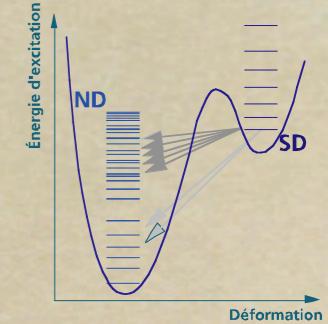
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Pairing GAP is
reduced by Coriolis
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Experimental Routhians



$$\text{Routhian} : E'(\hbar\omega) = E(\hbar\omega) - E_{rot}(\hbar\omega)$$

Considered band

If not constant, shows that the nucleus is not rigid ...

In order to see the effect of individual orbitals we need to subtract a core

Effect of Rotation



$$E_{rot}(\hbar\omega) = \hbar\omega\sqrt{J(J+1) - K^2}$$

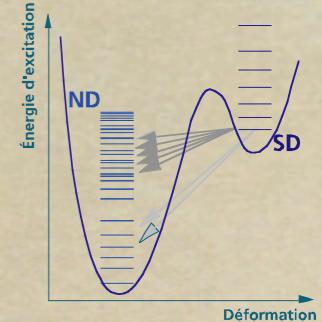
$$\hbar\omega = \frac{dE_{rot}}{dJ}$$

$$\hbar\omega \approx \frac{\Delta E}{\Delta J} = \frac{E(J+2) - E(J)}{(J+2) - J} = \frac{E_\gamma}{2}$$

$$\text{Subtracted Routhian} : e' = E'(\hbar\omega) - E_{ref}(\hbar\omega)$$

Core

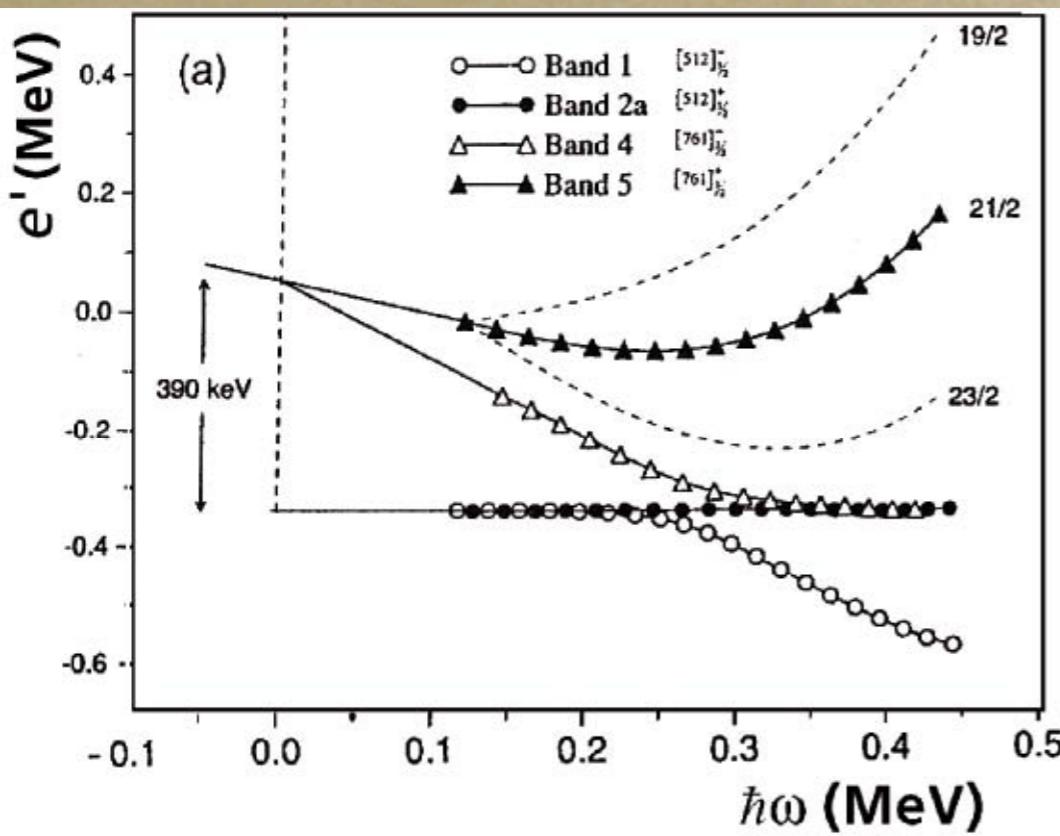
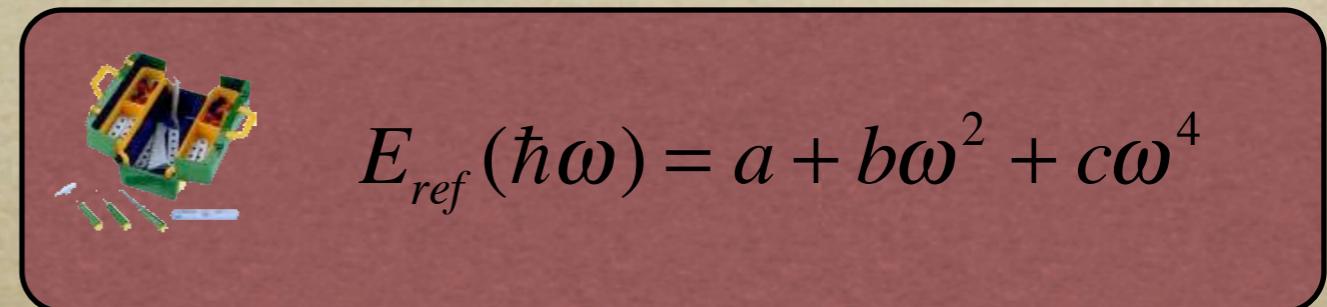
Experimental Routhians



Subtracted Routhian : $e' = E'(\hbar\omega) - E_{ref}(\hbar\omega)$

Example :

Spectroscopy of the odd-even nuclei ^{193}Hg

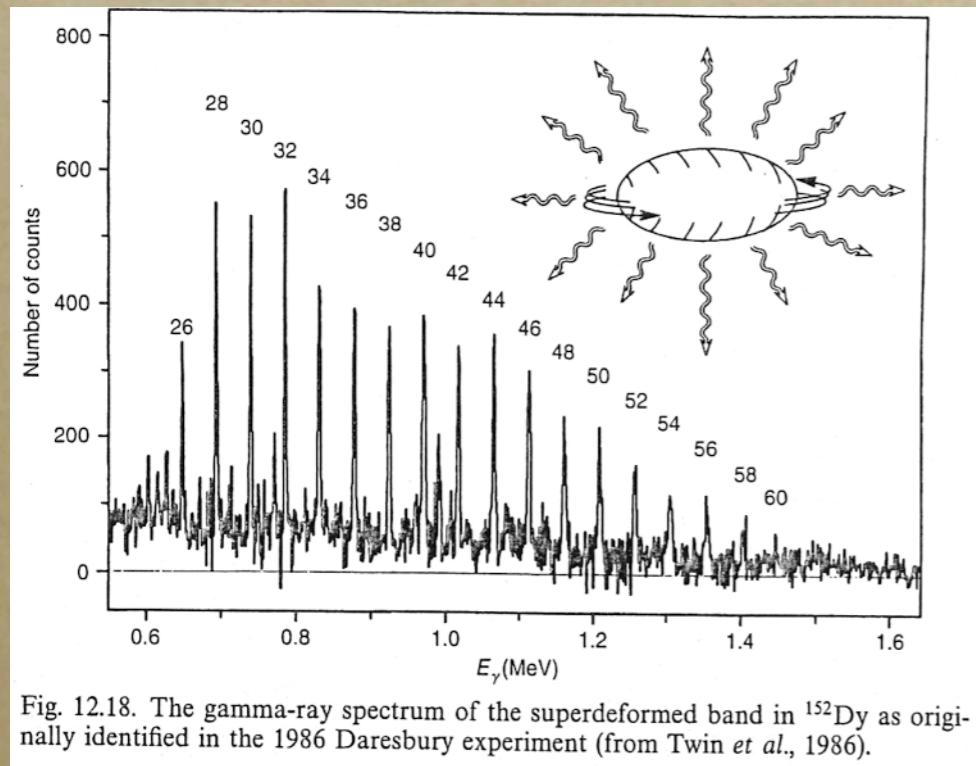


M.J. Joyce et al. Phys Rev. Lett. 71, 2176 (1993)

- » Intensity splitted over several bands
 - » The bands are linked together
 - » Study of Routhians
- Possibility to extract experimental quasi-particle routhians

Inertia and Rigid Rotor

$$E_{rot} = \frac{\hbar^2}{2\mathfrak{I}} J(J+1) \quad \text{corresponds for an even-even to} \quad E_{classical} = \frac{\hbar^2 I^2}{2\mathfrak{I}}$$

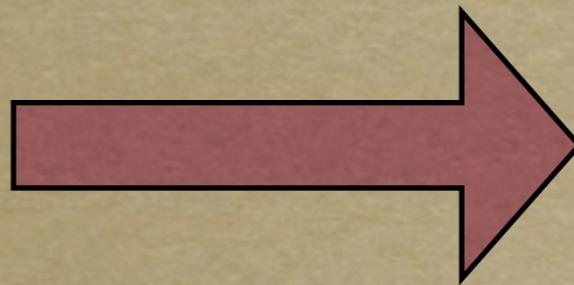


$$\mathfrak{I}_{rigid} = \frac{2}{5} MR^2 (1 + 0,31\beta)$$

$$\mathfrak{I}^{(1)} = \frac{\hbar^2}{2} \left(\frac{dE}{d(I^2)} \right)^{-1}$$

$$\mathfrak{I}^{(2)} = \hbar^2 \left(\frac{d^2 E}{dI^2} \right)^{-1}$$

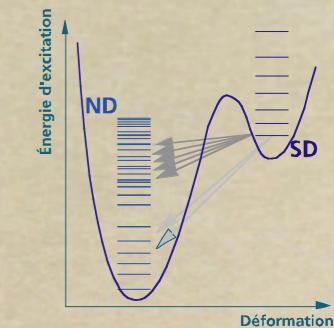
Inertia much smaller
than Rigid rotor



due to superfluidity

Nuclear Pairing dependance on

Rotation



Spectroscopy of ^{192}Hg and ^{194}Pb SD bands

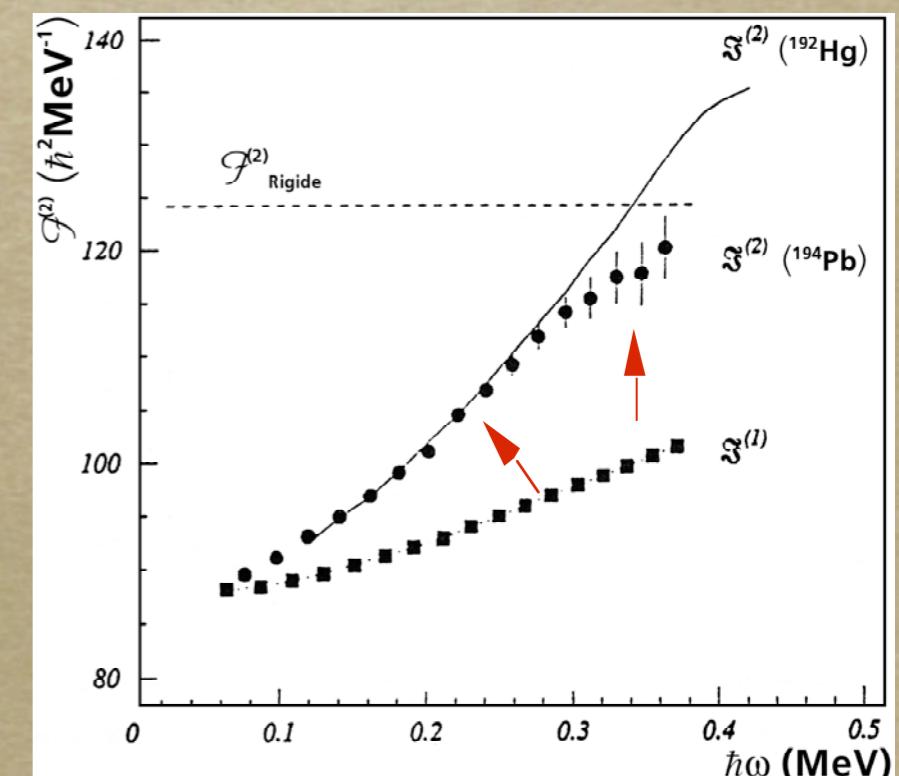
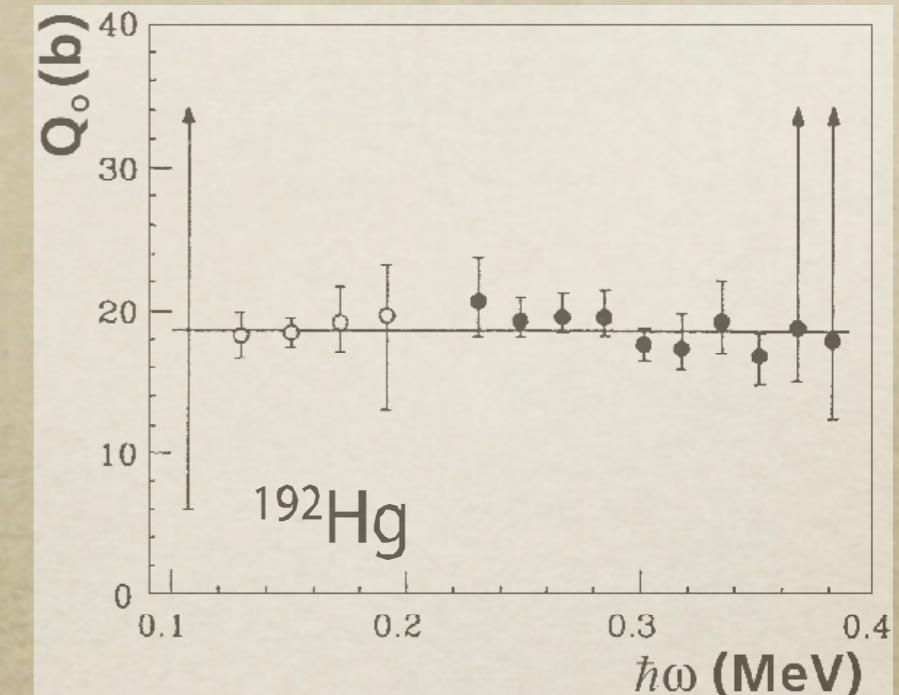
- Constant Quadrupolar Moment
- Dynamical Moment of inertia : $\mathcal{J}^{(2)}$

- » Steady increase
- » Saturation at high Frequency...

Sign of the progressive reduction of
Pairing-Correlations Effects with Rotation

- » Different Saturation for different bands !

Sign of the single particule content of the
nuclei especially in “intruder” orbitals



^{158}Er case : Backbendings

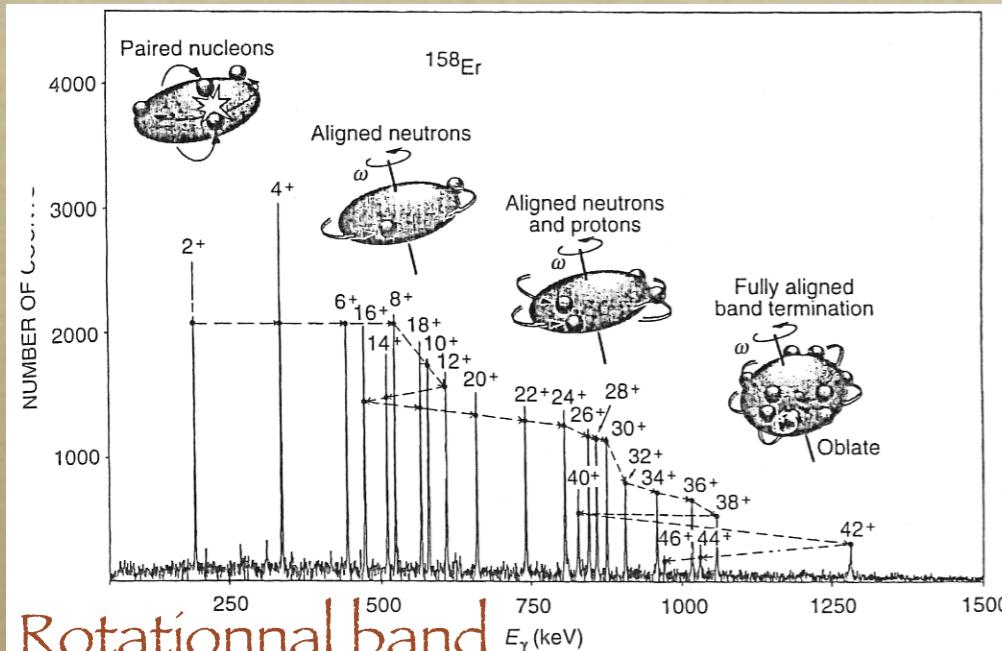
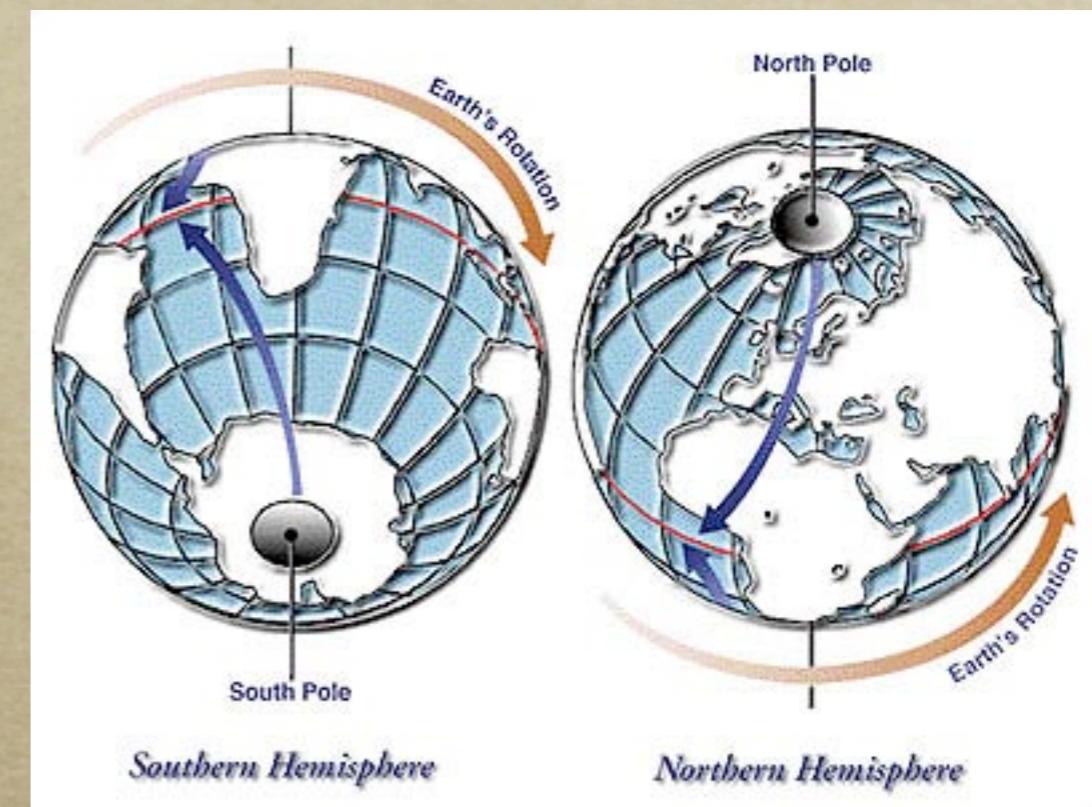


Fig. 11.12. Observed γ -ray energies of ^{158}Er formed in a reaction like the one illustrated in fig. 11.11. For $I \approx 14$ two $i_{13/2}$ neutrons become aligned resulting in a backbend while a second irregularity caused by the alignment of two $h_{11/2}$ protons is seen for $I \approx 32$. The features for $I \geq 38$ with the final band term $I = 46$ are discussed in chapter 12.

Coriolis force

$$\mathbf{F}_C = -2m\Omega \times \mathbf{v}$$



Alignment on rotation

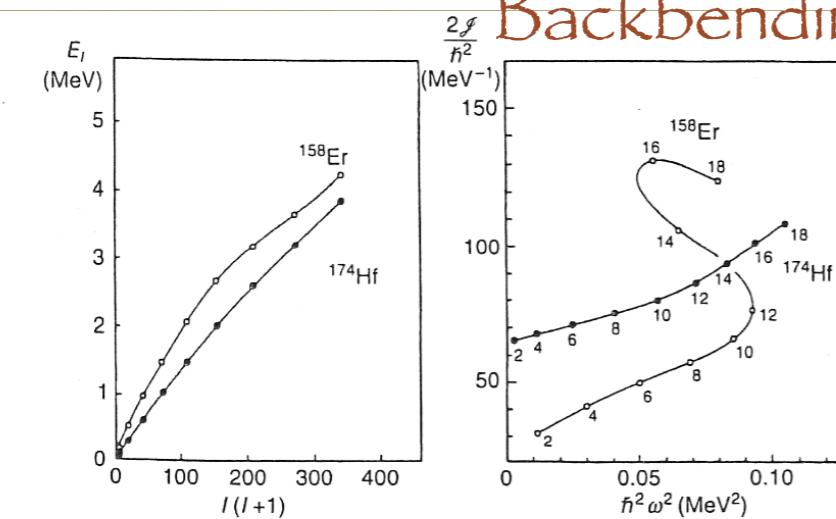


Fig. 11.13. Yrast energies in the $I = 0-18$ range of ^{158}Er and ^{174}Hf plotted versus $I(I+1)$ and corresponding back-bending plots with the moment of inertia J versus squared rotational frequency, ω^2 (from R.M. Lieder and H. Ryde, *Adv. in Nucl. Phys.*, eds. M. Baranger and E. Vogt (Plenum Publ. Corp., New York) vol. 10 (1978))

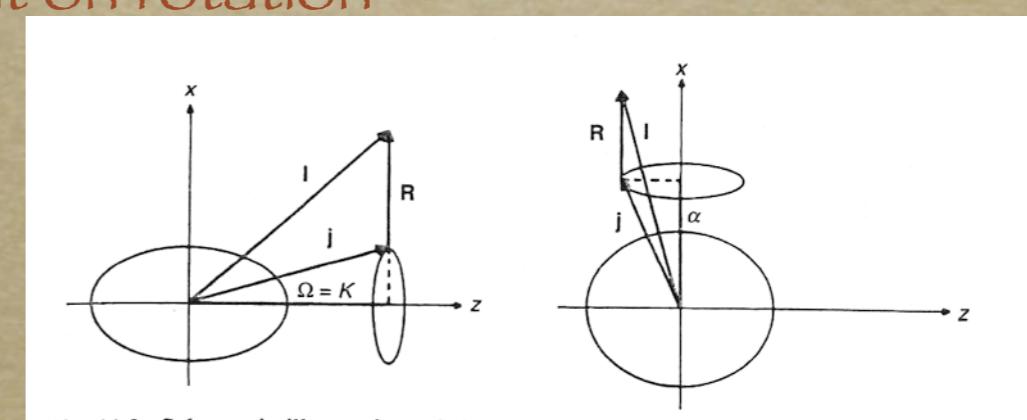
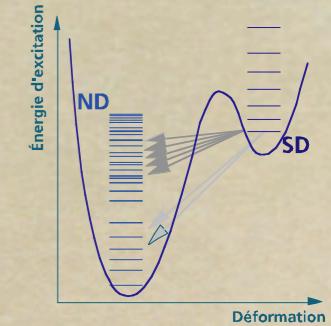


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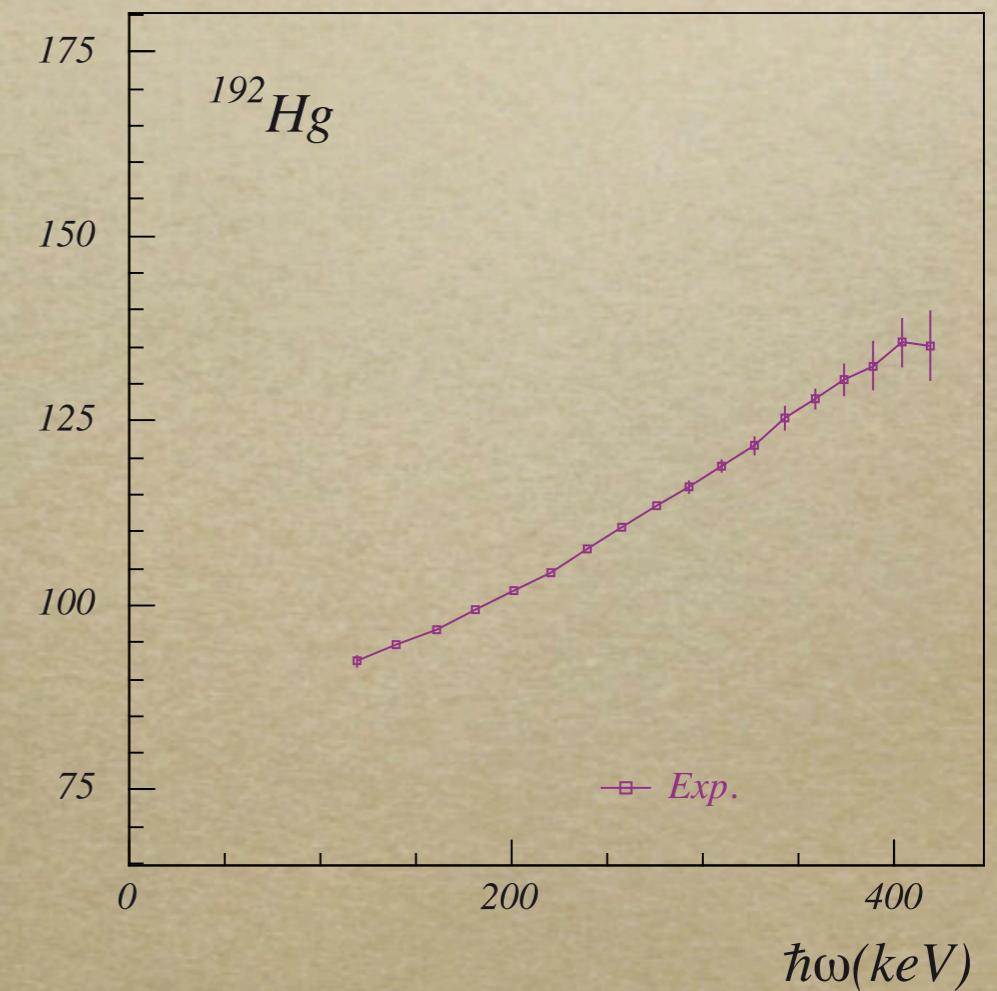
Nuclear Pairing dependance on

Rotation



Cranked Hartree-Fock code

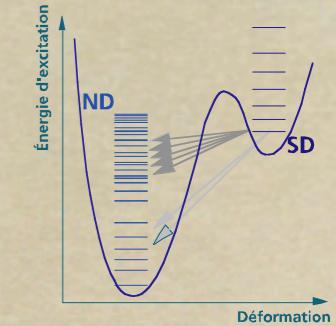
$$\mathcal{J}^{(2)}(\hbar^2 MeV^{-1})$$



($Skm^* + Seniority$ constant G)

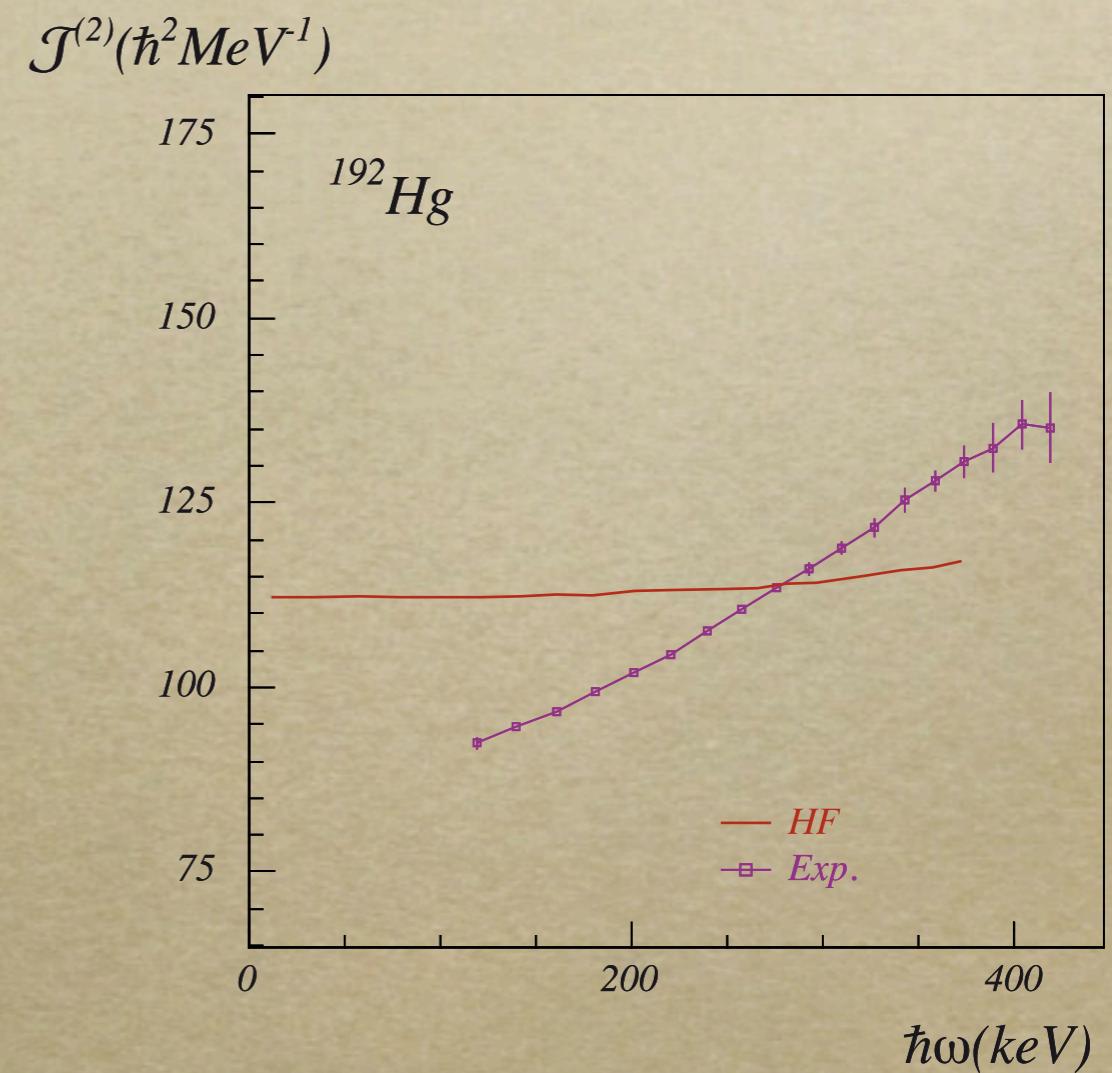
Nuclear Pairing dependance on

Rotation



Cranked Hartree-Fock code

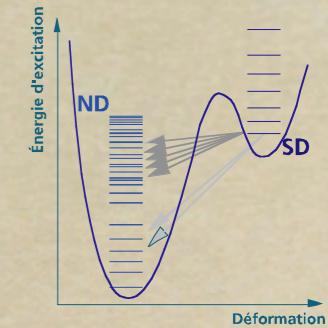
—» Pure HF almost flat



($Skm^* + Seniority$ constant G)

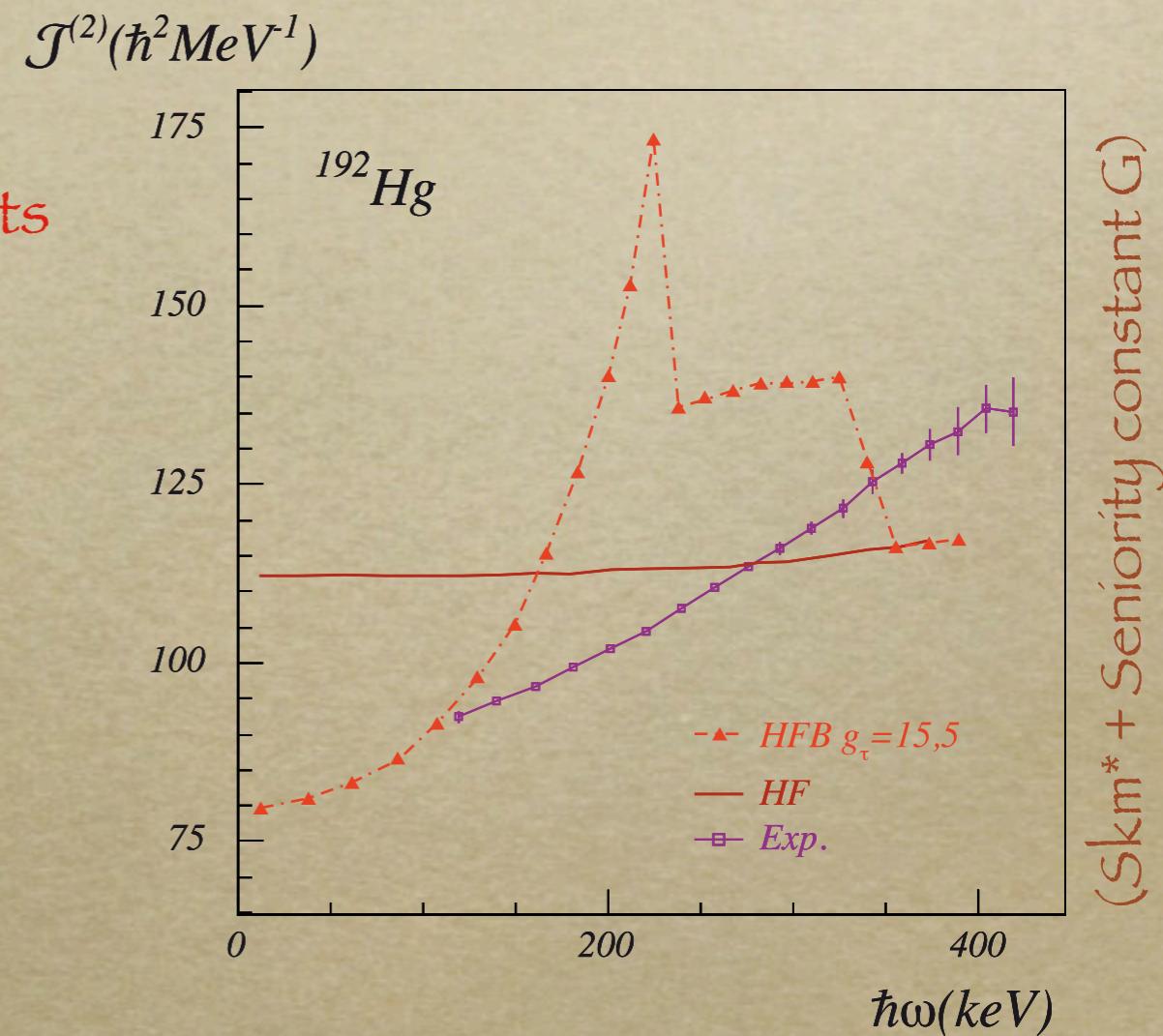
Nuclear Pairing dependance on

Rotation



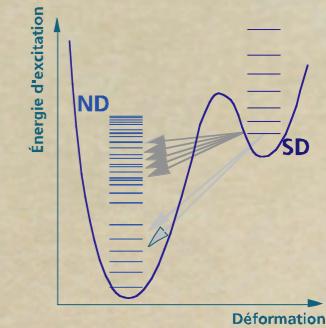
Cranked Hartree-Fock code

- » Pure HF almost flat
- » HFB Steady Increase but also sharp effects
ends on the HF solution at high-spin
...due to Pairing disappearance



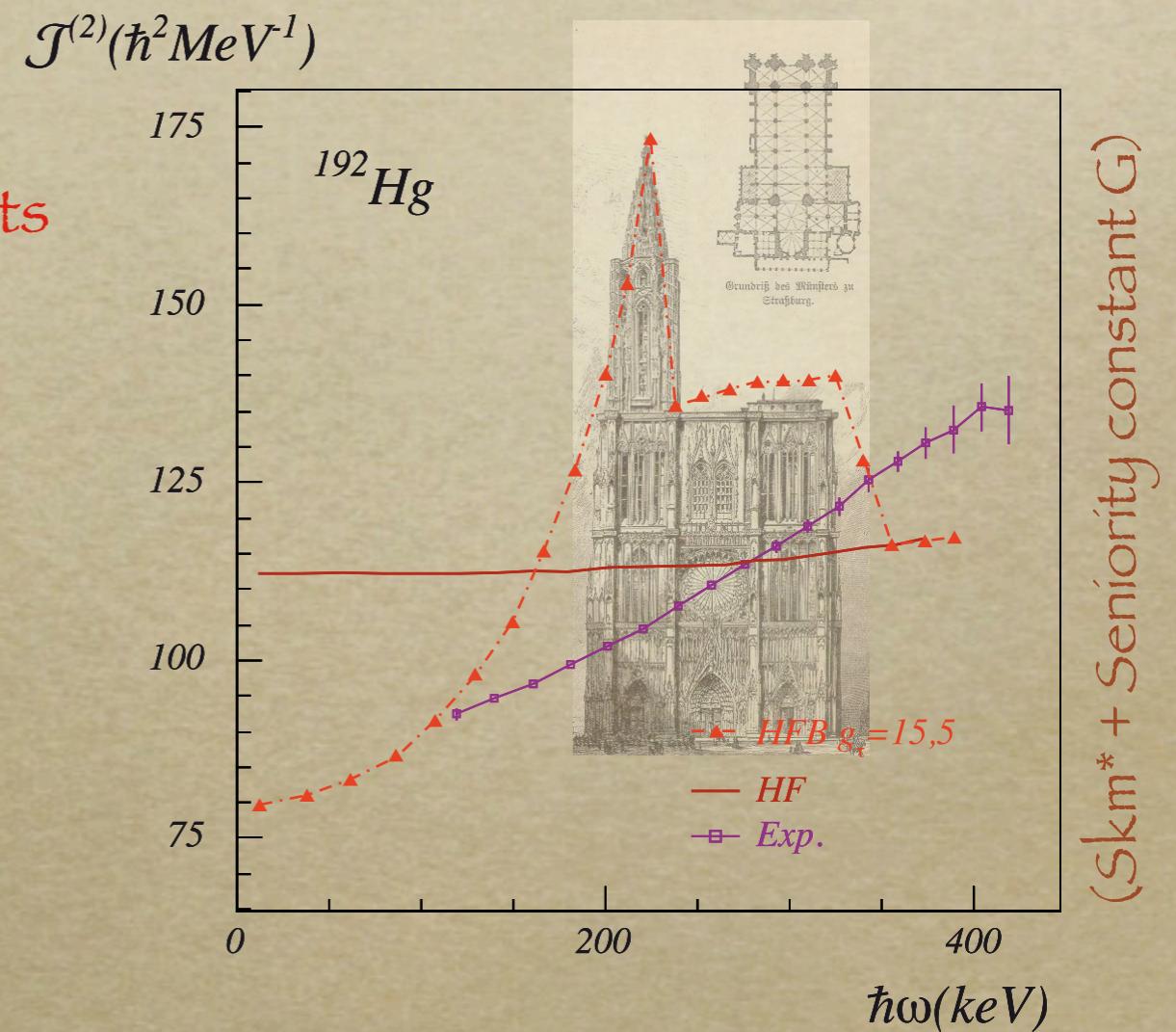
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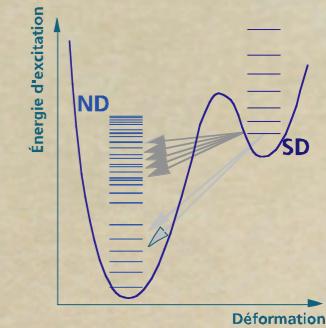
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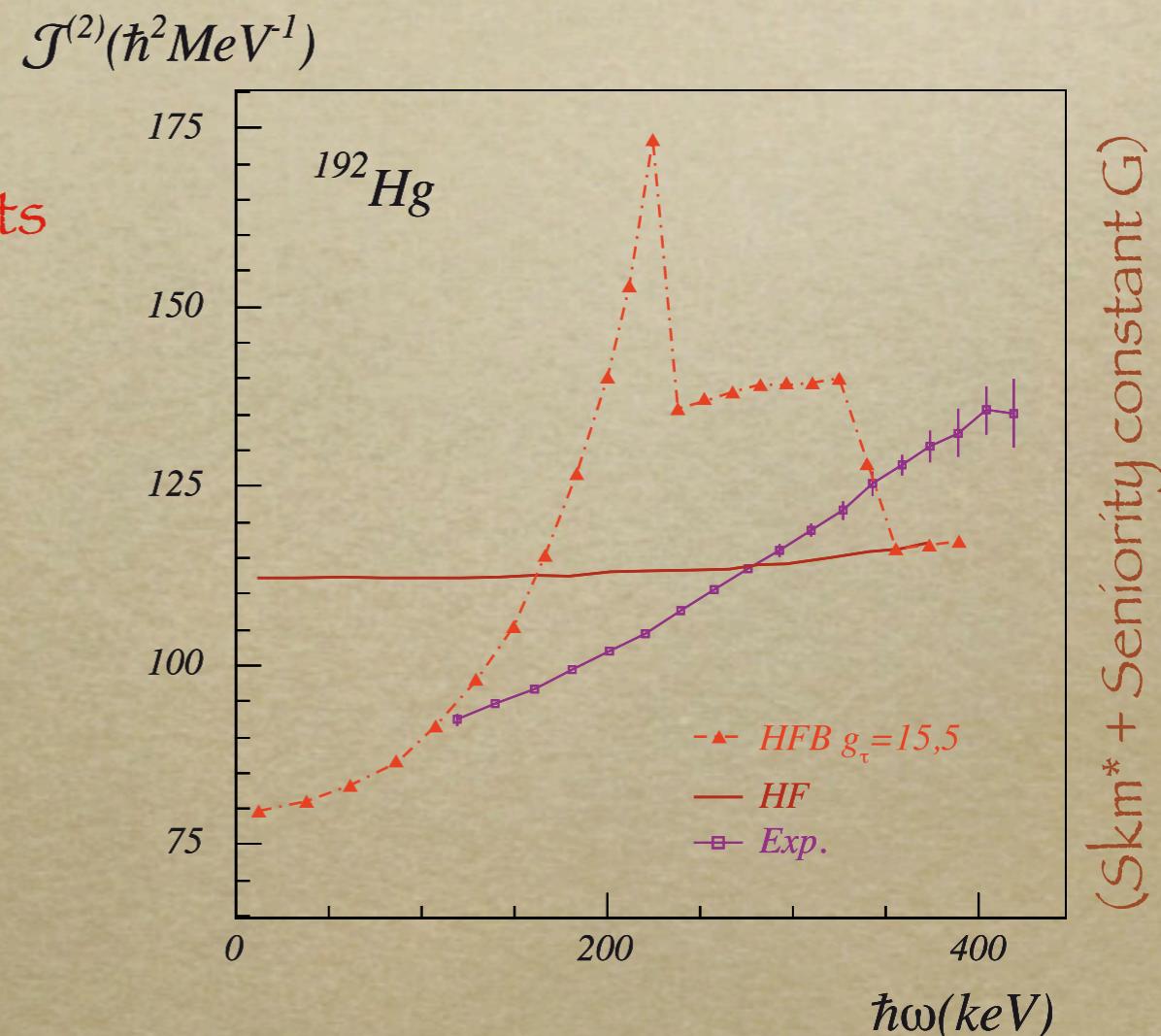
Rotation



Cranked Hartree-Fock code

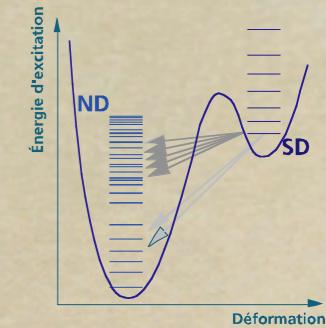
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ends on the HF solution at high-spin
...due to Pairing disappearance

Signature of the pairing content and
underlying Single-Particles orbitals



Nuclear Pairing dependance on

Rotation

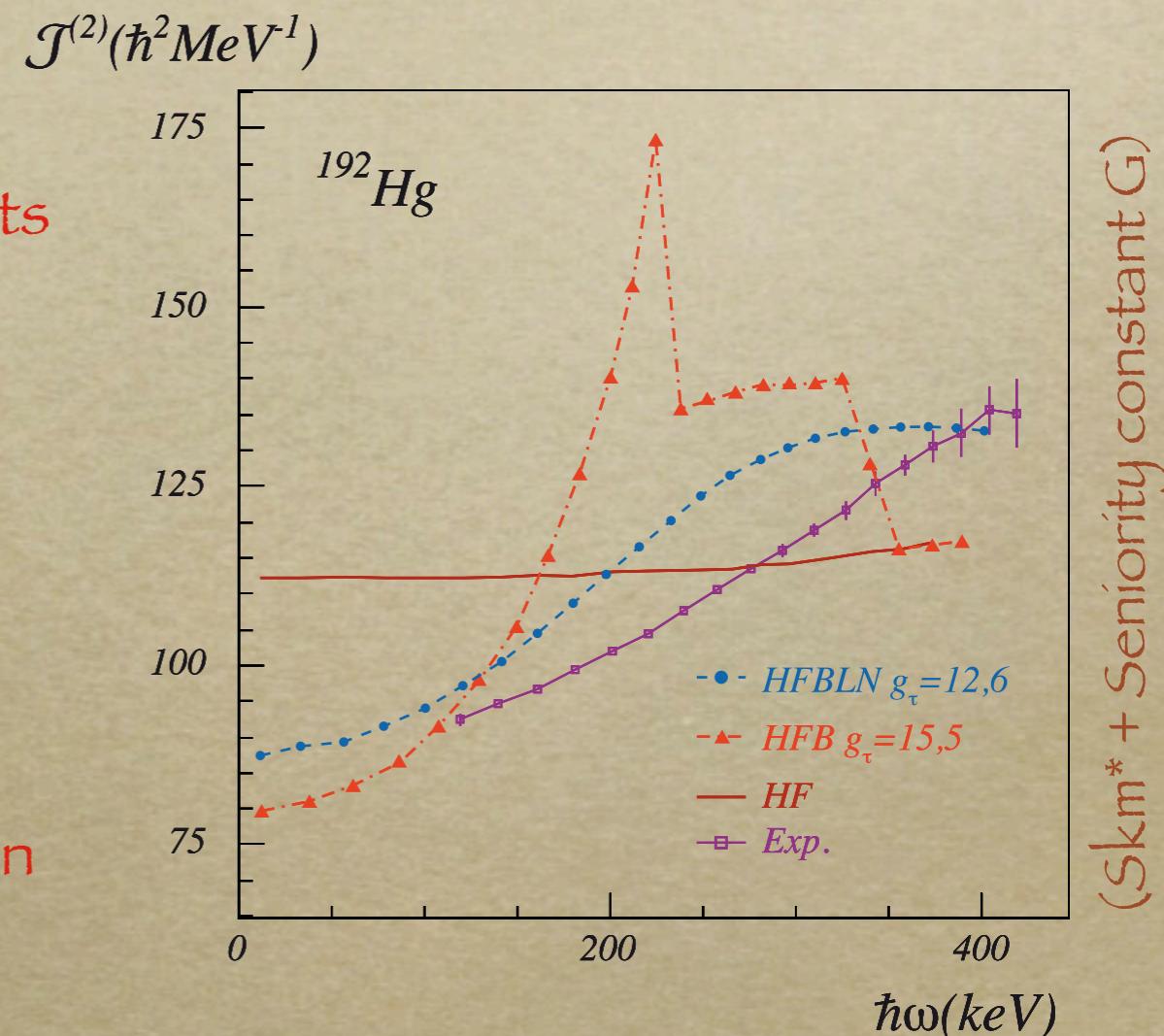


Cranked Hartree-Fock code

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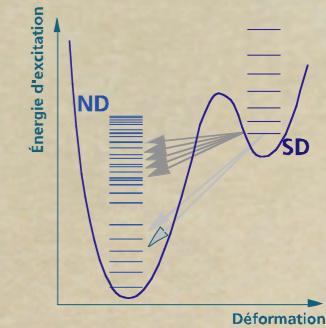
Signature of the pairing content and
underlying Single-Particles orbitals

- » HFB ~LN approximate particle # projection



Nuclear Pairing dependance on

Rotation



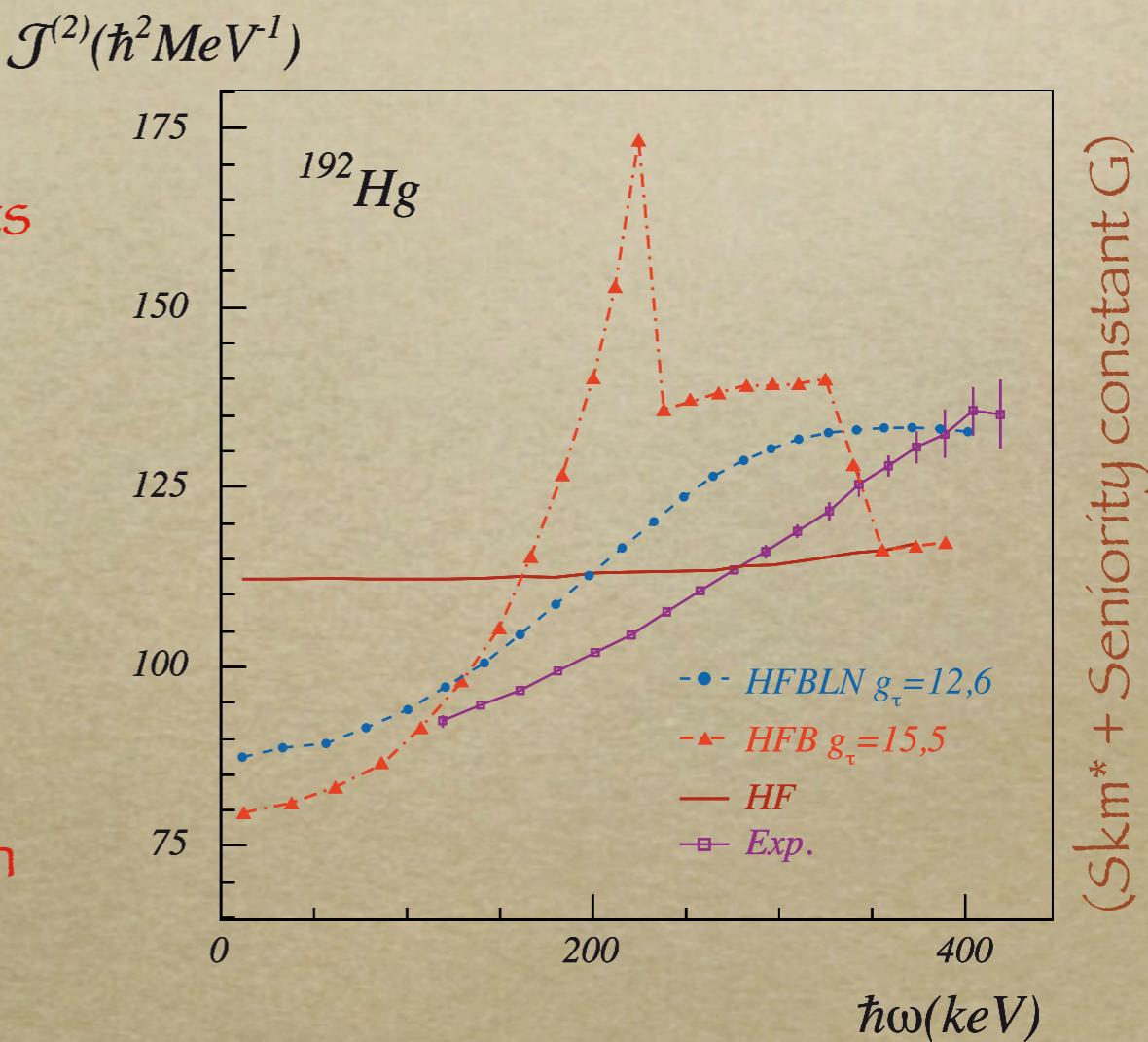
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Signature of the pairing content and
underlying Single-Particles orbitals

- » HFB ~LN approximate particle # projection
Behaviour in agreement with experiment
Need more investigations

On the good way ...



Improvements of the nuclear pairing description

SD-Bands in A=150 ...

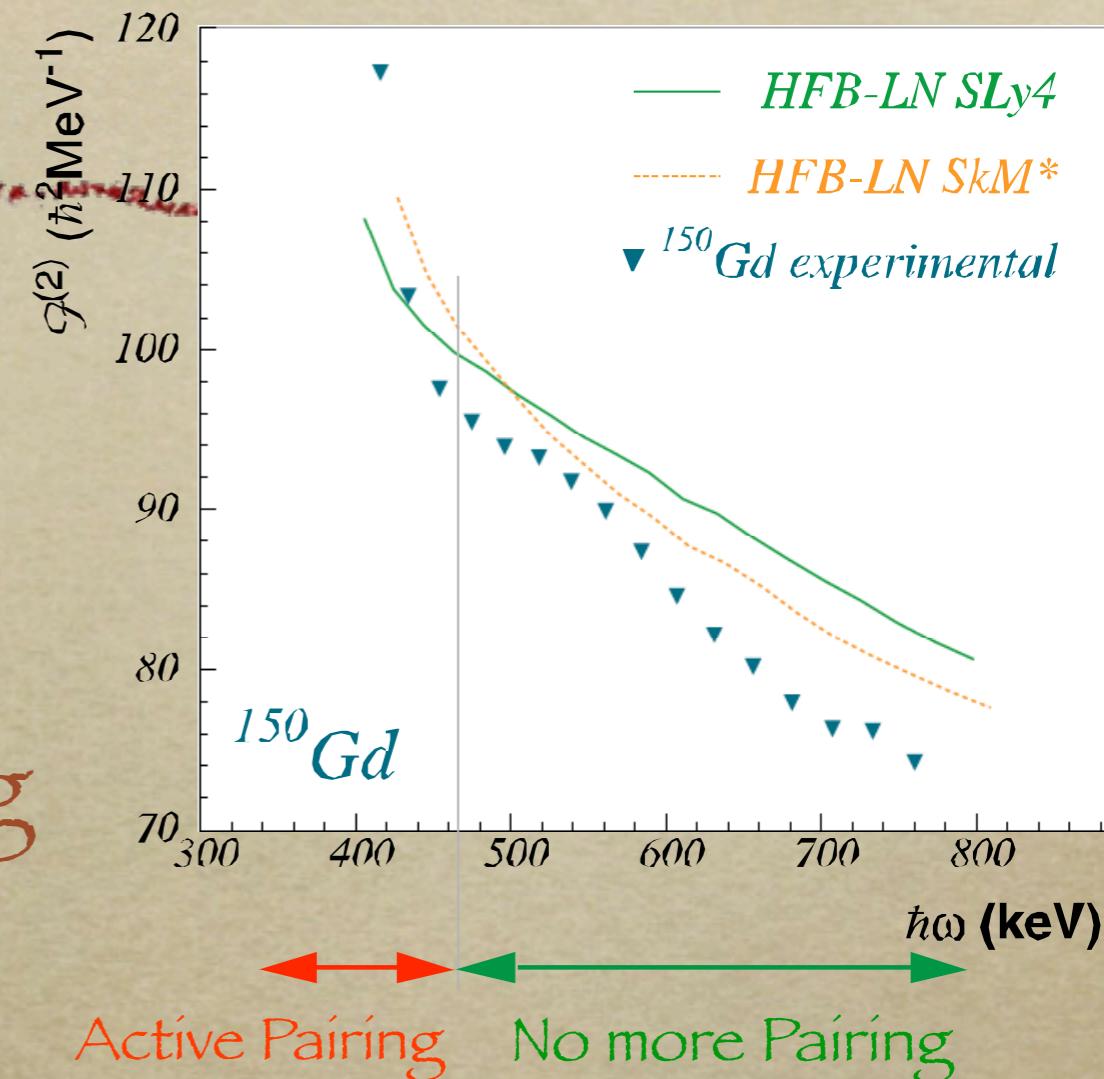
... Nuclear pairing still alive !

Implementation of a delta Pairing

$$V_p = \frac{V_0}{2} \cdot (1 - P^\sigma) \cdot \left(1 - \frac{\rho(r_1)}{\rho_c} \right) \cdot \delta(r_1 - r_2)$$

[J. Terasaki et al., NP A593(1995)1]

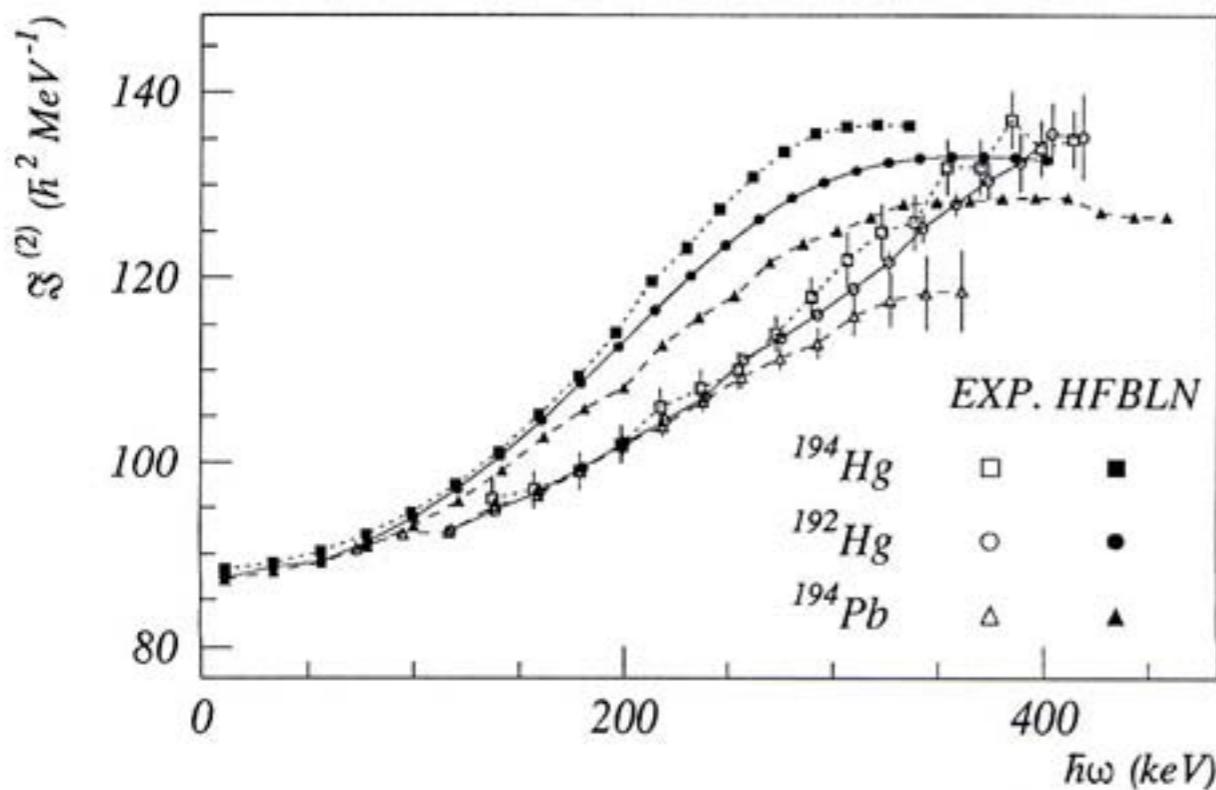
- determination of the right intensity
- Behaviour in agreement with experiment
- ID- Bands : Signature of the underlying Single-Particles orbitals (intruders)



	SLy4	SkM*
1 cut	1000	880
2 cuts	1250	nd

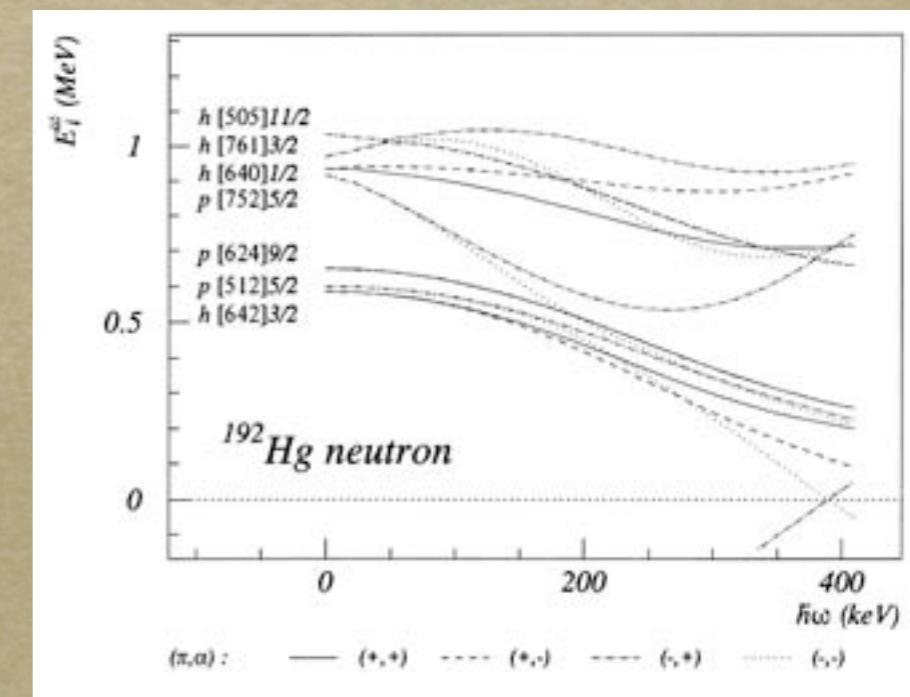
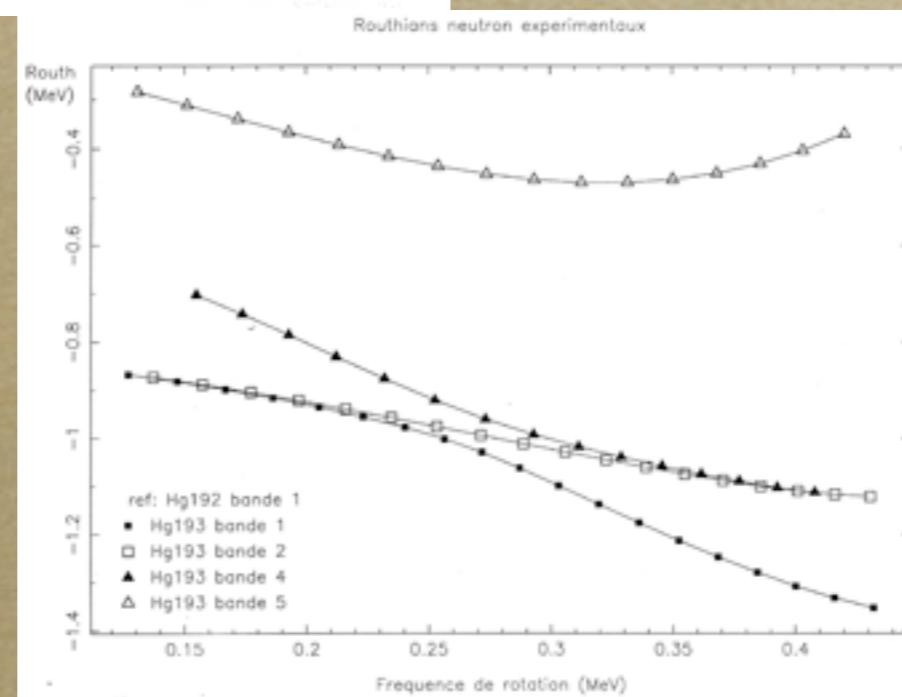
C. Rigollet PhD at CRN Strasbourg

Experiment-Theory : complementarity



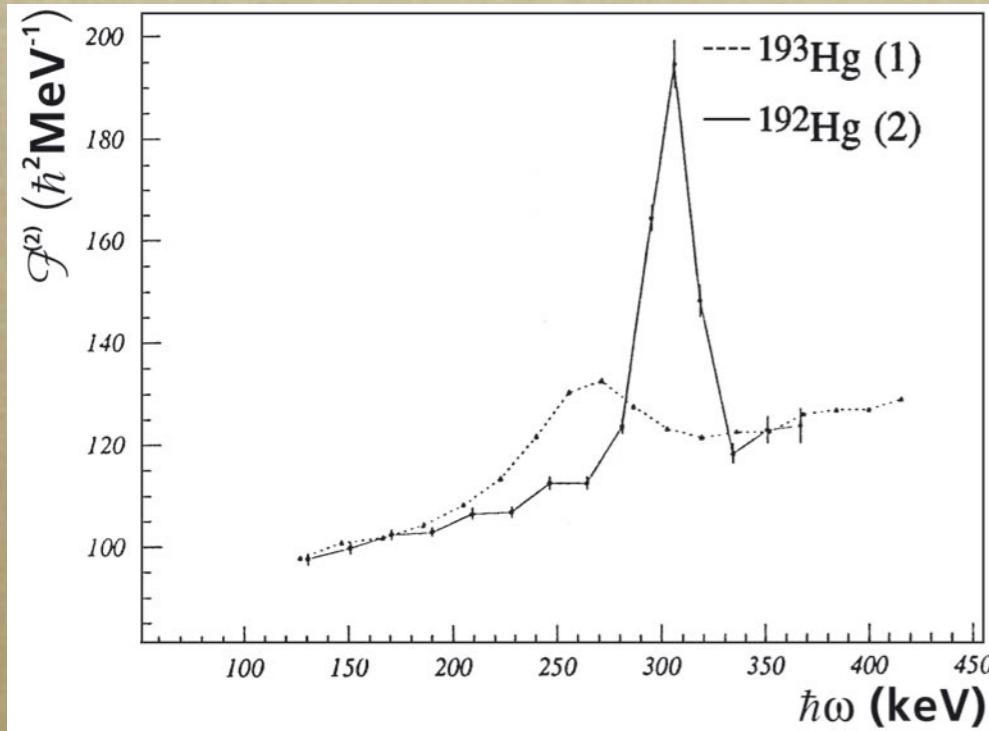
$A=190$ Sd Bands All Identical ?

- Behaviour in agreement with experiment
- Signature of the pairing content and underlying Single-Particles orbitals

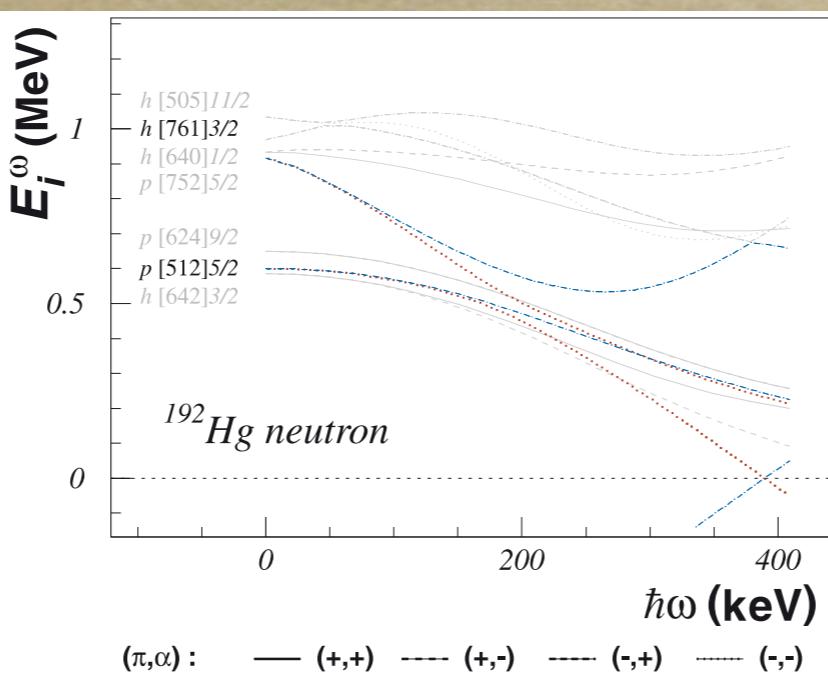
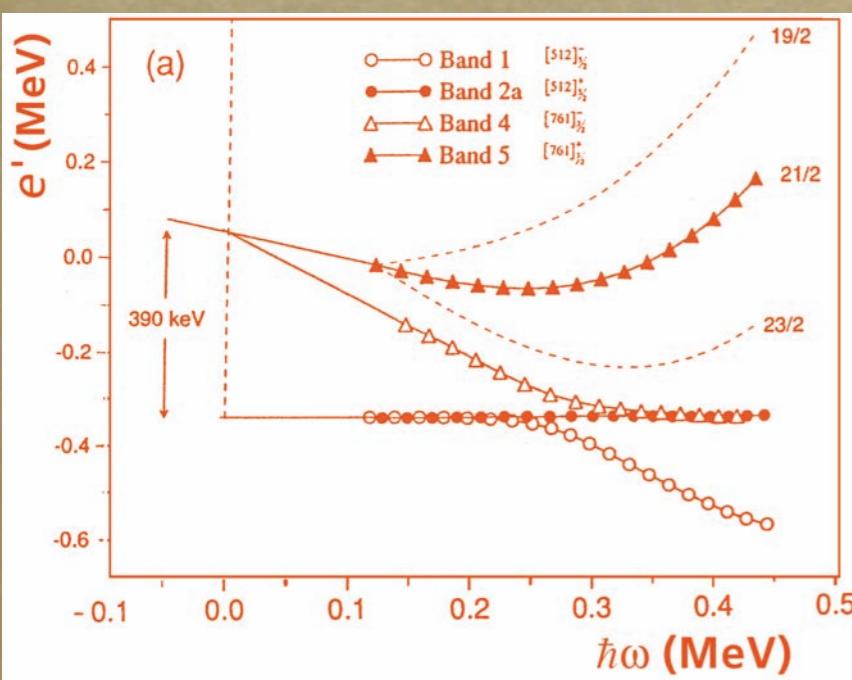
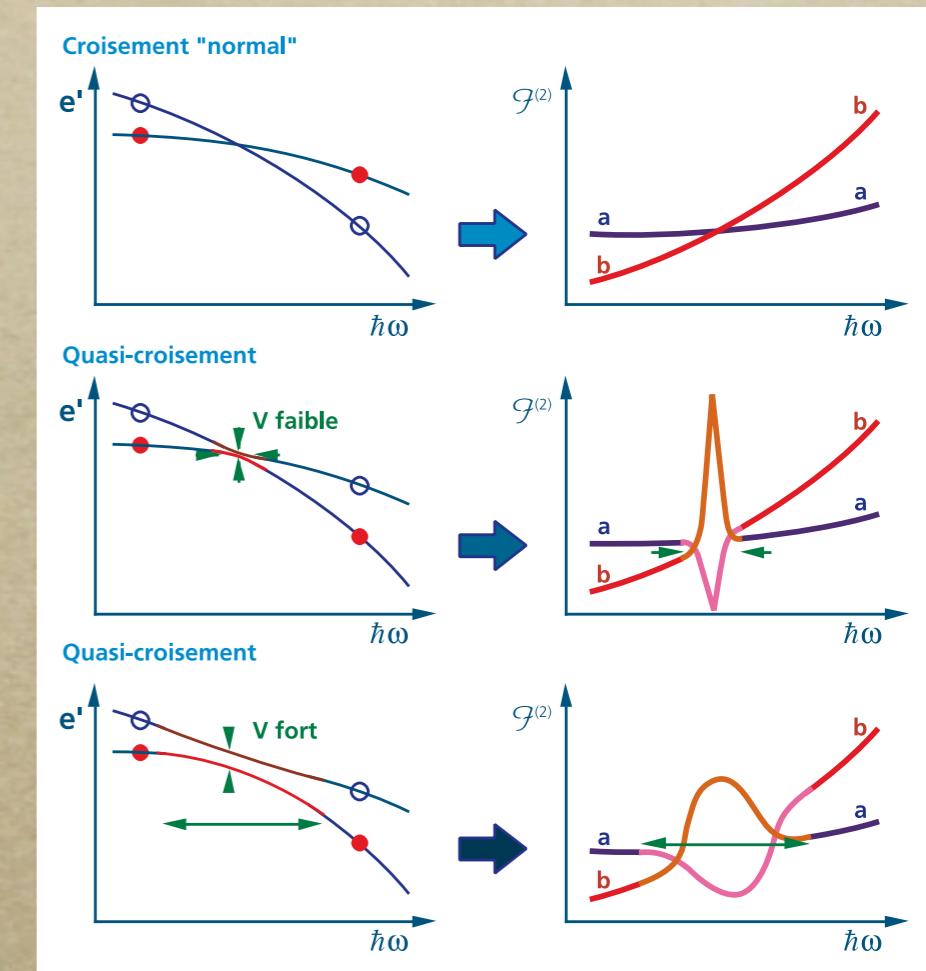


Complementarity

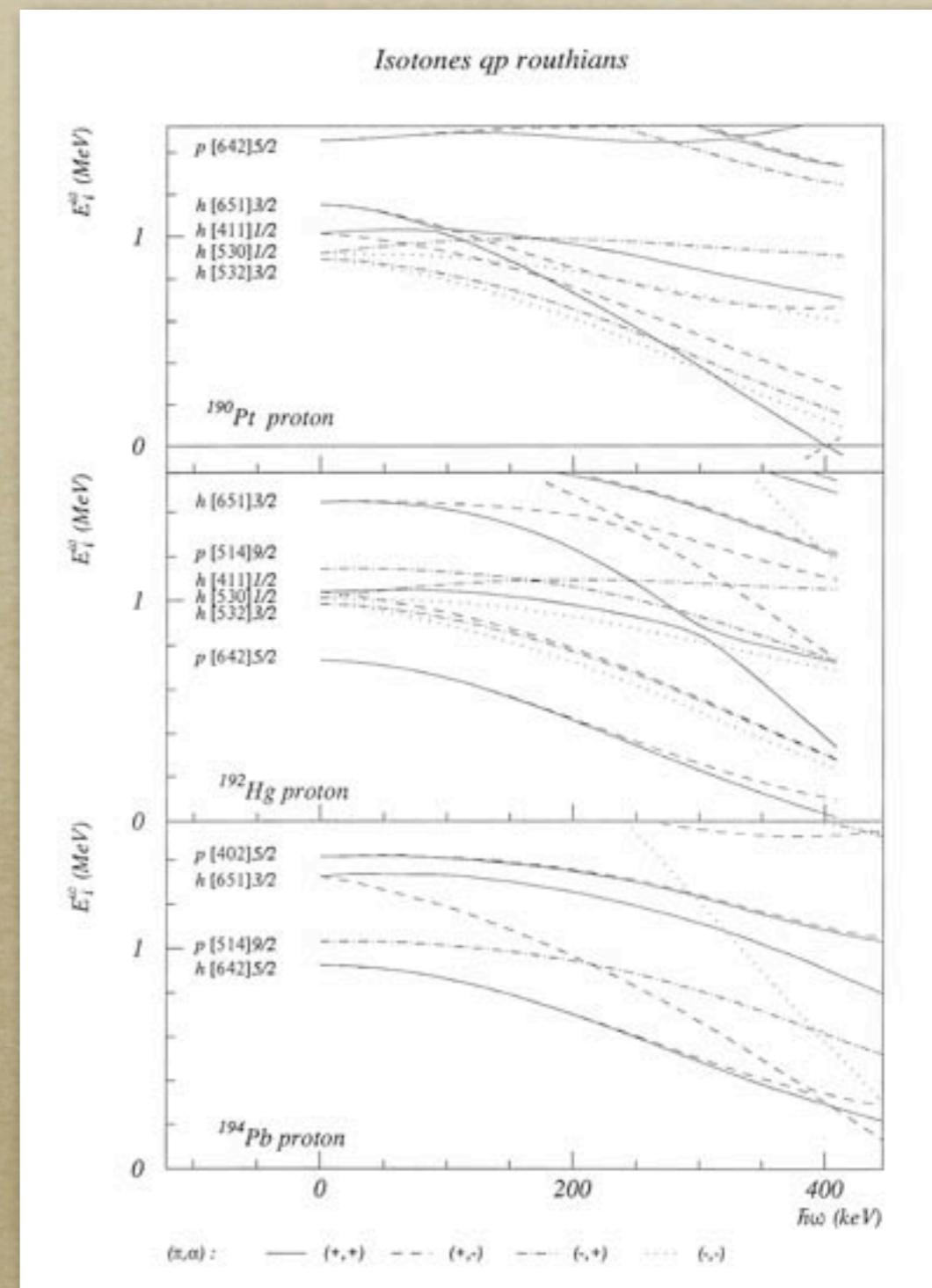
Orbital crossing



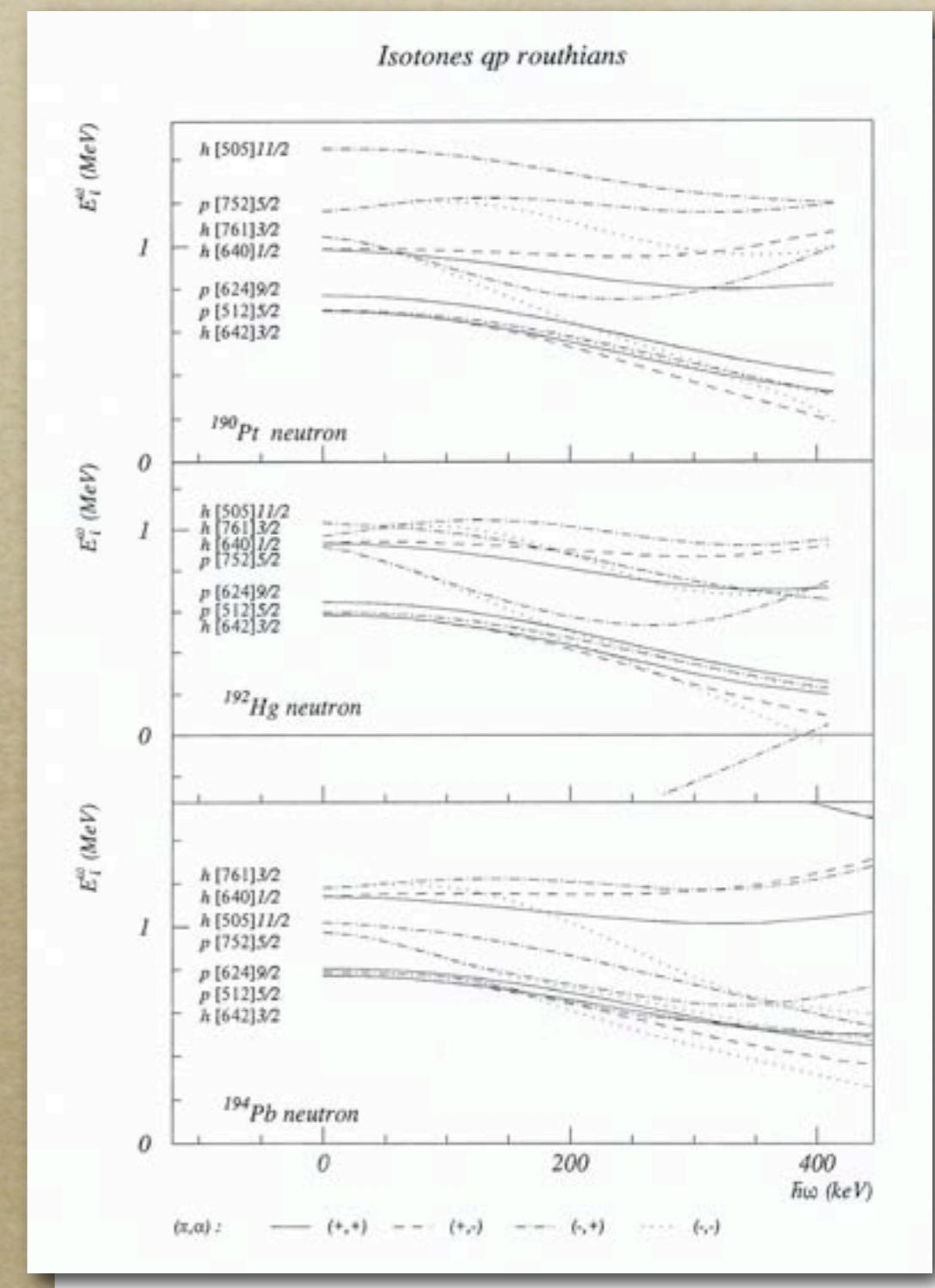
[512]5/2 et [761]3/2 crossing in ^{193}Hg (1) and ^{192}Hg (2)



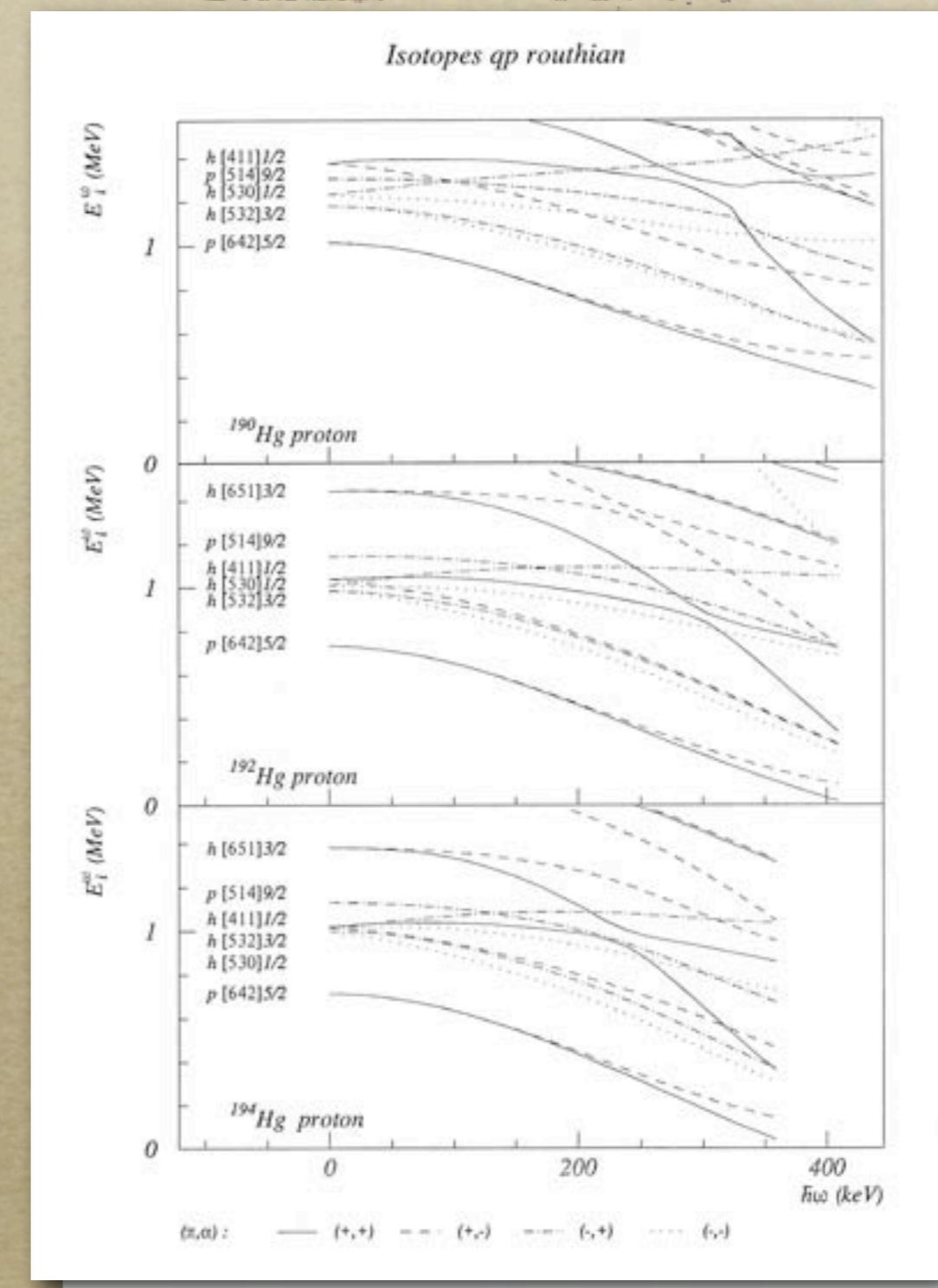
Experiment-Theory : complementarity



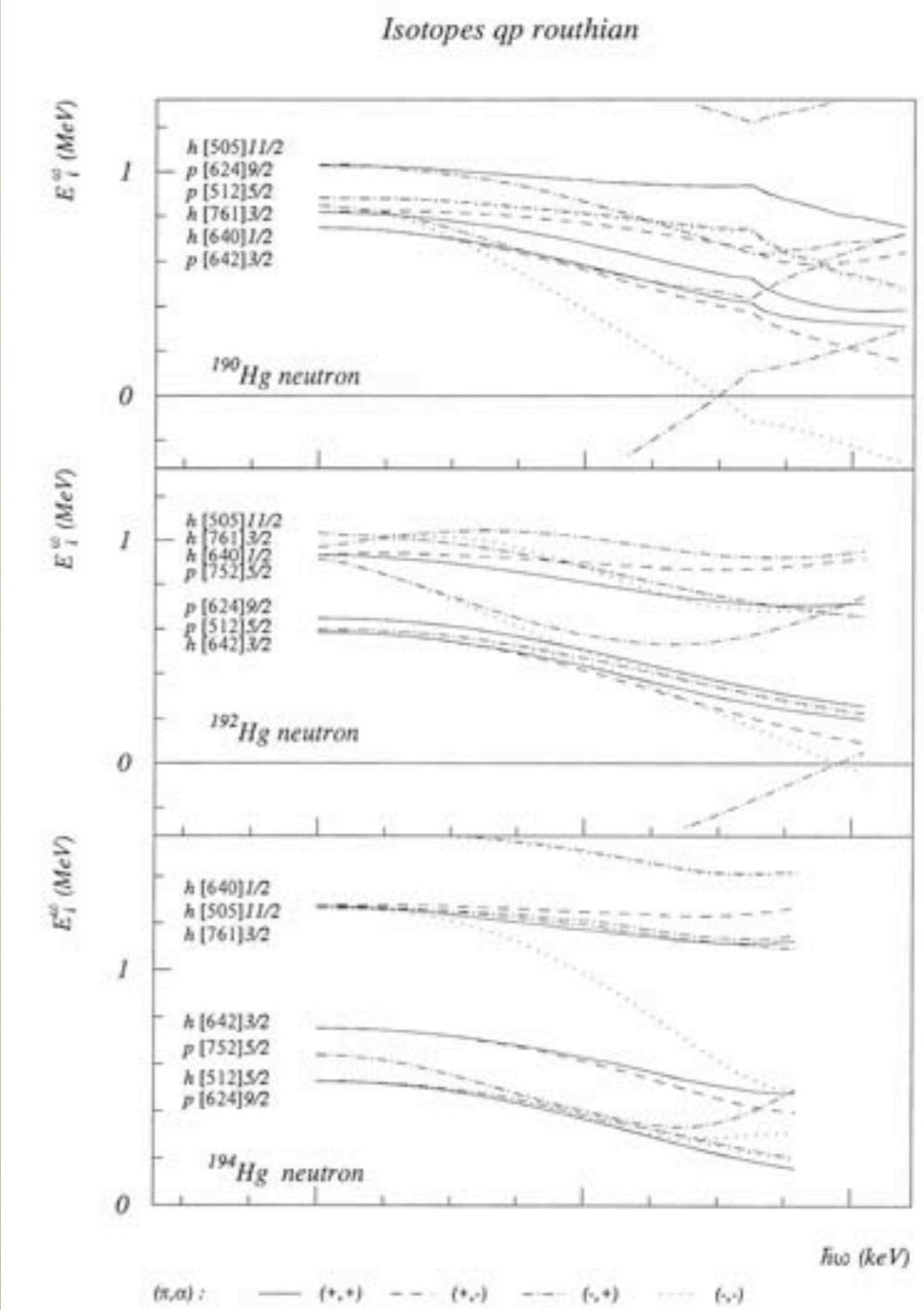
Experiment-Theory : complementarity



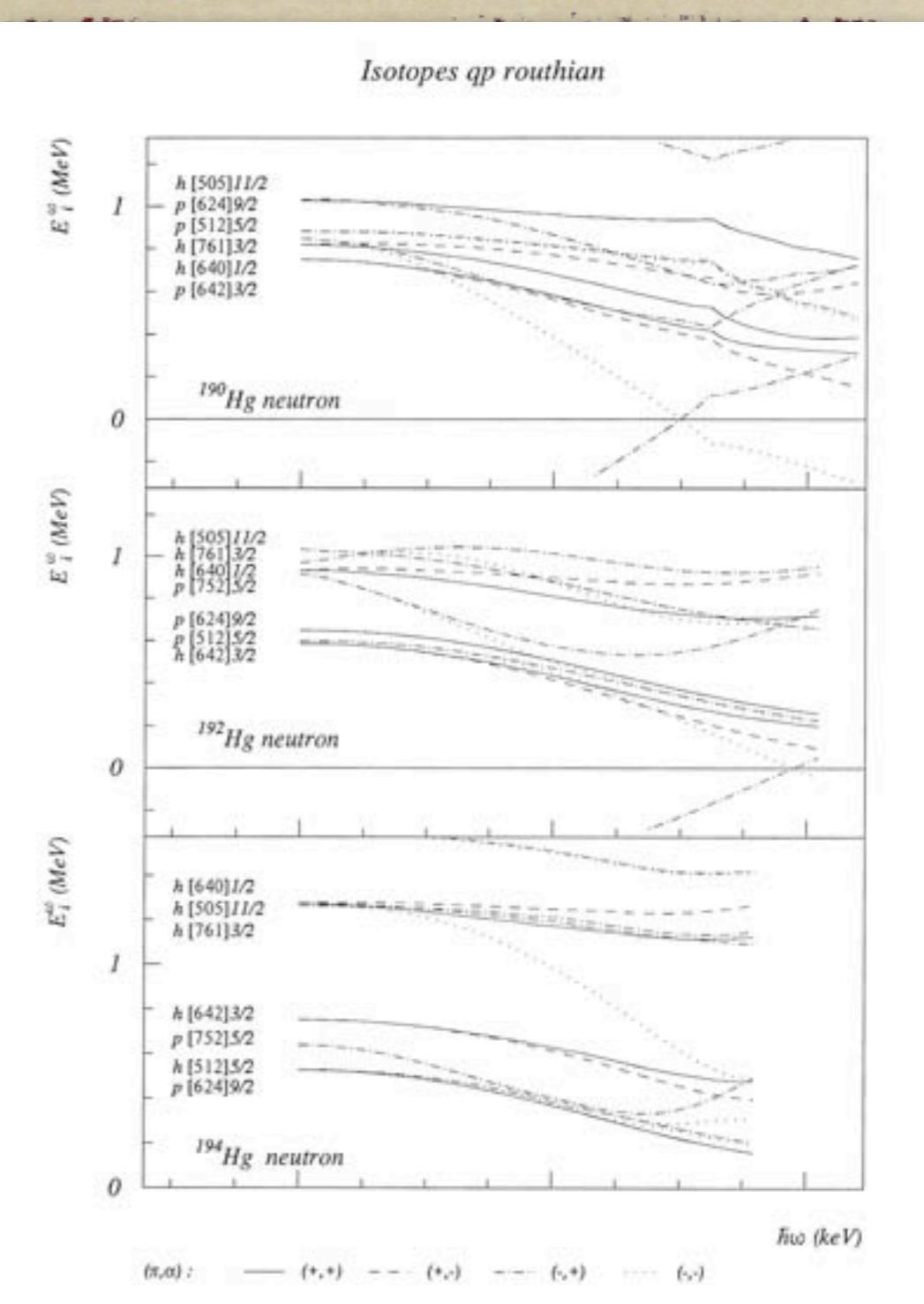
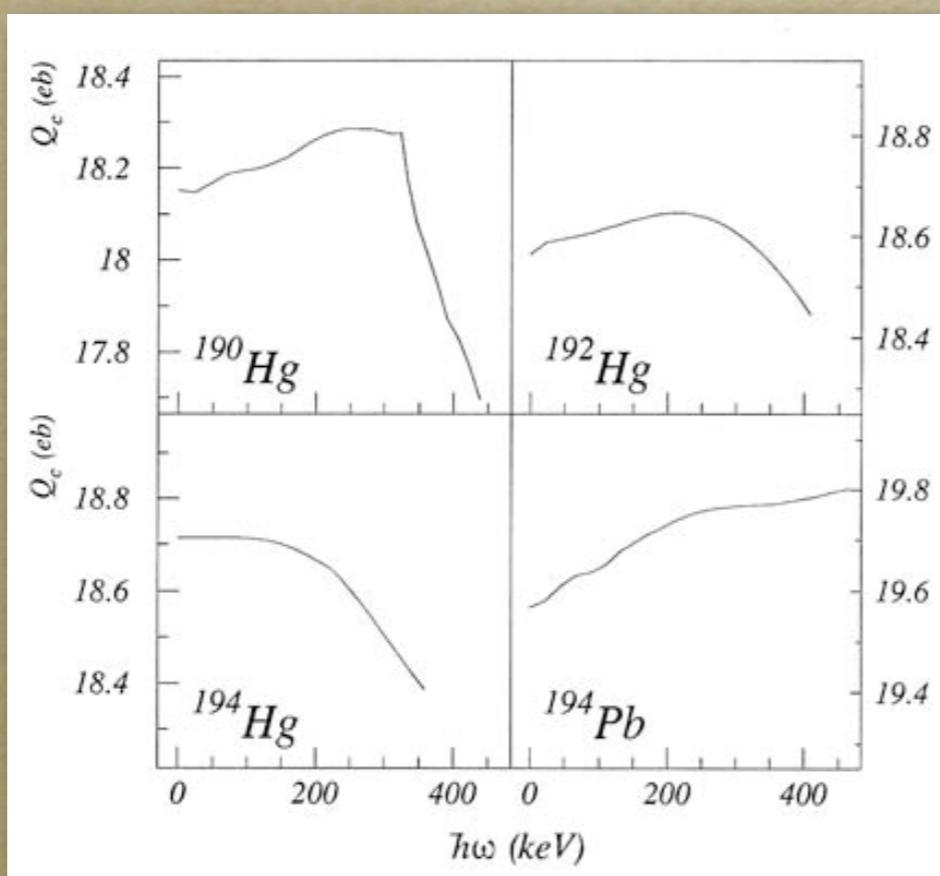
Experiment-Theory : complementarity



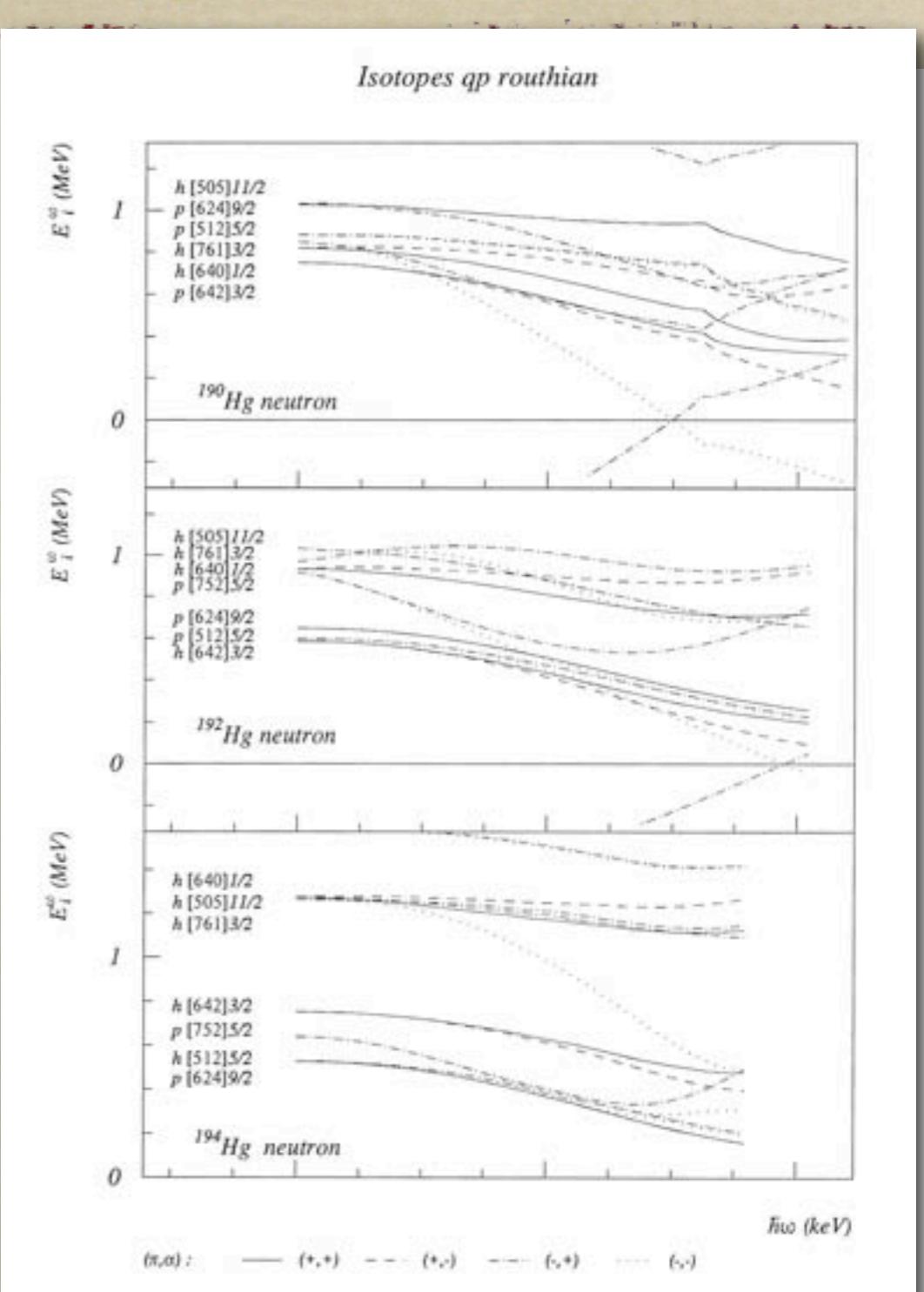
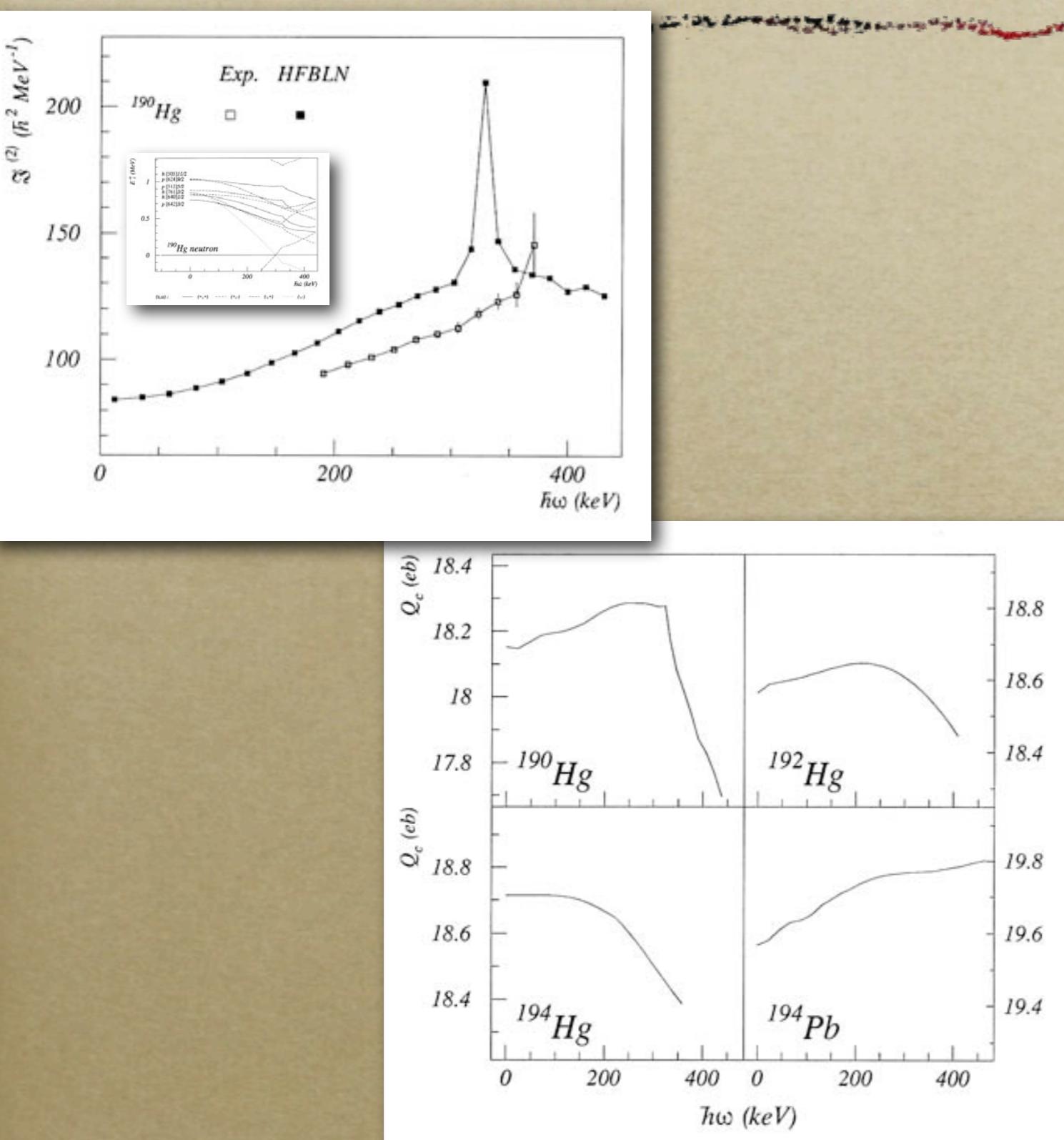
Experiment-Theory : complementarity



Experiment-Theory : complementarity



Experiment-Theory : complementarity



Outline

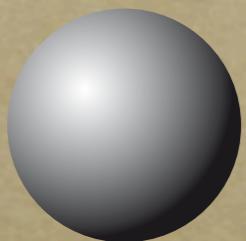
- ⦿ Preliminary considerations
- ⦿ Excitations of the nuclei; case of rotationnal bands
- ⦿ Effect of Nuclear deformation
- ⦿ Experimental toolboxes & selected cases

Simples nuclear shapes

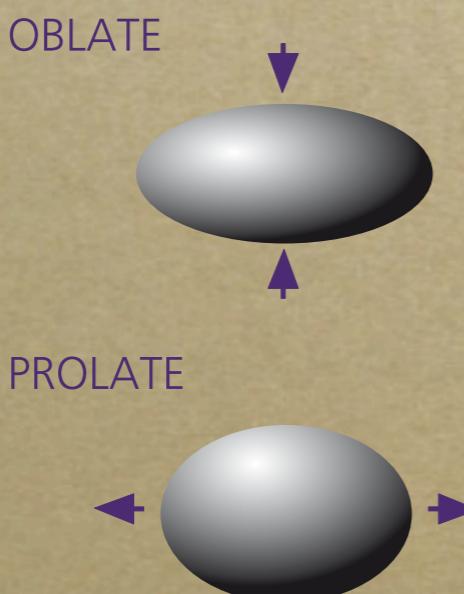
Paramétrisation of the

nuclear radius : $R(\theta, \phi) \propto Y_{\lambda\mu}(\theta, \phi)$

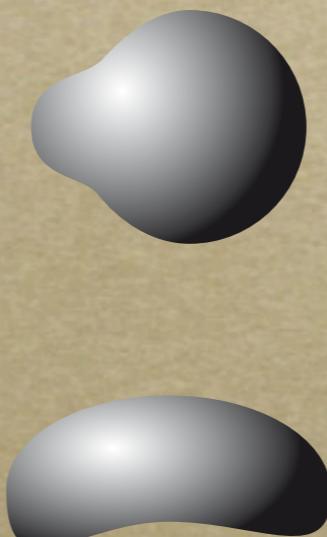
$\lambda = 0$
Sphère



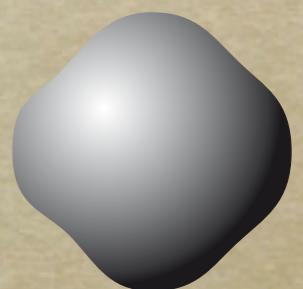
$\lambda = 2$
Quadrupôles



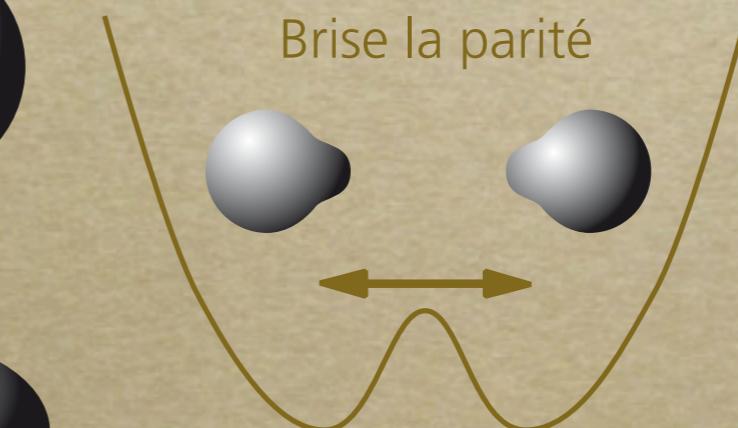
$\lambda = 3$
Octupôles



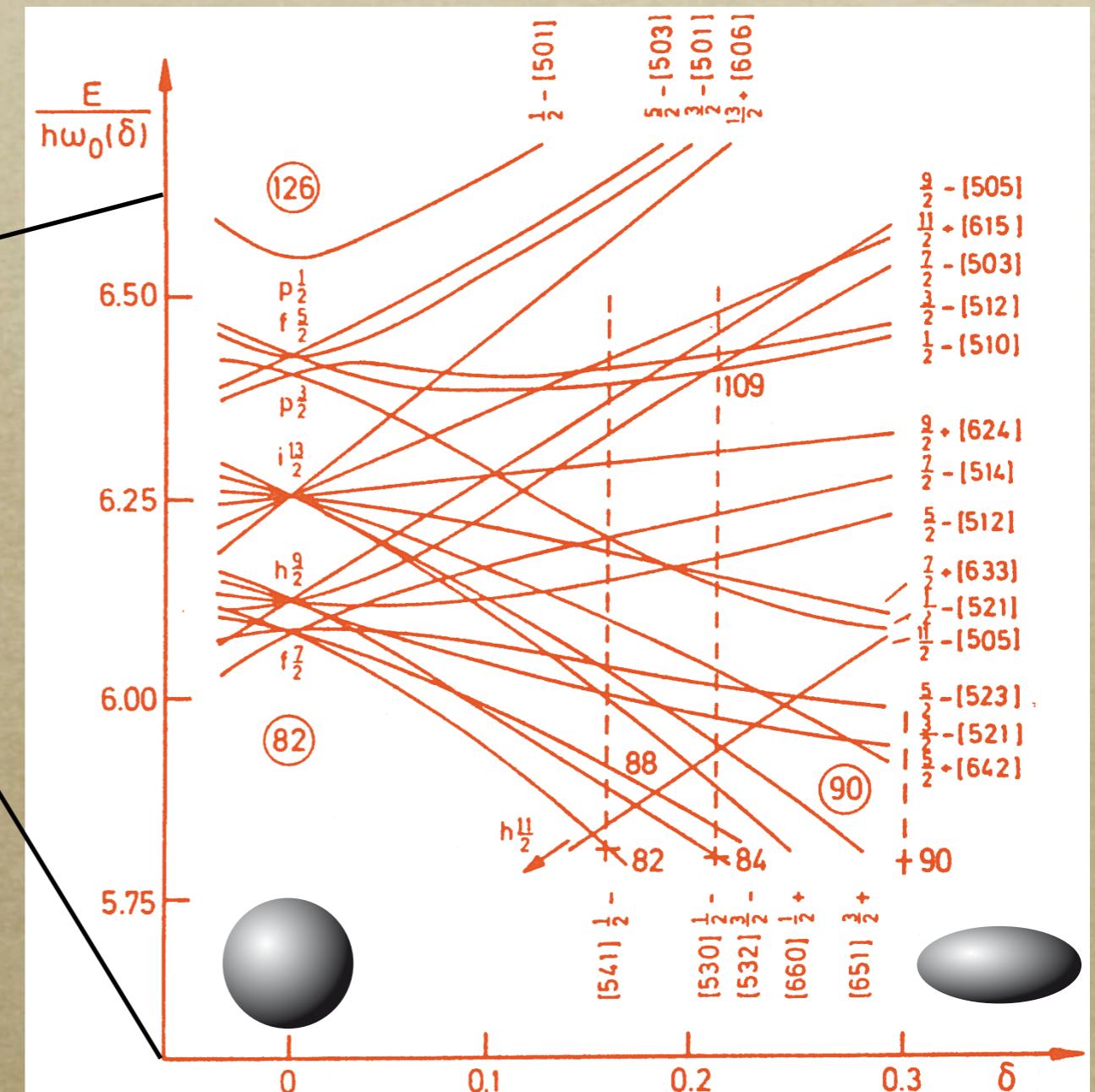
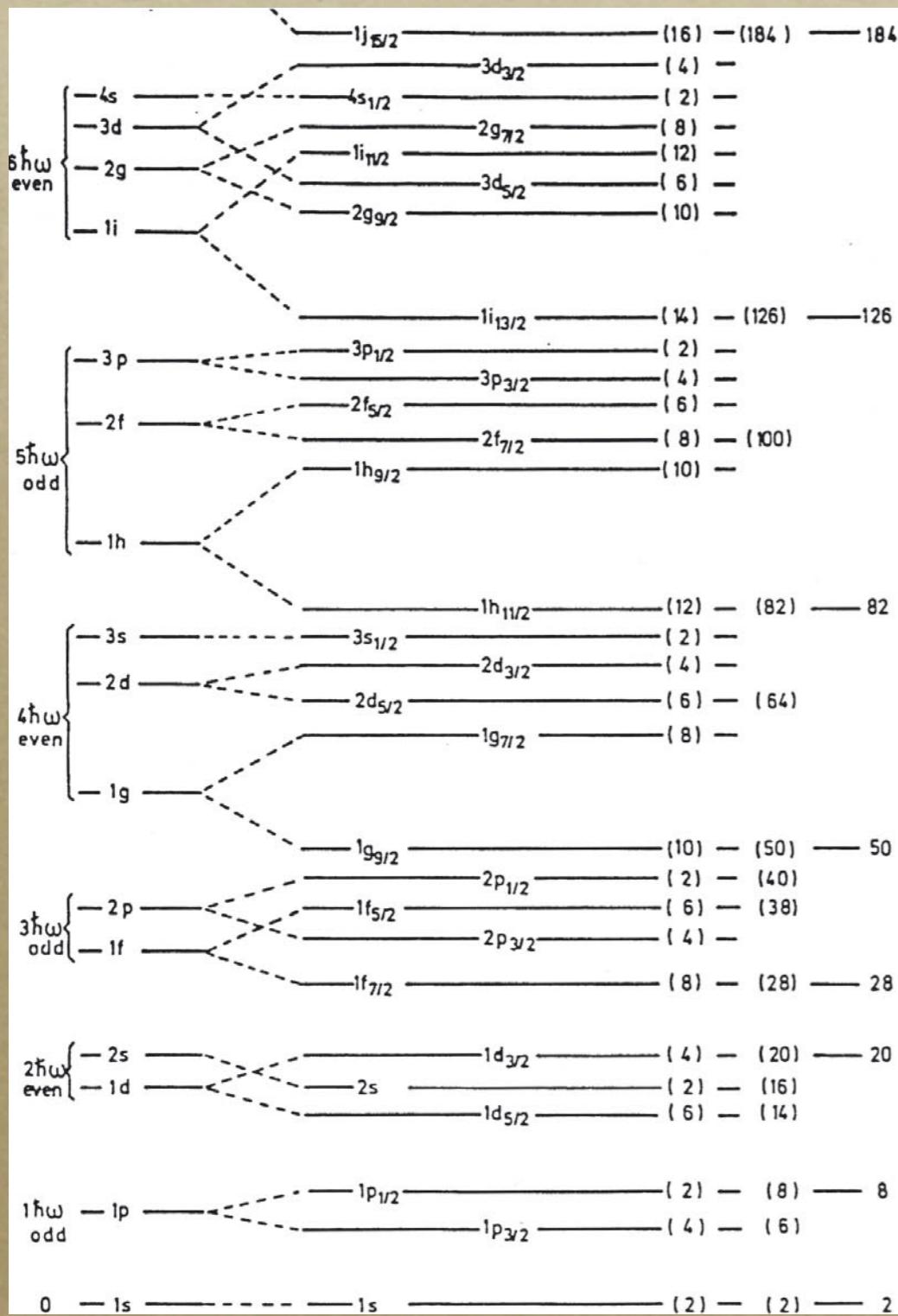
$\lambda = 4$
Hexadécapôles



Brise la parité



Effect of deformation on e_{sp}



Les VHE ...

on the road to SHE

What are the SHE gaps ?

Deformed gaps in VHE ...

Common Orbitals ? ...

Prompt Spectroscopy :

- Moment of inertia
- g-factor (odd nuclei)

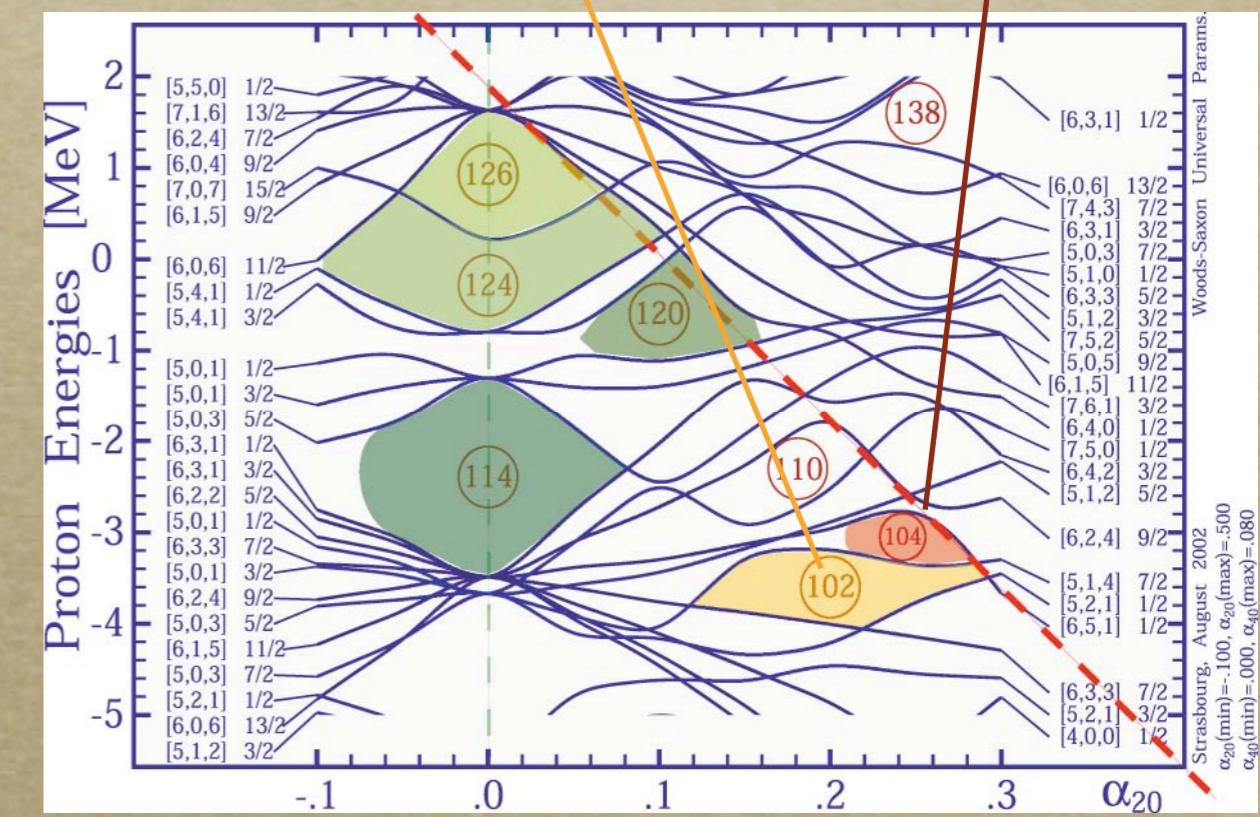
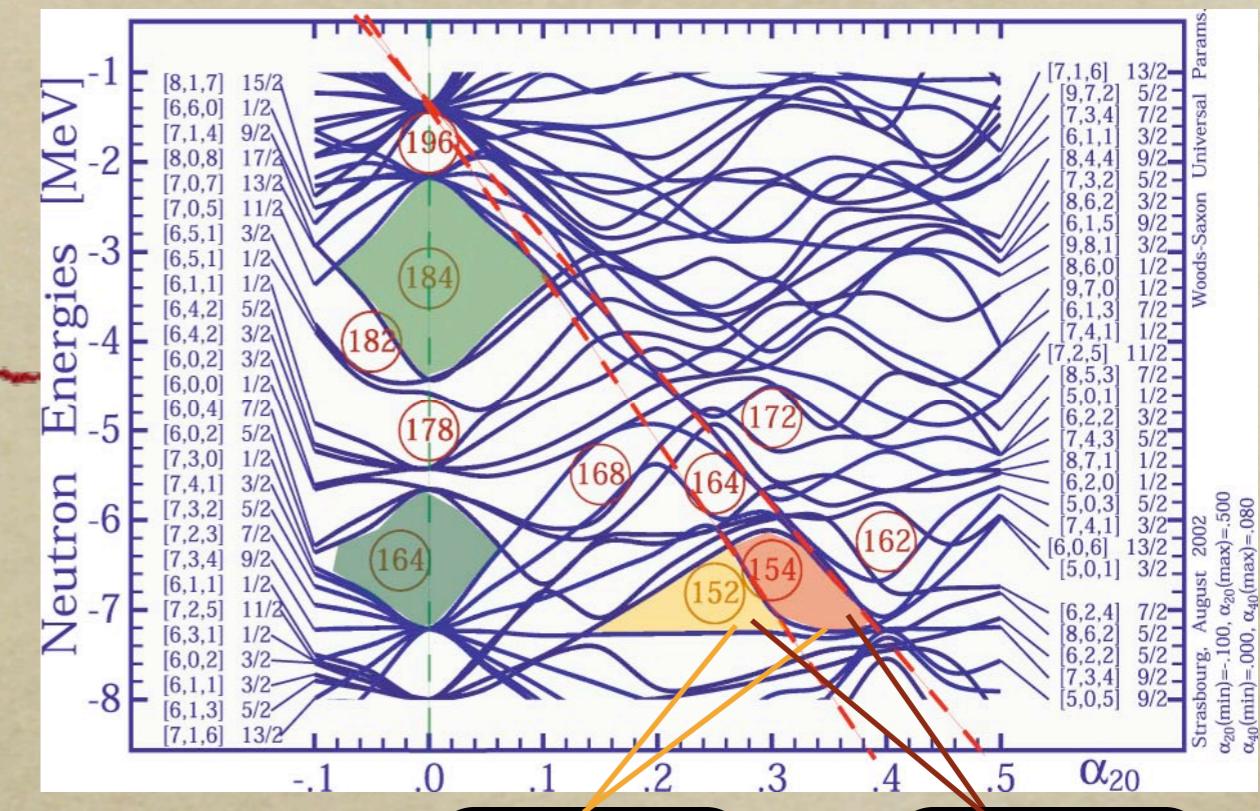
Decay spectroscopy

- isomers

Constraints on the different theories

Spectroscopy of $Z > 100$ fruitfull but...

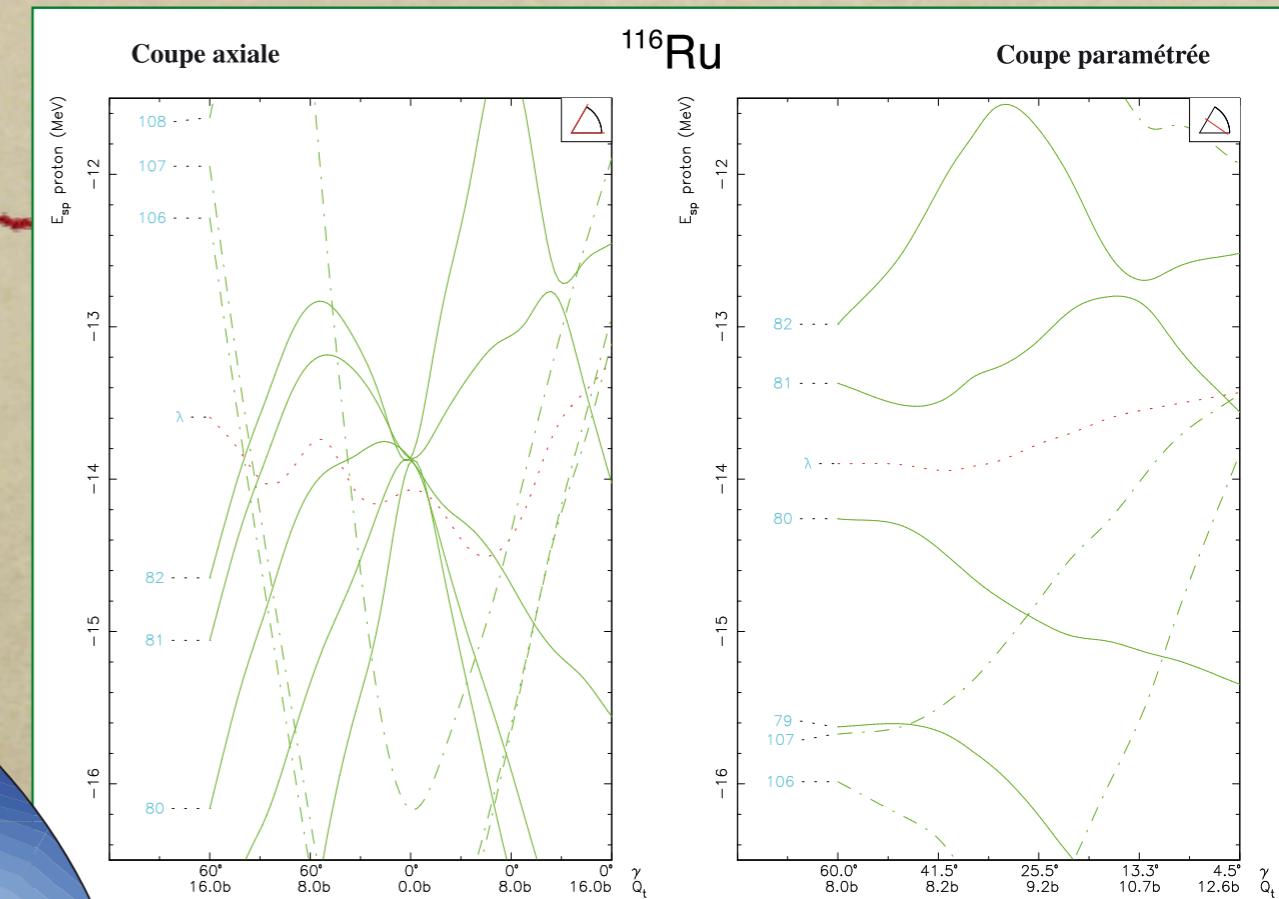
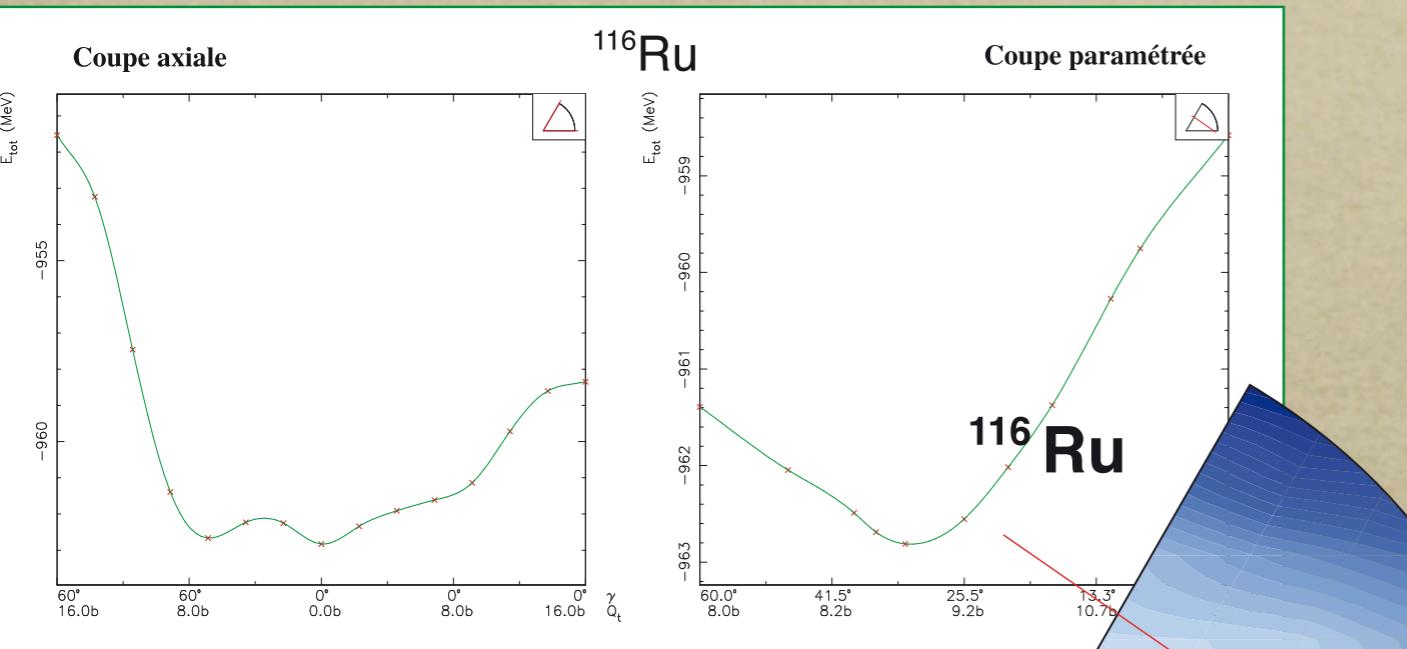
- Very low production cross-sections
- and low-energy transitions highly-converted ...



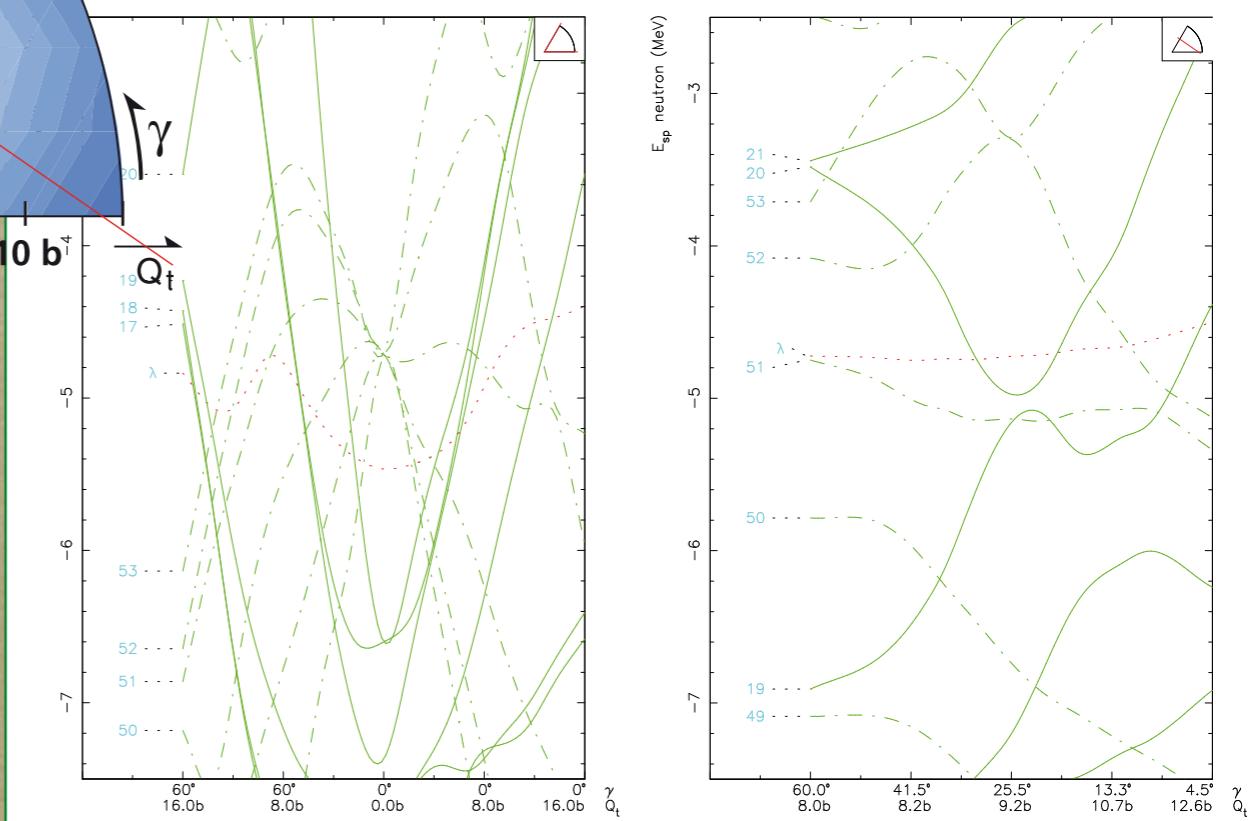
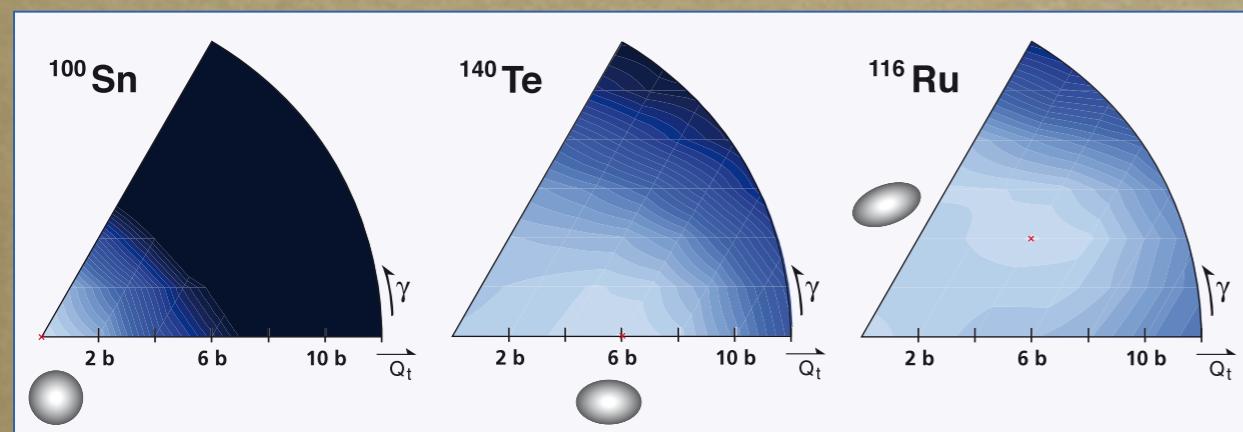
Need of new developpments

A ~ 100 Neutron-rich Nuclei

Spectroscopy



Triaxial nucleus
Diagonal cuts ...



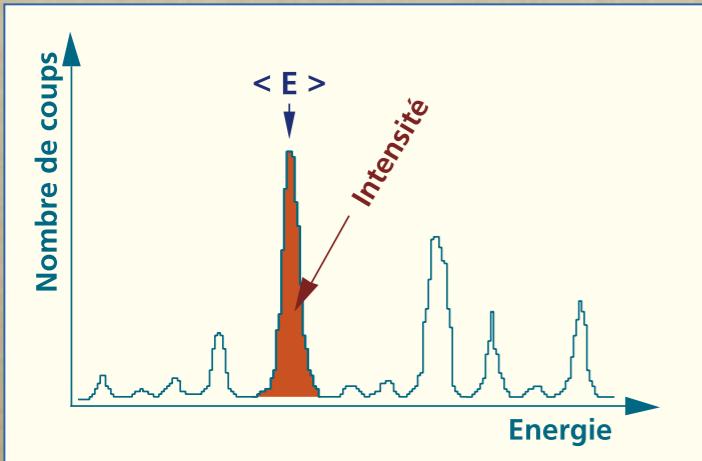
Outline

- ⦿ Preliminary considerations
- ⦿ Excitations of the nuclei; case of rotationnal bands
- ⦿ Effect of Nuclear deformation
- ⦿ Experimental toolboxes & selected cases



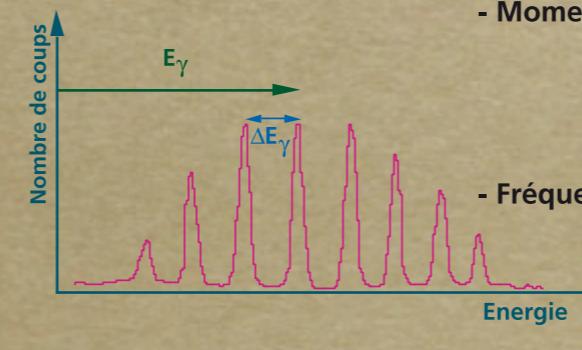
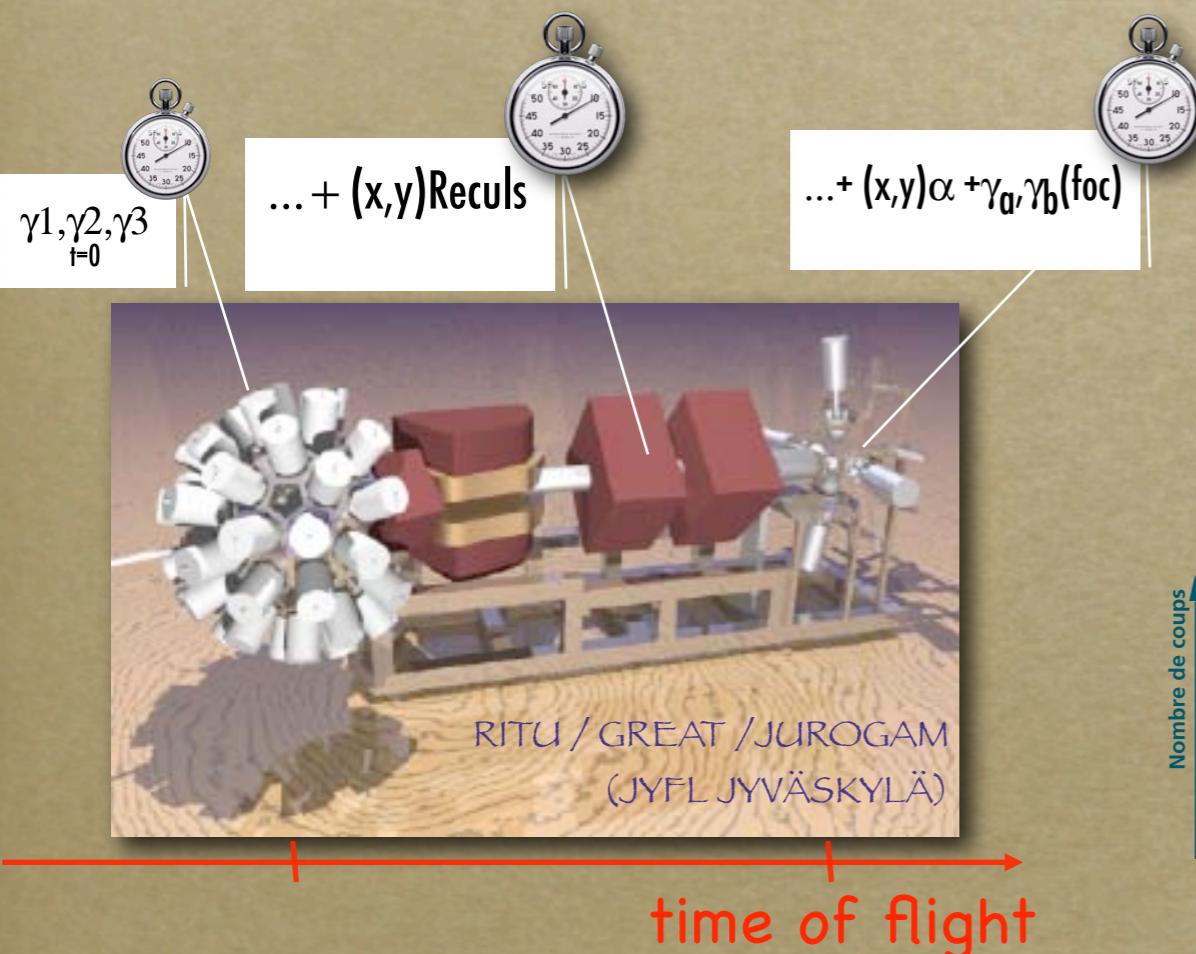
Experimental toolbox ...

... & selected cases



$$Q_o(eb) = \iiint \rho_p \cdot (3z^2 - r^2) \cdot dv$$

$$B(E2, I_i \rightarrow I_f) = -\frac{5}{16\pi} e^2 Q_o^2 \langle |I_i 2 K 0| |I_f K\rangle^2$$

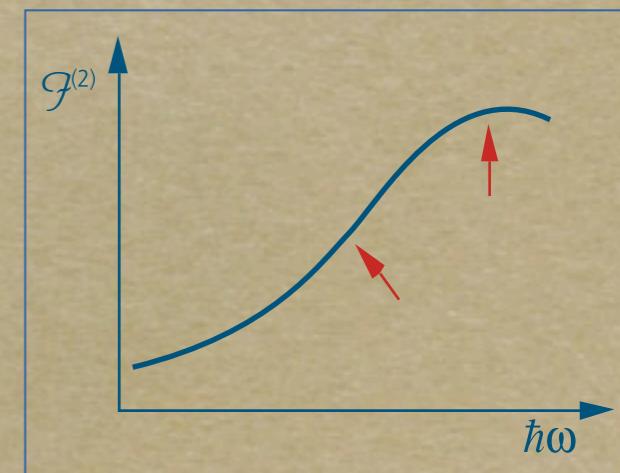
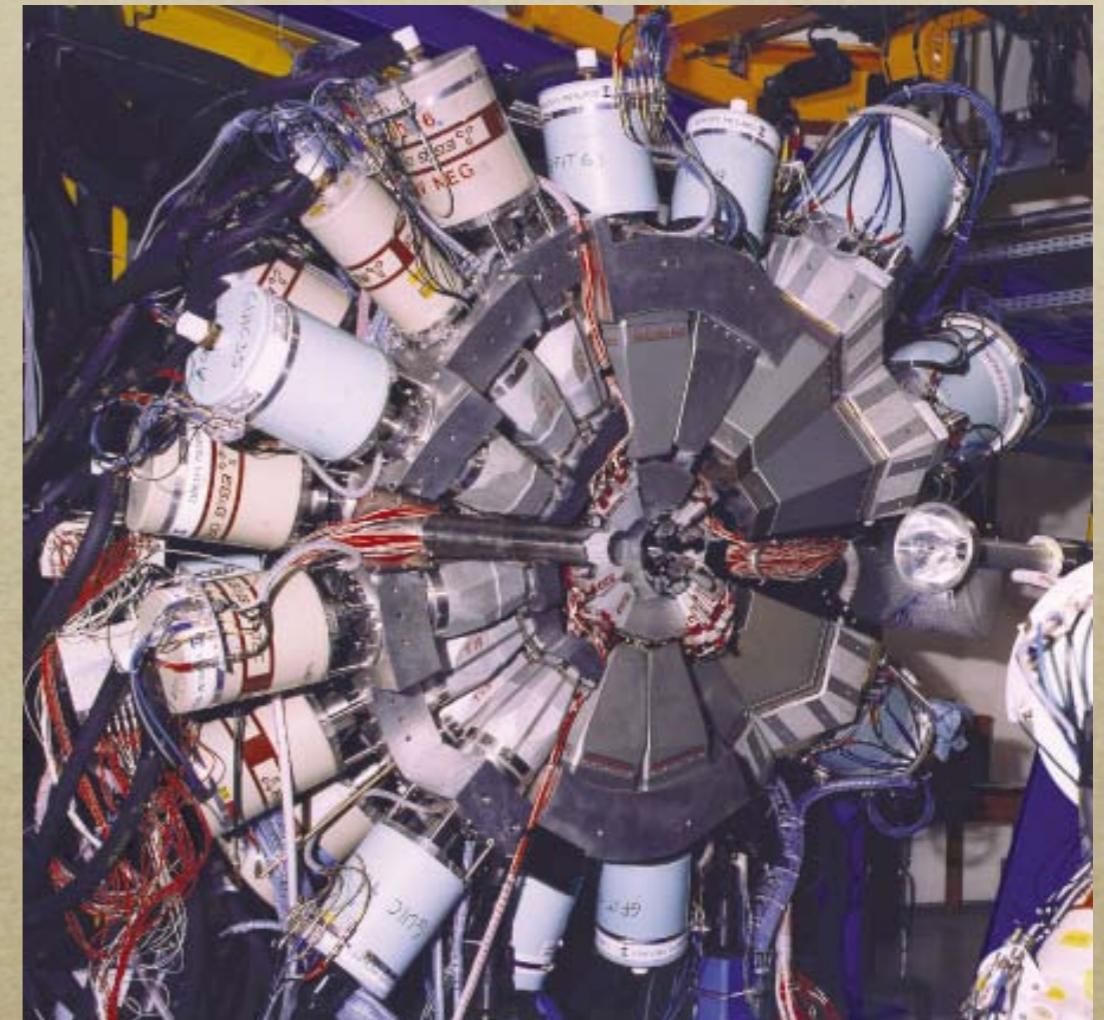


- Moment d'inertie dynamique :

$$\mathcal{J}^{(2)} = \frac{\Delta E_\gamma}{4}$$

- Fréquence de rotation :

$$\hbar\omega = \frac{E_\gamma}{2}$$

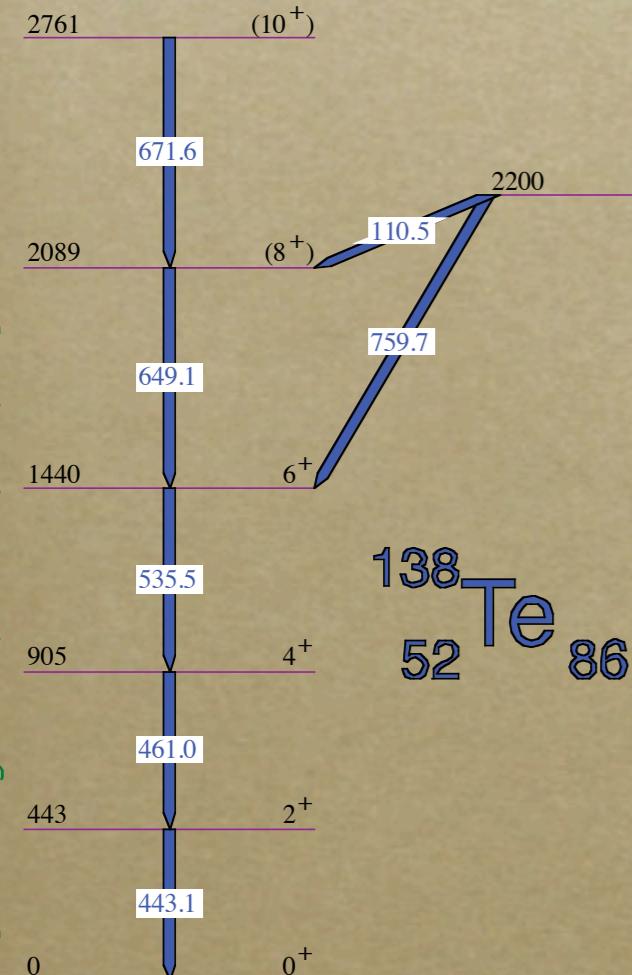


A ~ 100 Neutron-rich

Nuclei

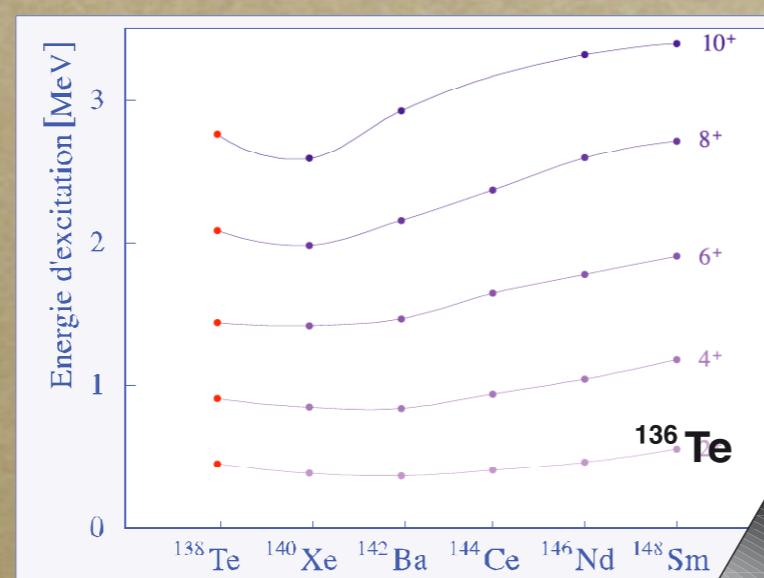
Fission-Fragments Spectroscopy

^{138}Te correspond to a vibrational structure



	Vibration	Rotation	^{138}Te
$E(4^+)/E(2^+)$	2	3,3	2,06
$E(6^+)/E(2^+)$	3	7,0	3,26
$E(8^+)/E(2^+)$	4	12,0	4,71

^{138}Te is calculated prolate ...



Taux de production (% fission)

- >1.0
- 0.1-1.0
- 0.01-0.1
- 0.001-0.01
- 0.0001-0.001
- <0.0001
- Stable

Fission de ^{252}Cf

Z

N

^{82}Pb

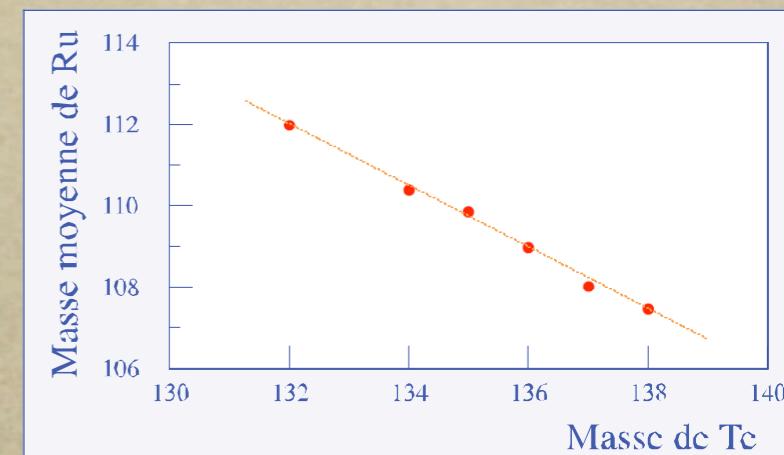
80 Hg
78 Pt
76 Os
74 W
72 Hf
70 Yb
68 Er
66 Dy
64 Gd
62 Sm
58 Ce
56 Ba
54 Xe
50 Sn
48 Cd
46 Pd
42 Mo
40 Zr
38 Sr
36 Kr
34 Se
32 Ge
30 Zn
28 Ni
26 Fe
24 Cr
22 Ti
20 Ca

112 114
108
106
102
100
98
96
94
92
88
86
84
82
78
76
74
72
70
68
66
64
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46
44
42
40
38
36
34
32
30
28

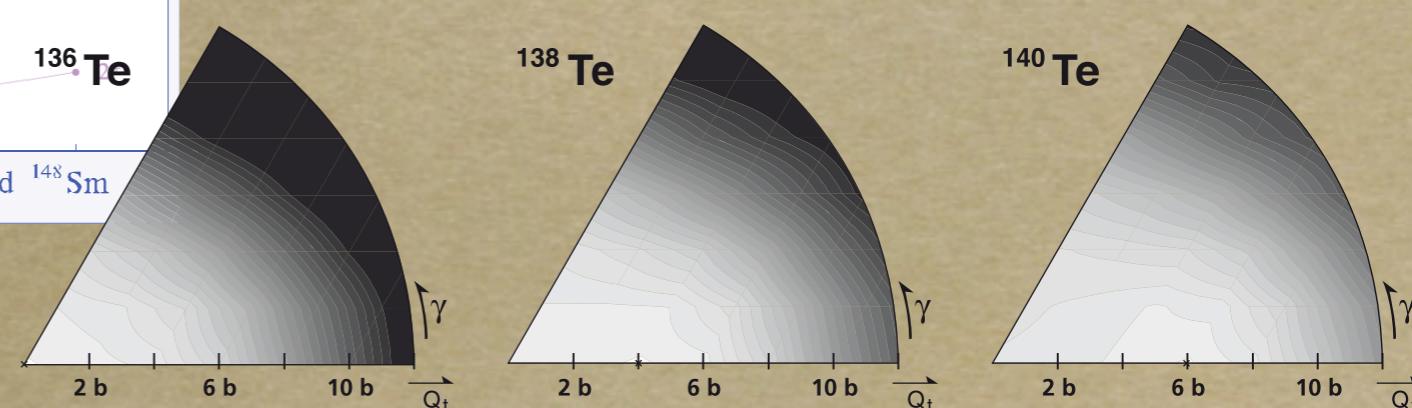
N = 89,90 : déformation octupolaire stable

Structure nucléaire près des couches fermées, ^{132}Sn

Bandes Identiques dans Ru et Mo



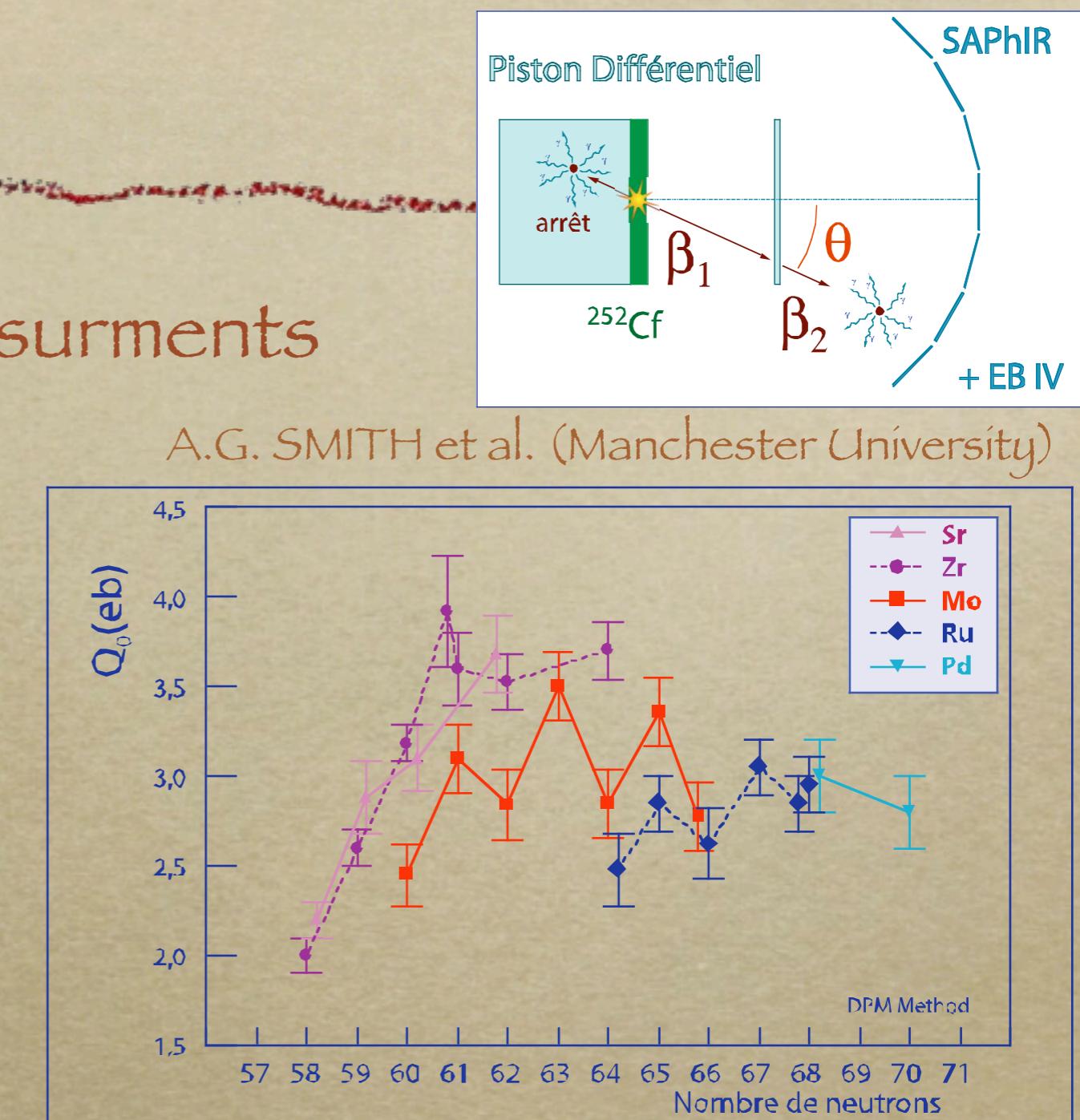
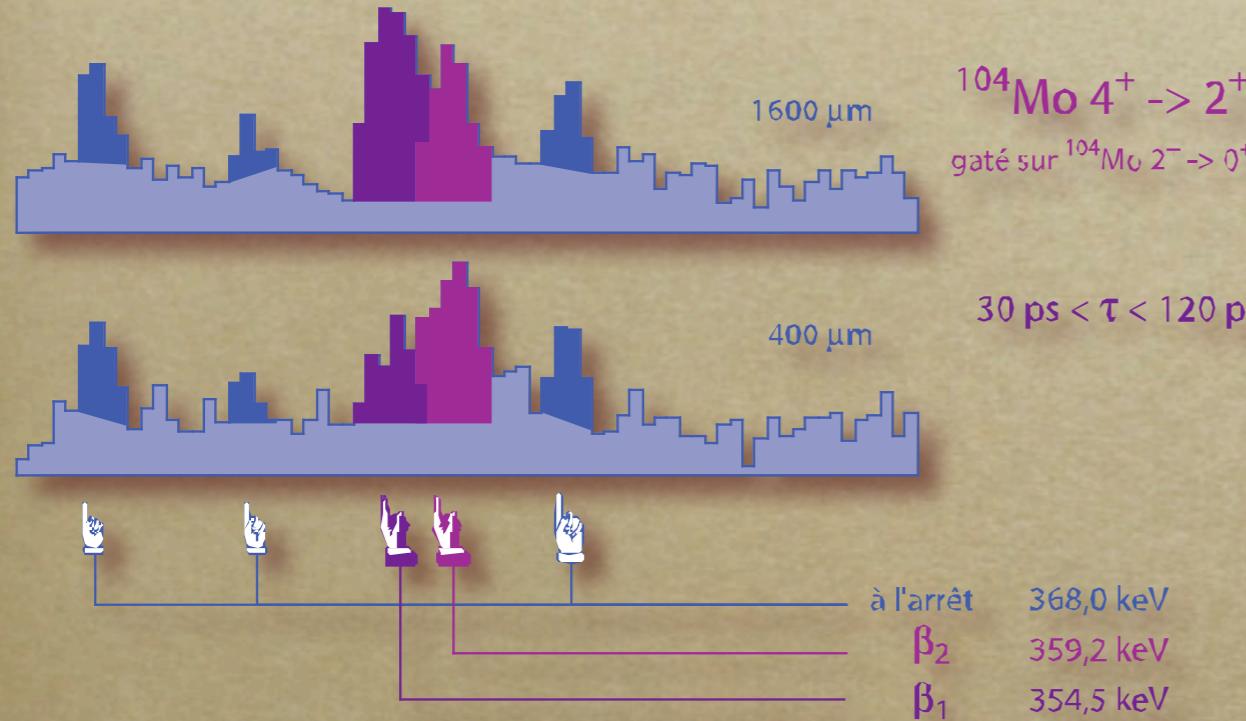
The spherical to prolate shape transition is higher in mass for Te's



A ~ 100 Neutron-rich Nuclei

Spectroscopy

Quadrupole Moment Measurements

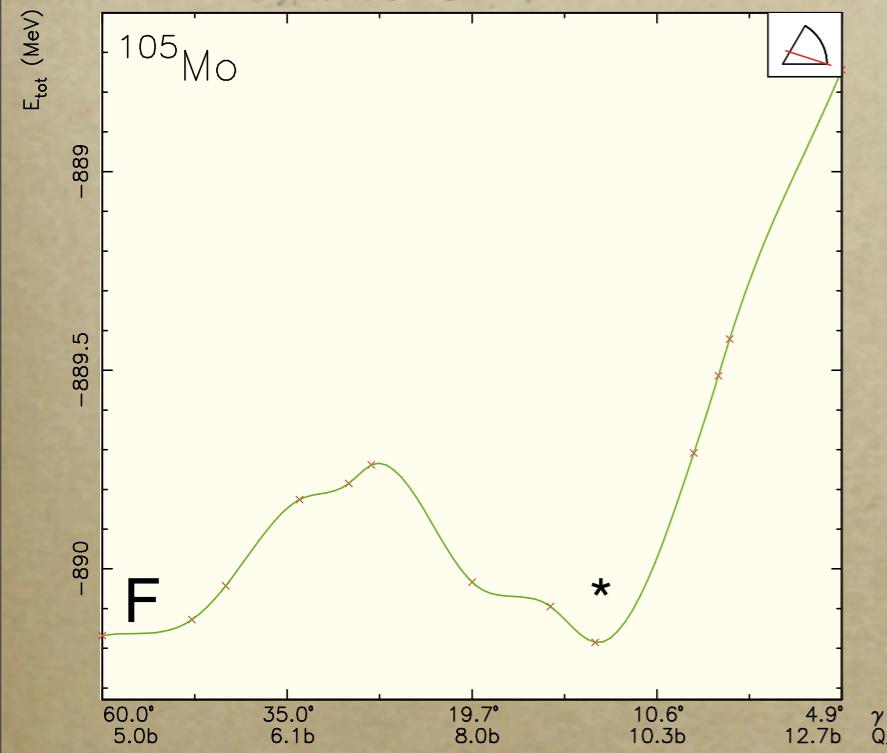


The Mo isotopes oscillate between two behaviors (Sr, Zr) and (Ru, Pd) ... Shape transition Région

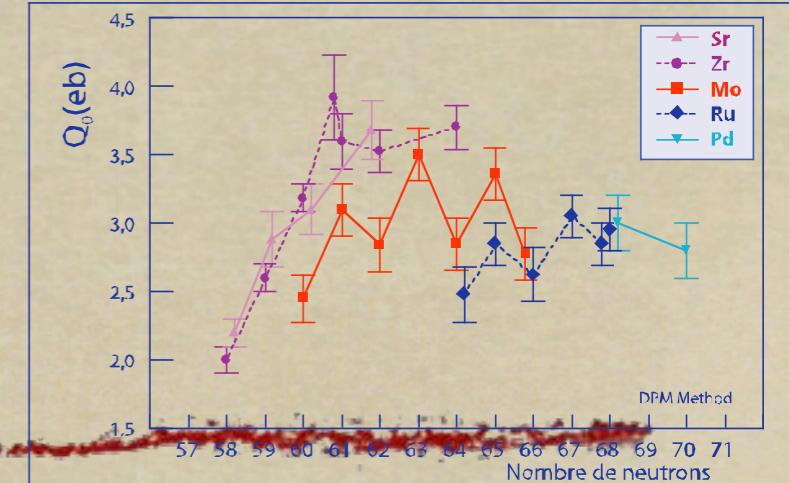
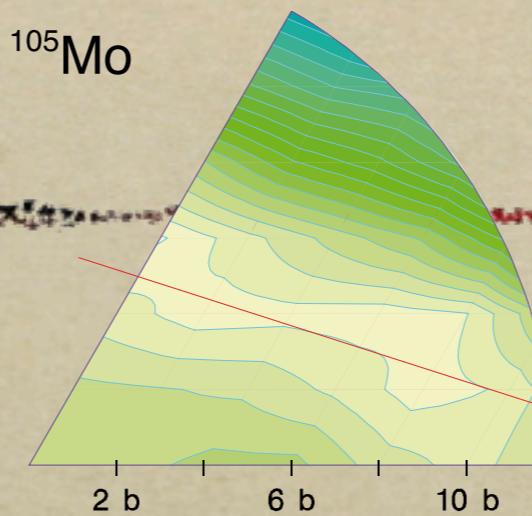
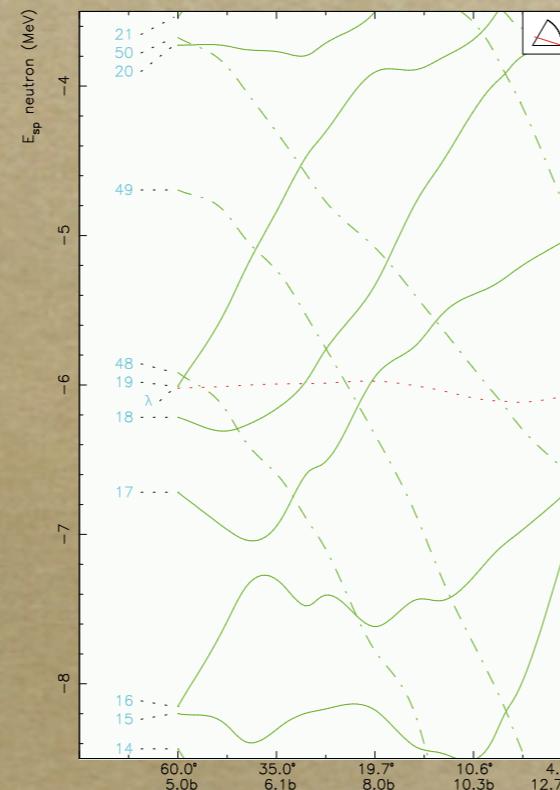
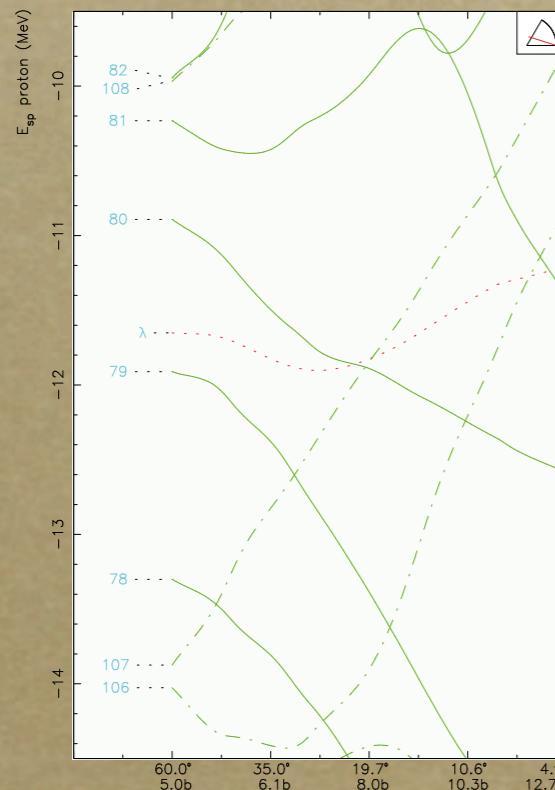
Experiments in Strasbourg

A ~ 100 Neutron-rich Nuclei

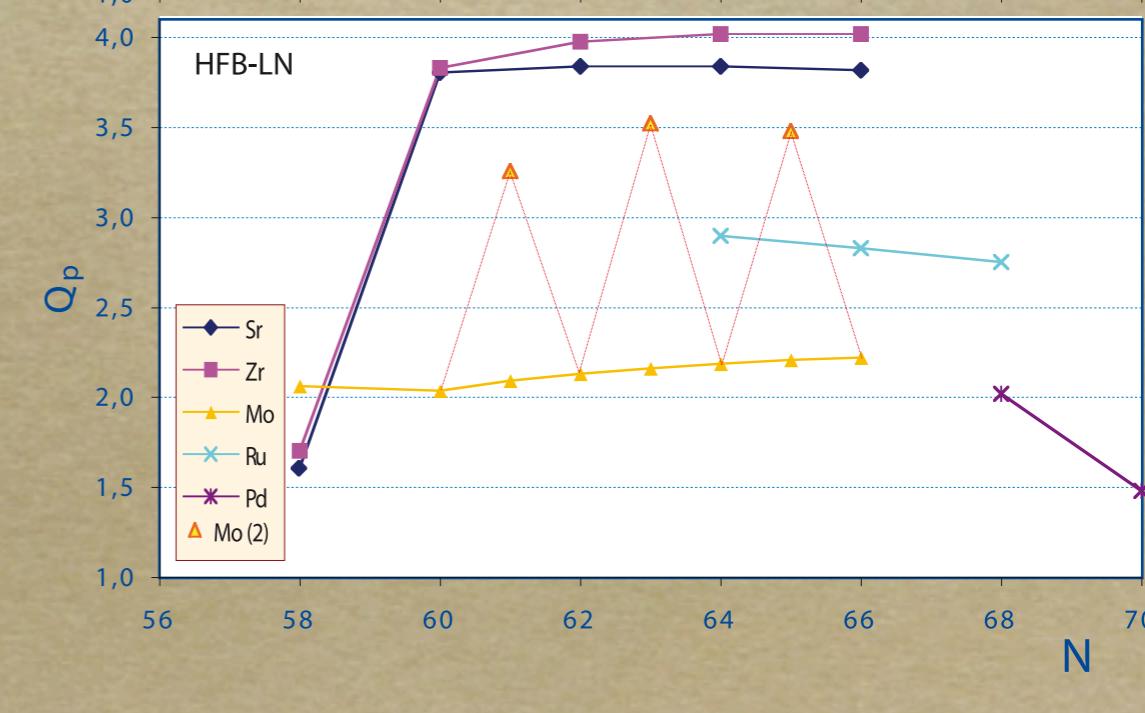
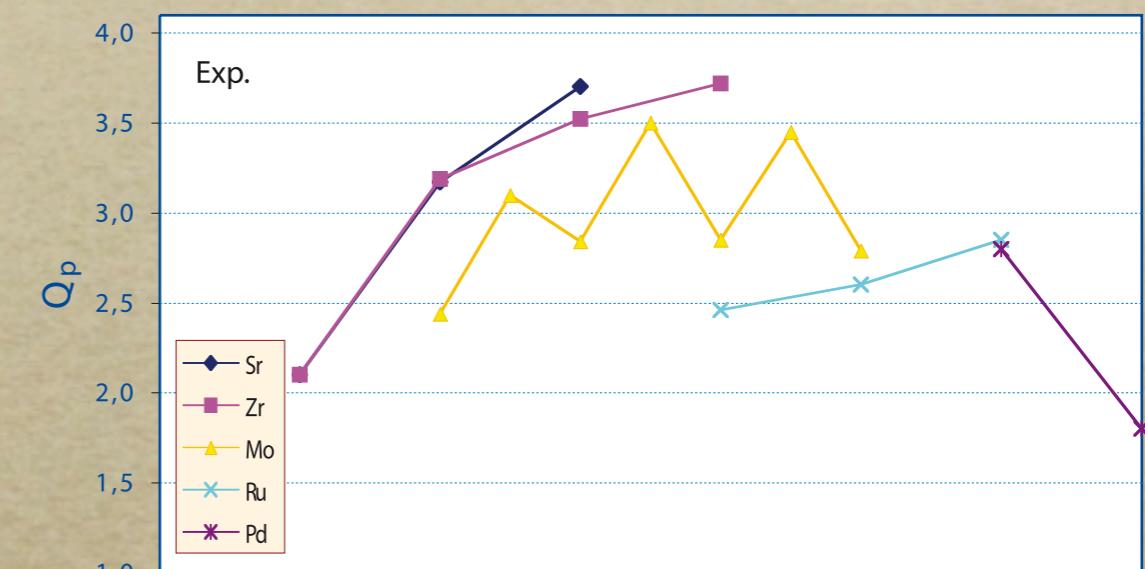
Spectroscopy



Diagonal cuts ...



Gamma-soft nucleus



N

Nuclear Pairing dependance on Rotation - even-even SD Bands

Spectroscopy of Yrast ^{192}Hg and ^{194}Pb SD bands

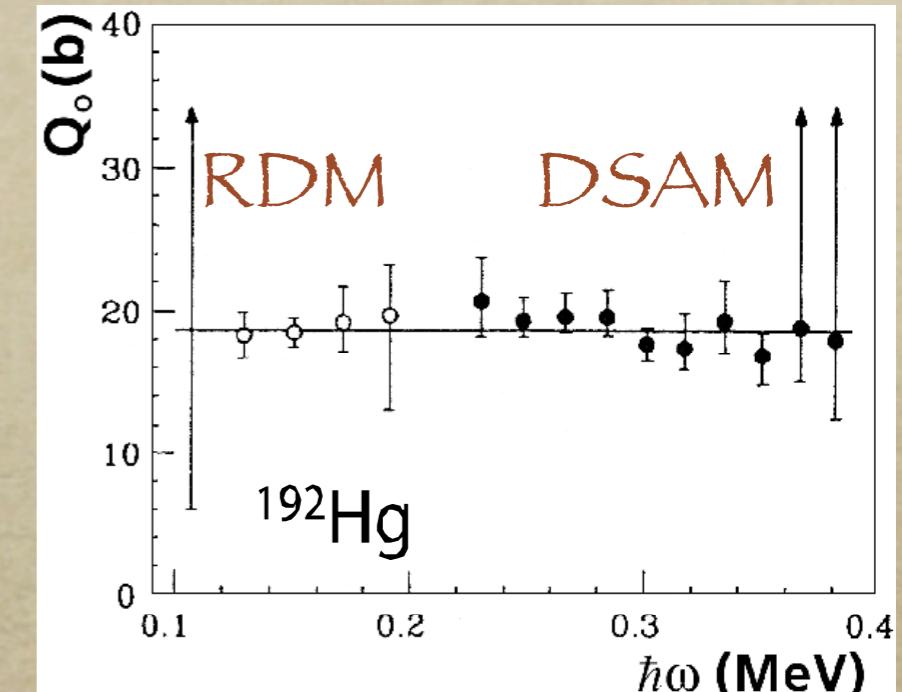
- Quadrupolar moment measurement

→ DSAM

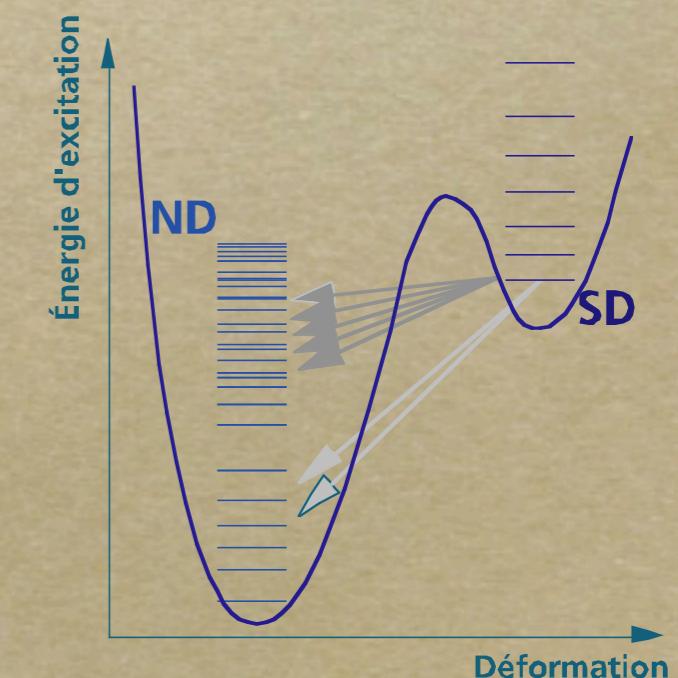
→ RDM

The deformation stays Constant from
higher spin of the SD-band up to the
lower spins of the band ...

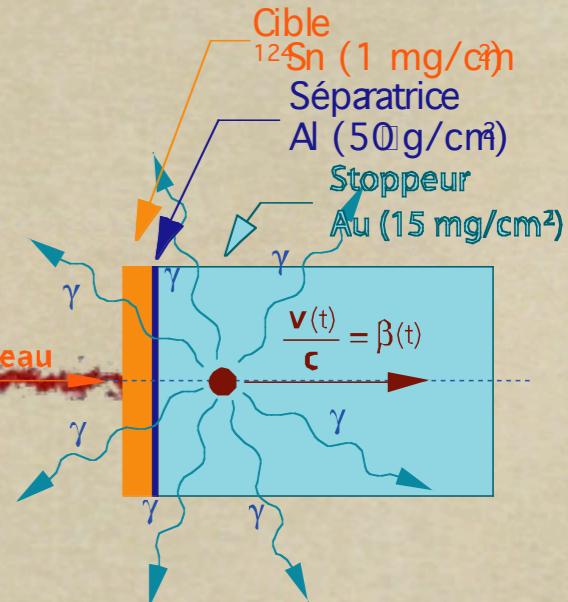
Best “lab” to study the influence of
rotation alone on nuclear pairing.



P. Willsau et al. Nucl. Phys A574 (1994) 560



A=150 Identical Bands and quadrupole moments



	protons	neutrons	Q_0 (H.S.)	Q_0 (C.R.)	Q_0 (HFB)	Q_0 (OH)	$\epsilon_2 (\epsilon_4)$
$^{148}\text{Gd}(\gamma)$	$6^2 \bullet \bullet$	$7^1 \bullet \bullet \bullet \circ \circ$	14,6 0,2	-	x	16,0 (14,7)	0,545 (0,029)
$^{148}\text{Gd}(2)$	$6^2 \bullet \bullet$	$7^1 \bullet \bullet \circ \bullet \circ \circ$	14,8 0,3	-	x	16,0 (14,7)	0,545 (0,029)
$^{148}\text{Gd}(5)$	$6^4 \circ \circ$	$7^2 \circ \circ \bullet \bullet \circ \circ$	17,8 1,3	-	x	19,6 (18,0)	0,618 (0,029)
$^{149}\text{Gd}(\gamma)$	$6^2 \bullet \bullet$	$7^1 \bullet \bullet \bullet \bullet \circ \circ$	15,0 0,2	-	15,5	16,5 (15,2)	0,555 (0,029)
$^{149}\text{Gd}(2)$	$6^2 \bullet \bullet$	$7^2 \bullet \bullet \bullet \circ \circ \circ$	15,6 0,3	-	-	16,7 (15,4)	0,556 (0,029)
$^{149}\text{Gd}(3)$	$6^3 \circ \bullet$	$7^1 \bullet \bullet \bullet \bullet \circ \circ$	15,2 0,4	-	-	17,4 (16,0)	0,576 (0,029)
$^{149}\text{Gd}(4)$	$6^4 \circ \circ$	$7^2 \bullet \bullet \bullet \circ \circ \circ$	17,5 0,6	-	-	19,3 (17,8)	0,612 (0,029)
$^{152}\text{Dy}(\gamma)$	$6^4 \bullet \bullet$	$7^2 \bullet \bullet \bullet \bullet \circ \circ$	17,5 0,4	18,5 0,5	17,5	18,9 (17,4)	0,582 (0,029)
$^{153}\text{Dy}(\gamma)$	$6^2 \bullet \bullet$	$7^3 \bullet \bullet \bullet \bullet \circ \circ$		18,4 0,5	17,6	-	-
$^{153}\text{Dy}(2)$	$6^2 \bullet \bullet$	$7^2 \bullet \bullet \bullet \bullet \bullet \circ$		17,9 0,5	17,2	-	-
$^{153}\text{Dy}(3)$	$6^2 \bullet \bullet$	$7^2 \bullet \bullet \bullet \bullet \circ \bullet$		18,2 0,5	17,2	-	-
Config ->	$6_x [301]1/2, -1/2$ $[301]1/2, +1/2$	$7^y [411]1/2, -1/2$ $[411]1/2, +1/2$ $[651]1/2, -1/2$ $[651]1/2, +1/2$ $[402]5/2, -1/2$ $[402]5/2, +1/2$	Experiment		Theory		

Identical bands correspond to similar quadrupole moments but to slightly different deformation (see last row)

DSAM experiments with same stopper :

$^{124}\text{Sn}(^{30}\text{Si}, 6-5n)^{148,149}\text{Gd}$ à 158 MeV (@EGII)

$^{120}\text{Sn}(^{36}\text{S}, 4n)^{152}\text{Dy}$ à 170 MeV (@EGII)

$^{120}\text{Sn}(^{34}\text{S}, 6-5n)^{152-153}\text{Dy}$ à 175 MeV (@GS)

Absolute errors due to stopping power remains but relative errors are small

HFB-LN (SLy4, pub, 2 cuts) Calculations

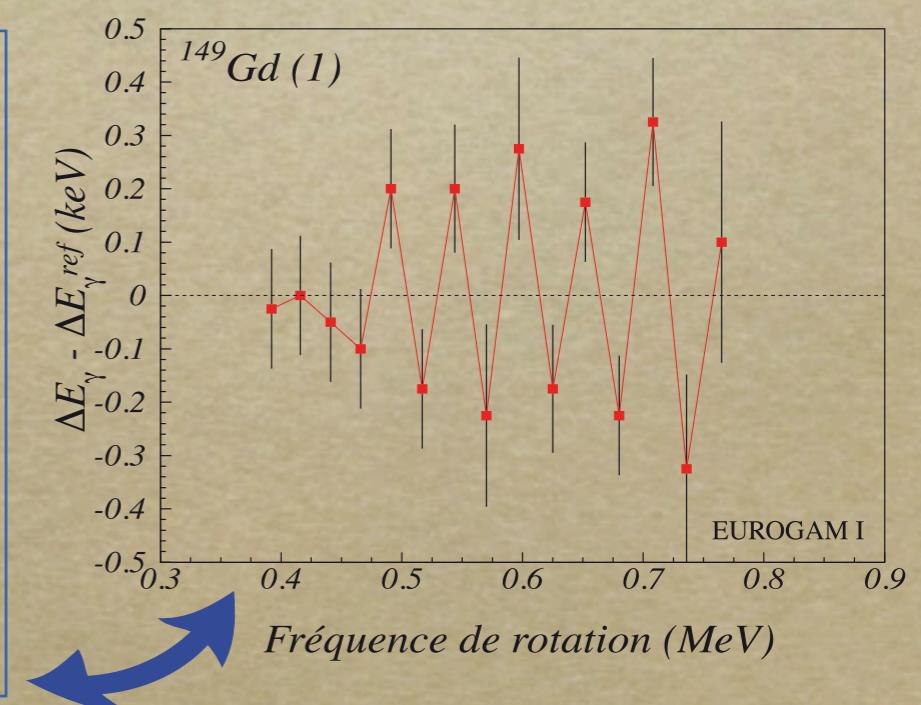
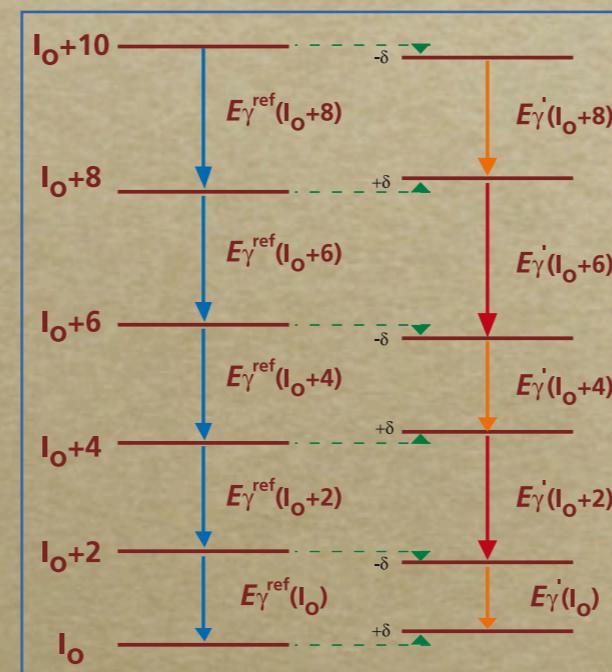
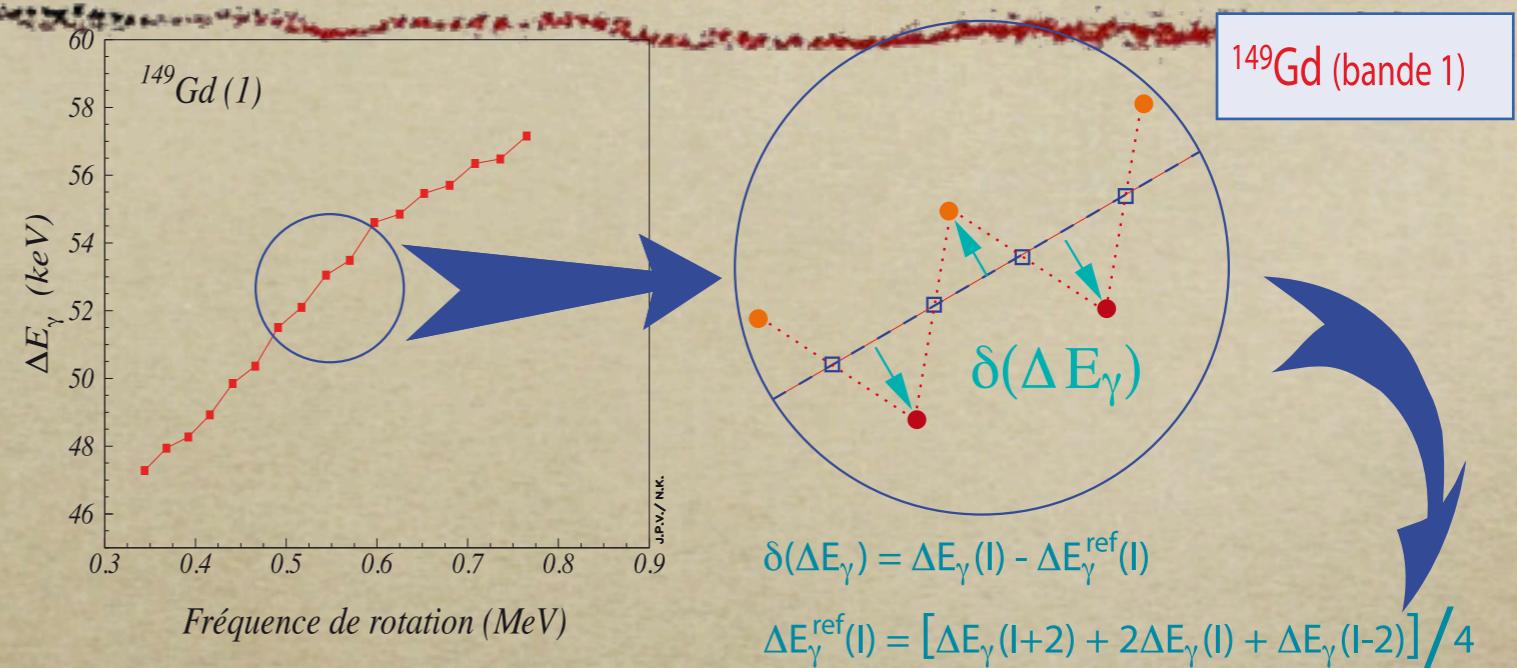
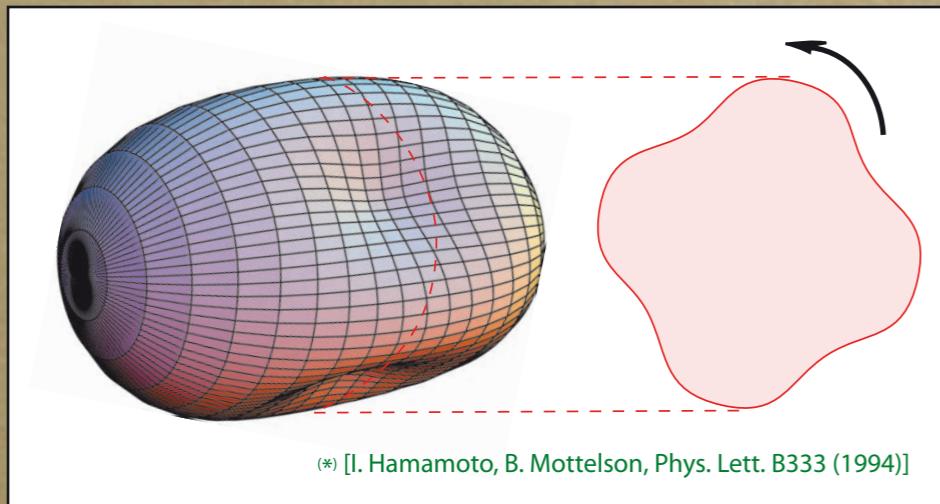
Good agreement with experimental quadrupolar moments

Important Influence of

intruders orbitals

C₄ symmetry ... Staggering...

Very small Phenomenon
 60 +/- 10 eV @ 20 MeV
 excitation energy ...

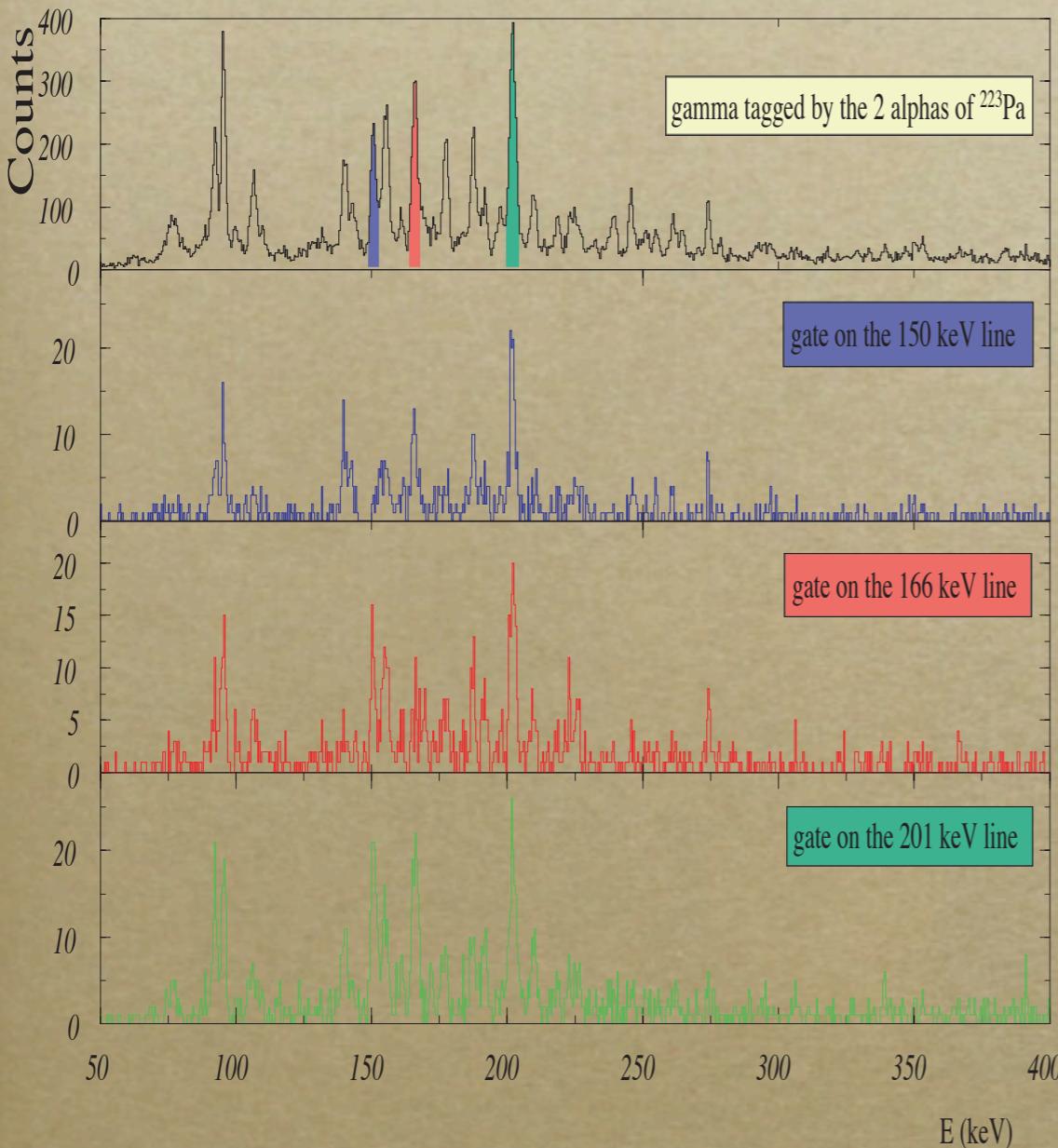


2 séquences de spin :
 I, I+4, I+8, ...
 I+2, I+6, I+10, ...

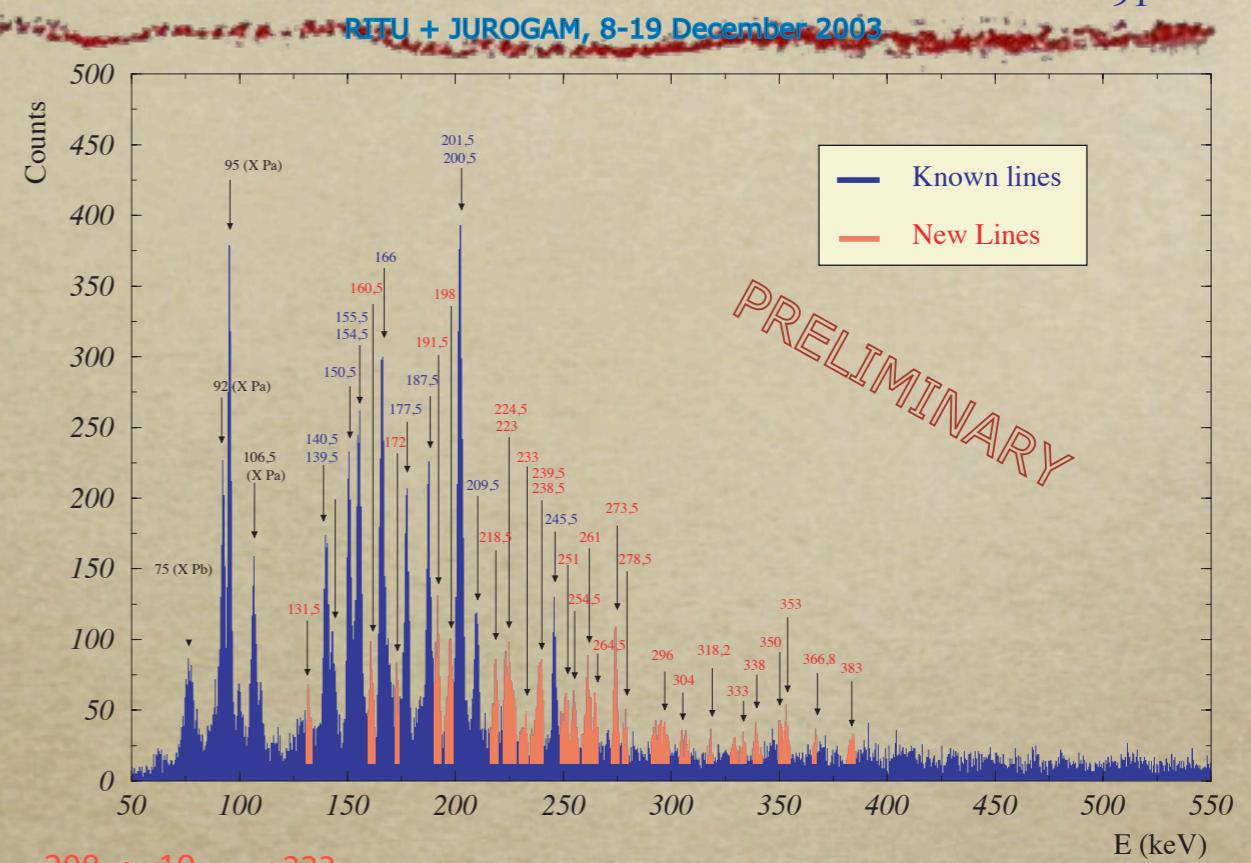
(*) [Flibotte et al., PRL71 (1993)]
 (***) [N. Kintz Thèse IReS/ULP 2000]

Octupole Deformation in ^{223}Pa

Gamma gated spectra Tagged by the 2 alpha lines of ^{223}Pa

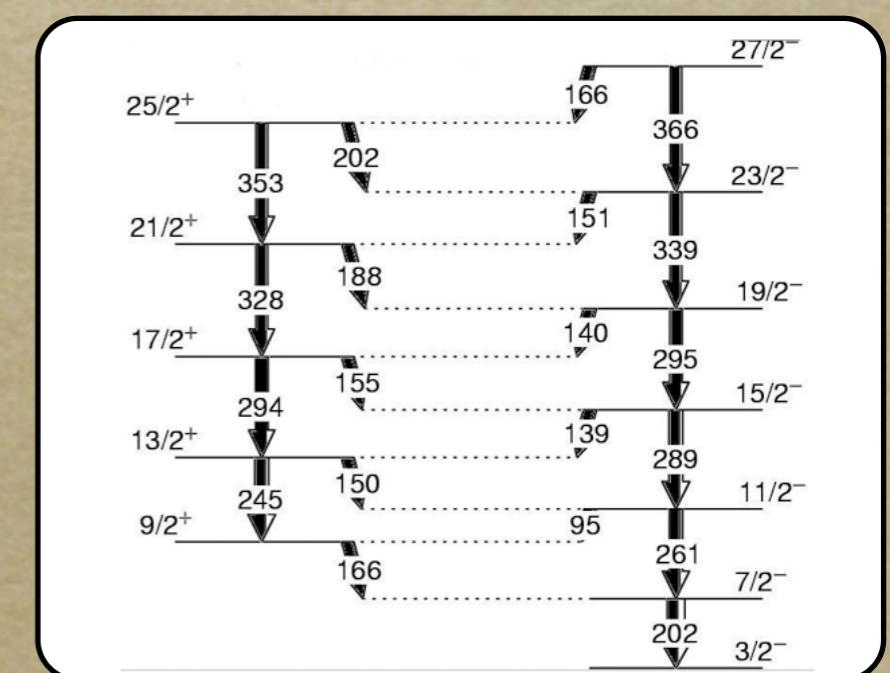


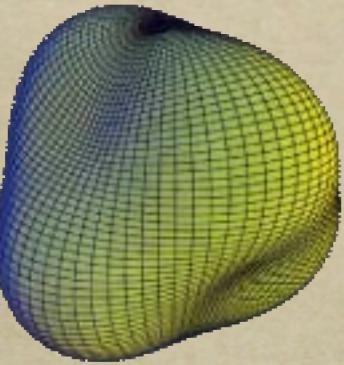
Gamma-rays spectrum Tagged by the 2 alpha lines of ^{223}Pa



Reaction: $^{208}\text{Pb}(^{19}\text{F},4\text{n})^{223}\text{Pa}$ @ 99 MeV,

$v/c = 0.8 \%$,
 $e = 150 - 250 \mu\text{g}/\text{cm}^2$,
 $I \sim 40 \text{ pnA}$,
 $\sigma \sim 100 \mu\text{b}$

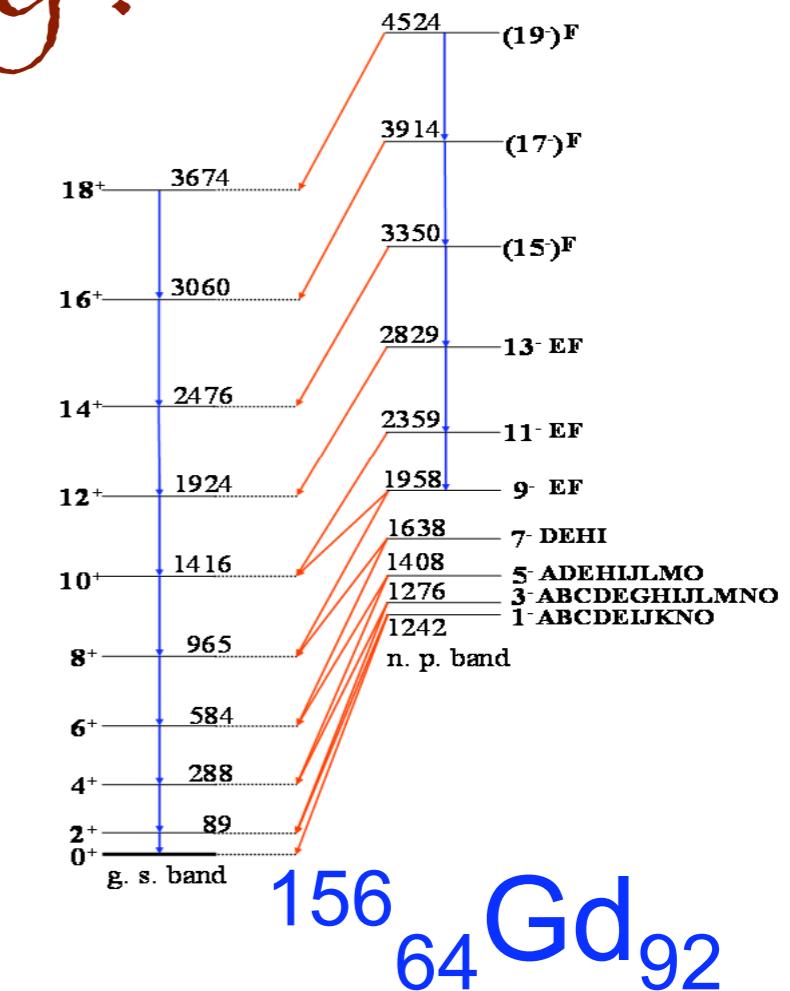
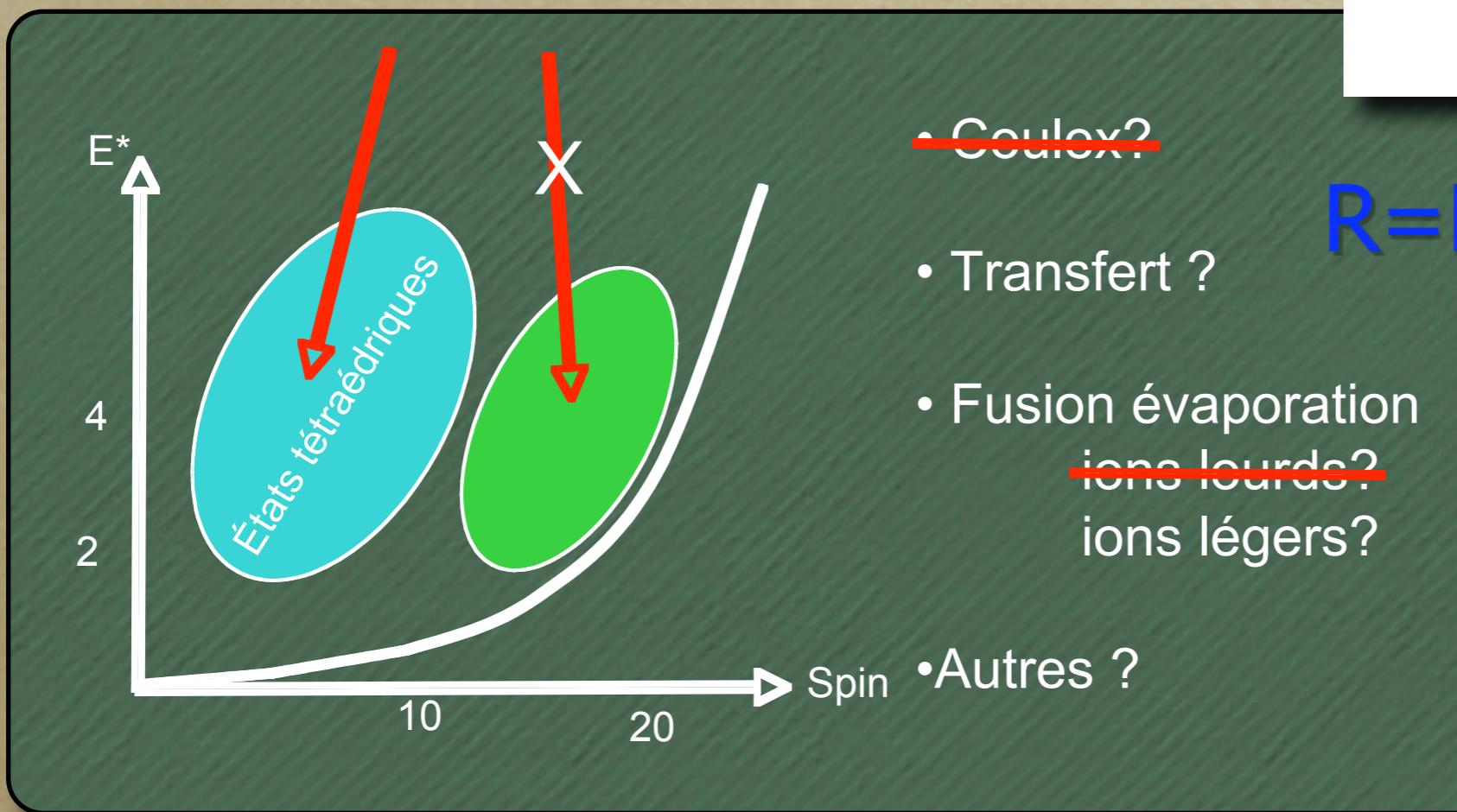




Higher order symmetry : Tetrahedral Shapes ?

Tetrahedral Fingerprints:

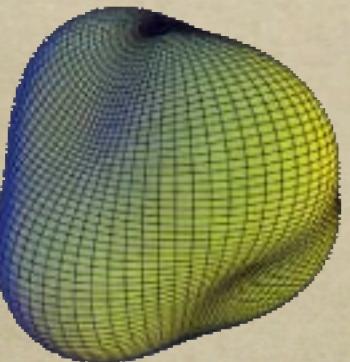
- Vanishing Q₂ (rotational bands without E2's)
- Large B(E1; I --> I-1)
 - Branching ratios are spin dependent (difference with usual octupole)



$$R = B(E2)_{in} / B(E1)_{out}$$

Réactions possibles:

- A=155Gd(n, γ)
- D=156Gd(n,n' γ)
- E=154Sm(α ,2n γ)
- F=150Nd(^{13}C , α 3n γ)
- G=Coulomb Excitation
- L=158Gd(p,t)
- M= 154Gd(t,p)
- ?? 7Li transfert massif de 2p (7Li,p4n)



Higher order symmetry : Tetrahedral Shapes ?

The tetrahedral nuclei are predicted around the following new shell closures:

$$(Z_t, N_t) = (32, 40, 56, 64, 70, 90, 136)$$

Corresponding to the doubly magic nuclei:

64,72,88

Ge ($Z=32$)

80,96,110

Zr ($Z=40$)

112,126

Ba ($Z=56$)

134,154

Gd ($Z=64$)

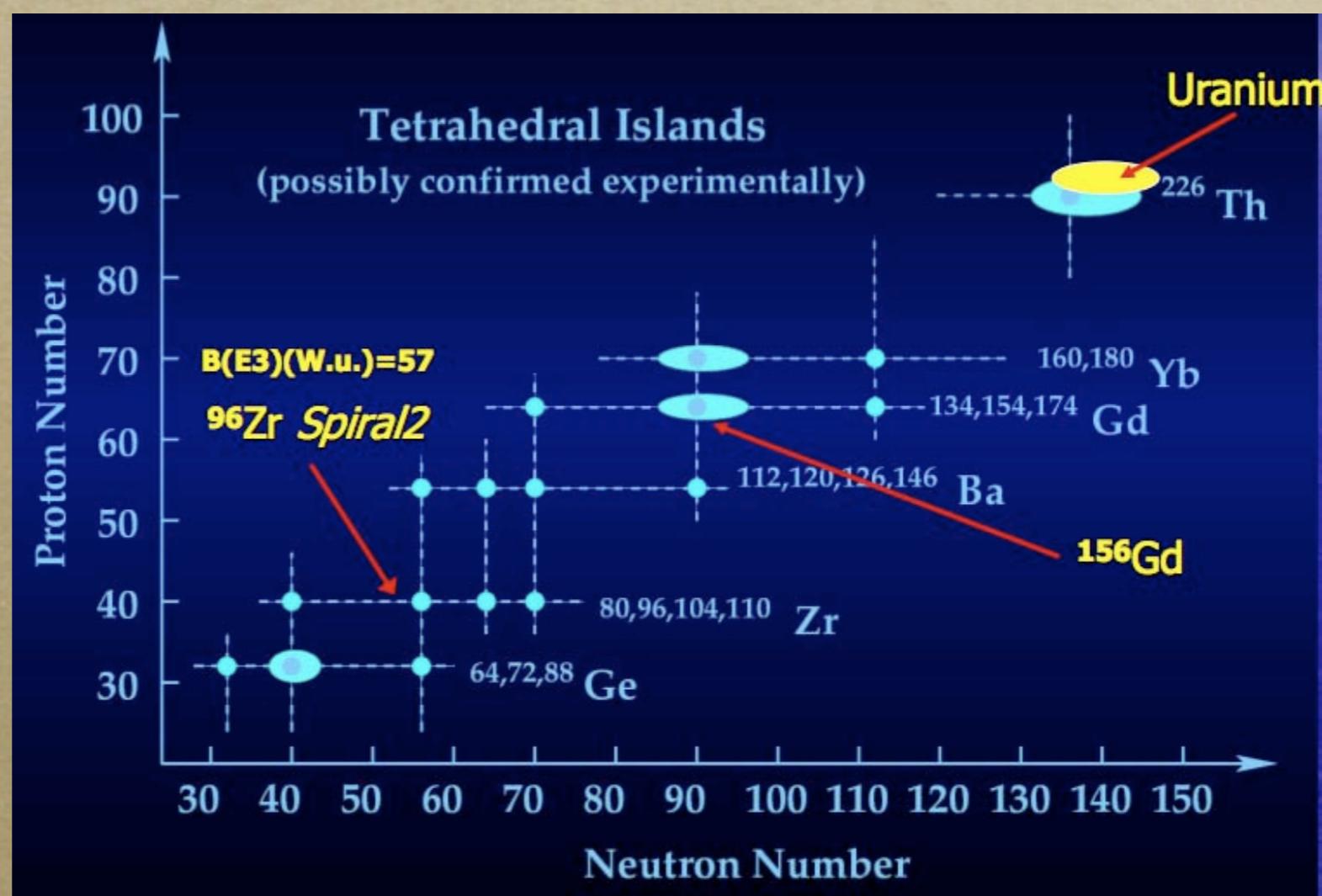
160

Yb ($Z=70$)

226

Th ($Z=90$)

Candidates ?



Summary

- ⦿ Preliminary considerations
- ⦿ Excitations of the nuclei; case of rotationnal bands
- ⦿ Effect of Nuclear deformation
- ⦿ Experimental toolboxes & selected cases

Pairing Correlations in Rotating Nuclei and the Frequency-Deformation Scaling

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Received January 18, 1990; accepted February 16, 1990

Abstract

The dynamical pairing correlations are discussed using the rotating harmonic oscillator model and the RPA formalism. The dependence of the pairing strength distribution on rotational frequency and deformation is given special attention. In particular, the influence of coupling between different oscillator shells is analyzed in detail. Explicit formulae are given for the overlap matrix elements between the rotating and nonrotating states of the cranked harmonic oscillator.

1. Introduction

The competition between the short-range pairing force giving rise to a superfluid structure and the Coriolis and centrifugal forces acting in a rotating atomic nucleus has been discussed for several years starting with a classical work by Mottelson and Valatin [1]. At very high spins the Coriolis and centrifugal forces may become strong enough as to destroy to a large extent the superfluid pairing correlations. In the description of nuclear structure in terms of a mean-field approximation (such as, e.g. the Hartree-Fock-Bogolyubov-Cranking model or its simpler version — the Rotating-BCS model, RBCS) this effect manifests itself by the existence of a critical angular frequency ω_c of rotation below which the pairing-gap Δ collapses. In this picture the static pair deformation (corresponding to $\Delta \neq 0$) disappears. Nevertheless, the short-range pairing interactions may still play an important role by creating a dynamical type of correlations usually referred to as a pair-vibrations [2]. At this point it is worthwhile to stress that the conventional division into the "static" and "dynamic" pairing makes sense only within the mean field theory where correlations are neglected and the particle number symmetry is spontaneously broken. The mean field approach is useful if correlations can be added and the broken symmetry restored with only minor perturbation of the intrinsic state. In a general case some more powerful methods such as for example the particle number projection before variation (FBCS) or the generator coordinate method (GCM) could be employed. For a system with a finite number of particles, like the atomic nucleus, the mean field approximation breaks down around the pairing phase transition from superfluid to normal phase (for more details concerning this point we refer reader to Ref. [3] and refs. quoted therein). Consequently, the vibrational corrections obtained within the RPA method cannot cure this pathological behaviour near the critical point. However, both below and above ω_c the

vibrational approximation has proved to be very accurate [4-6].

The systematics of high-spin experimental data indicate that at large rotational frequencies a gradual transition to the unpaired regime takes place [7]. Indeed, the near-yrast excitations observed in the 40–50 spin region have characteristic features that are not consistent with the quasiparticle picture [8].

The recent discovery of superdeformed (SD) rotational bands in the rare earth nuclei around ^{132}Dy (see, e.g. Ref. [9]) opens a possibility to study a competition between rotation, deformation and pairing in very extreme conditions. Due to the particularly low density of single-particle states in the SD configurations [10-13] pairing correlations are seriously quenched already at low rotational frequencies. A further reduction of pairing is then caused by the angular momentum alignment of high- j nucleons [14, 15] and the Coriolis-antipairing effect (CAP). The rotational frequencies in the SD bands are in the range of $500 \text{ keV} < \hbar\omega < 800 \text{ keV}$. At such high angular momenta the static pairing is gone [13, 15-17] and pairing fluctuations become important. When dynamical correlations are taken into account in calculations, the agreement between calculated SD rotational bands and experimental data is improved [14, 15, 17, 18]. This is due to the additional (negative) contribution to the total spin coming from the frequency-dependent pairing correlation energy.

In the previous paper [19] the importance of pairing fluctuations in fast rotating and well deformed nuclei was studied using the rotating harmonic oscillator model (rho). It has been shown that the pairing energy and the associated angular momentum (de)alignment depend on ω through the ratio ω/ϵ , where ϵ is a quadrupole deformation parameter. Such a rotation-deformation scaling can be easily understood as the Coriolis force is proportional to ω while the splitting between Nilsson orbitals is roughly proportional to ϵ . However, in Ref. [19] the couplings between different oscillator shells were neglected, an approximation that could modify some results for very elongated shapes. For example, the contributions because of the $\Delta N = 2$ coupling give around 10% of the total moment of inertia at $\epsilon \approx 0.6$ [20] and they can influence the calculated equilibrium deformations at very high spins [21]. The main objective of this study was, therefore, to check whether the concept of scaling can still be applied in the general case. As a by-product the explicit expressions for the



Pairing Correlations in Rotating Nuclei and the Frequency-Deformation Scaling

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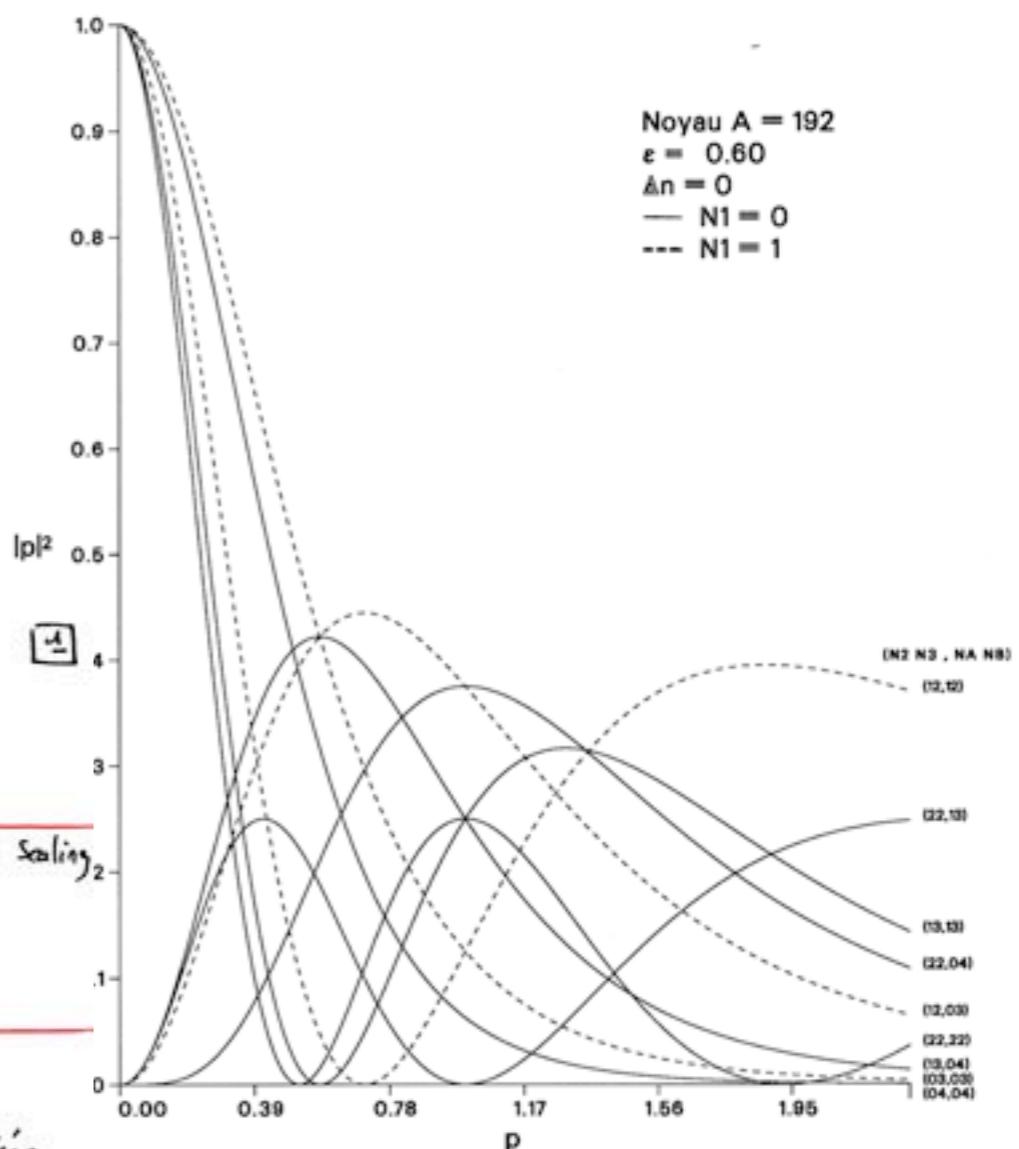
Abstract

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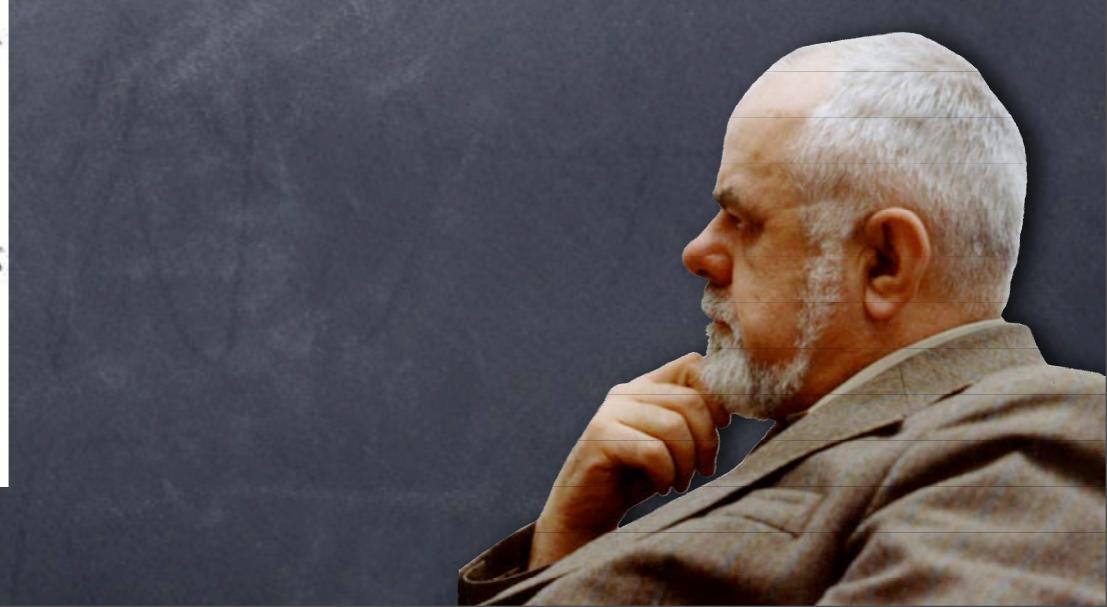
Force de pairing versus deformation

**STAGE DE DEA**Etude de l'article suivant :Pairing Correlations in Rotating Nuclei and the Frequency Deformation Scaling

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PHYSICA SCRIPTA. VOL 42, 515-521, 1990

Dans cet Article les corrélations dynamiques de Pairing sont discutées dans le cadre du modèle de l'oscillateur harmonique en rotation et du formalisme de la RPA. On donne une importance toute particulière à l'intensité de la force de pairing. L'analyse de l'influence du couplage de plusieurs couches de l'oscillateur est faite en détail. Des formules explicatives des recouvrements des fonctions d'onde en rotation et non tournante sont également données ici.



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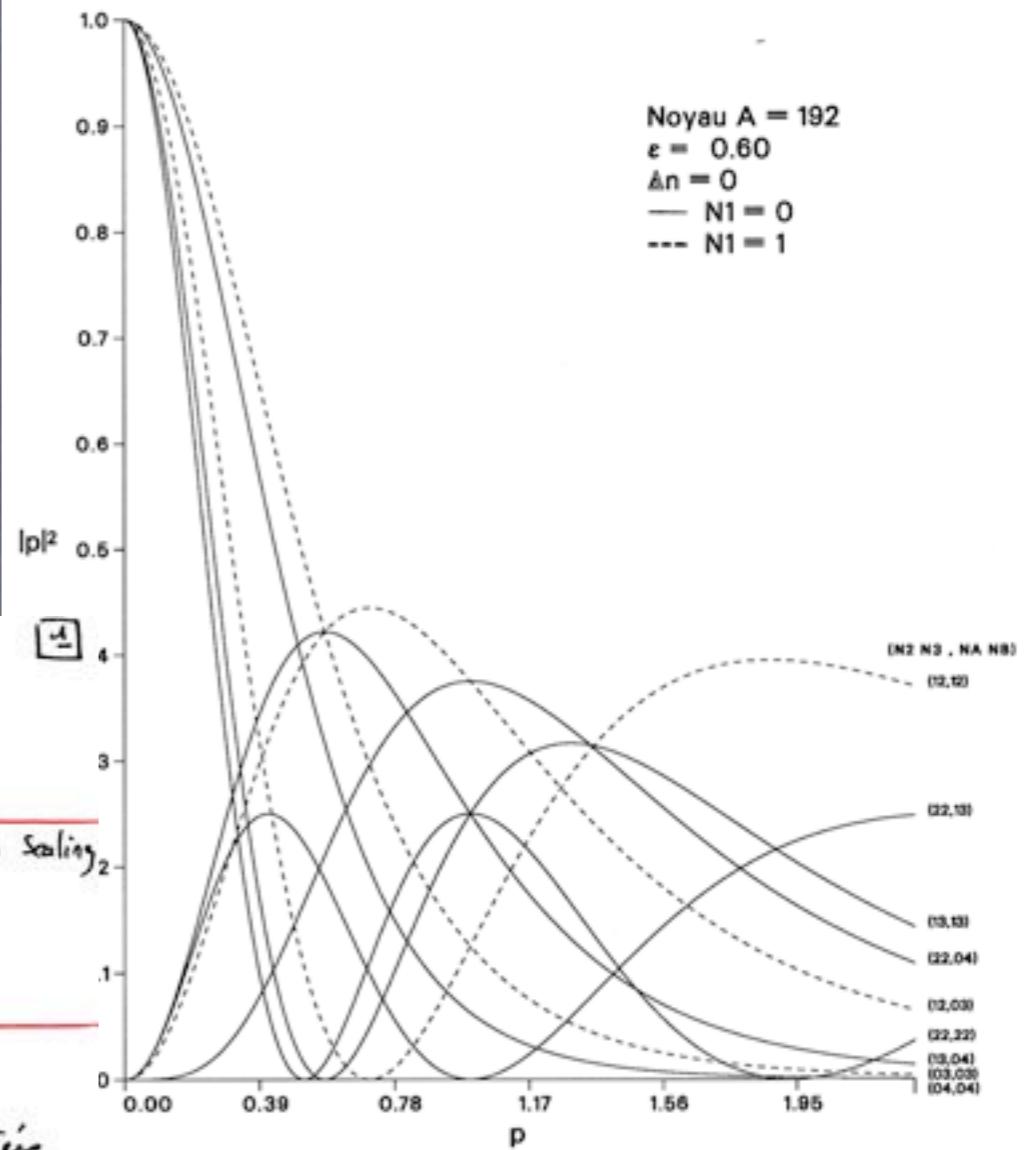
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