

# Super Heavy Elements and the Limits of Nuclear Stability

**UEE 2009**

**European Summer University**

"The Secrets of the Atomic Nucleus"

Strasbourg, France, June 28 - July 4, 2009



*Université de Strasbourg, France  
Strasbourg, July 3<sup>rd</sup> 2009*

Dieter Ackermann

Helmholtzzentrum für Schwerionenforschung GmbH



# **Super Heavy Elements and the Limits of Nuclear Stability**

**Dieter Ackermann, GSI Darmstadt, Germany**

## **Outline**

- 1. Introduction**
- 2. Reaction Mechanism of Heavy Ion Collisions at the Coulomb Barrier**
- 3. Synthesis and Investigation of Superheavy Nuclei**
- 4. Nuclear Structure of Heavy and Superheavy Nuclei**
- 5. Additional Methods**



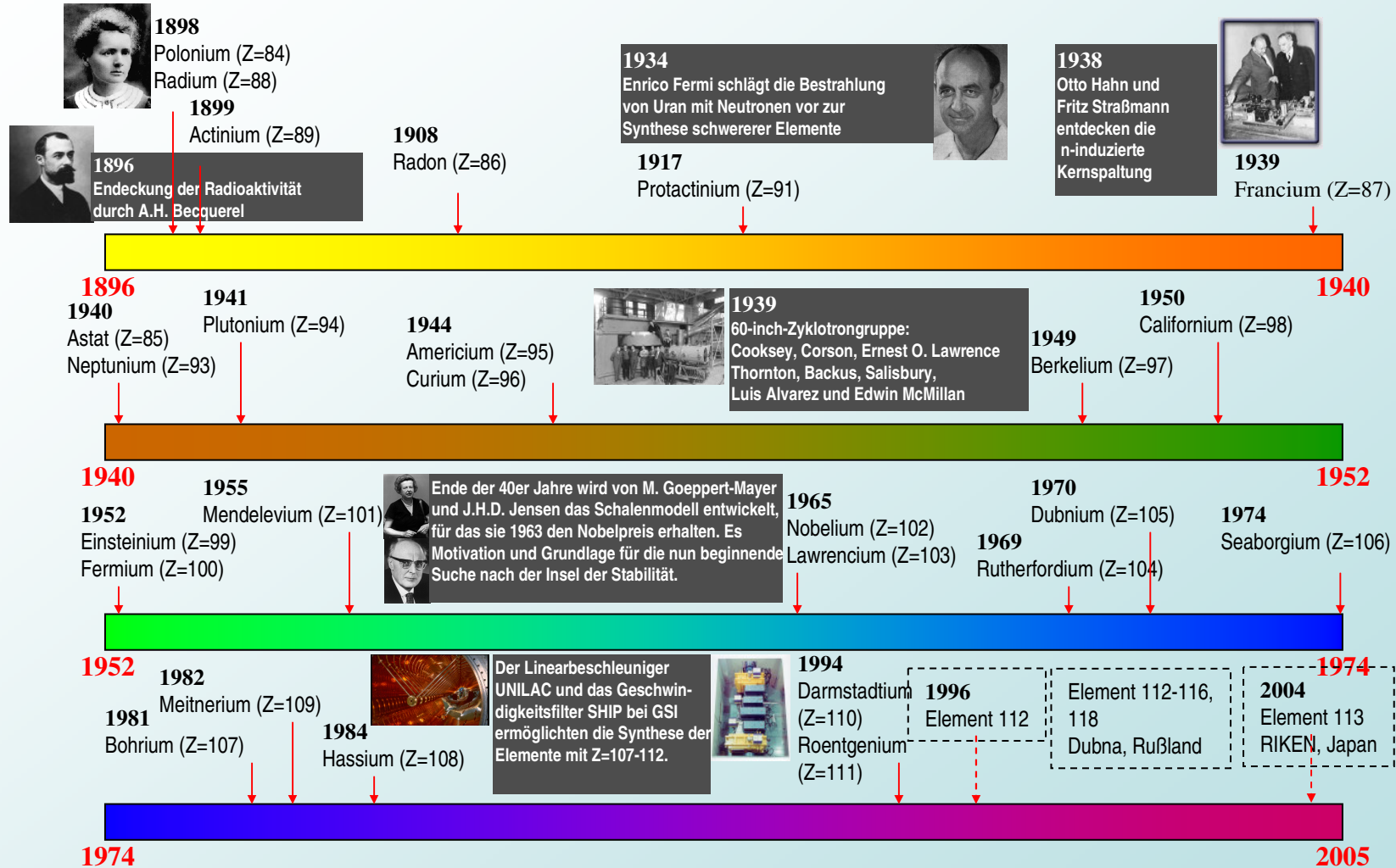
# History

## Outline

1. Introduction
2. Reaction Mechanism of Heavy Ion Collisions at the Coulomb Barrier
3. Synthesis and Investigation of Superheavy Nuclei
4. Nuclear Structure of Heavy and Superheavy Nuclei
5. Additional Methods



# Geschichte der Entdeckung und Synthese Schwerer Elemente





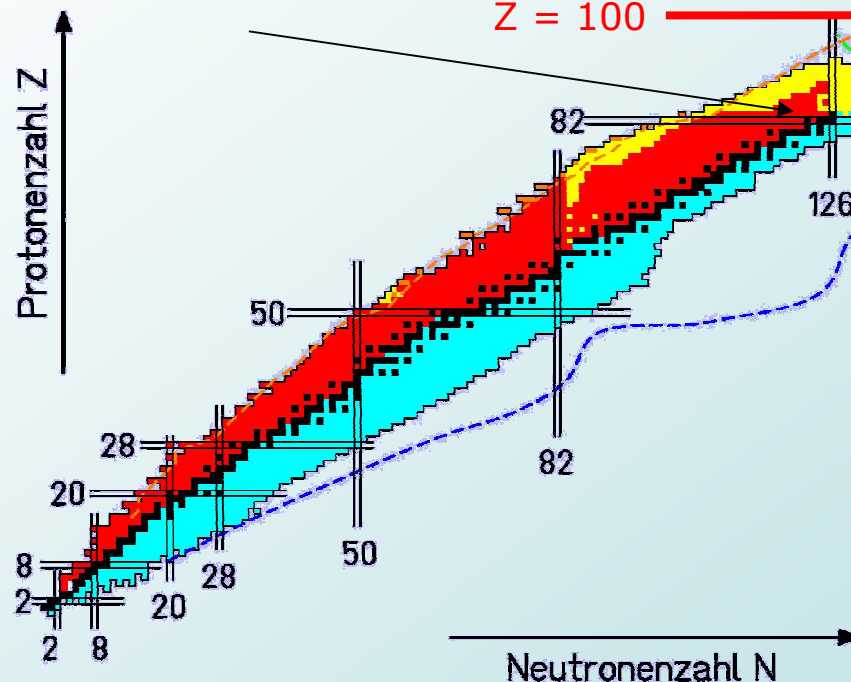
# The Chart of Nuclides

## – the "Playground" for Nuclear Physics I

### chart of nuclides:

- representation of the isotopes in the Z-N-plane
- isotope: atom (nucleus) of an element with different number of neutrons

Pb (lead) and Bi (bismuth)



island of stability

?

126  
120  
114

184

# SHE

U (uranium) and Th (thorium)

- black:** stable isotope
- red:**  $\beta^+$ -unstable isotope
- blue:**  $\beta^-$ -unstable isotope
- yellow:**  $\alpha$ -unstable isotope
- green:** spontan fission

# Reaction Mechanism of Heavy Ion Collisions at the Coulomb Barrier

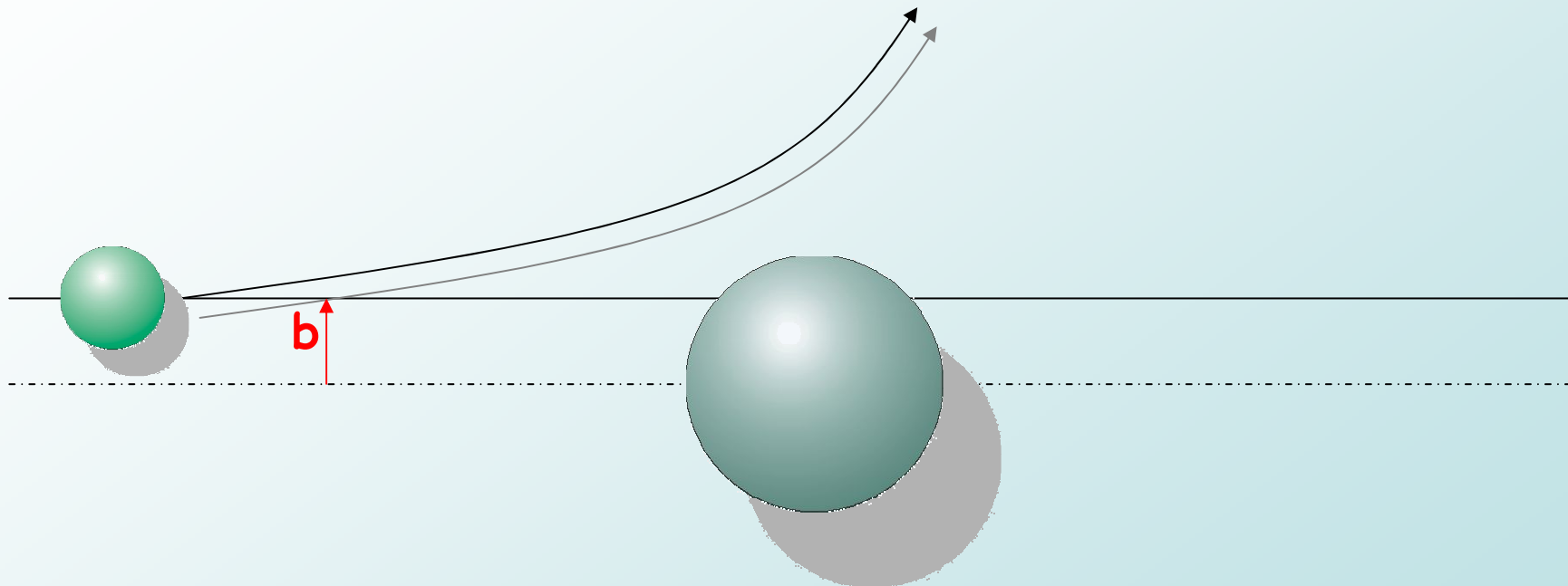
## Outline

1. Introduction
2. Reaction Mechanism of Heavy Ion Collisions at the Coulomb Barrier
  - Competing reaction channels
  - Fusion excitation function
  - The concept of barrier distribution
  - The compound nucleus spin distribution
3. Synthesis and Investigation of Superheavy Nuclei
4. Nuclear Structure of Heavy and Superheavy Nuclei
5. Additional Methods

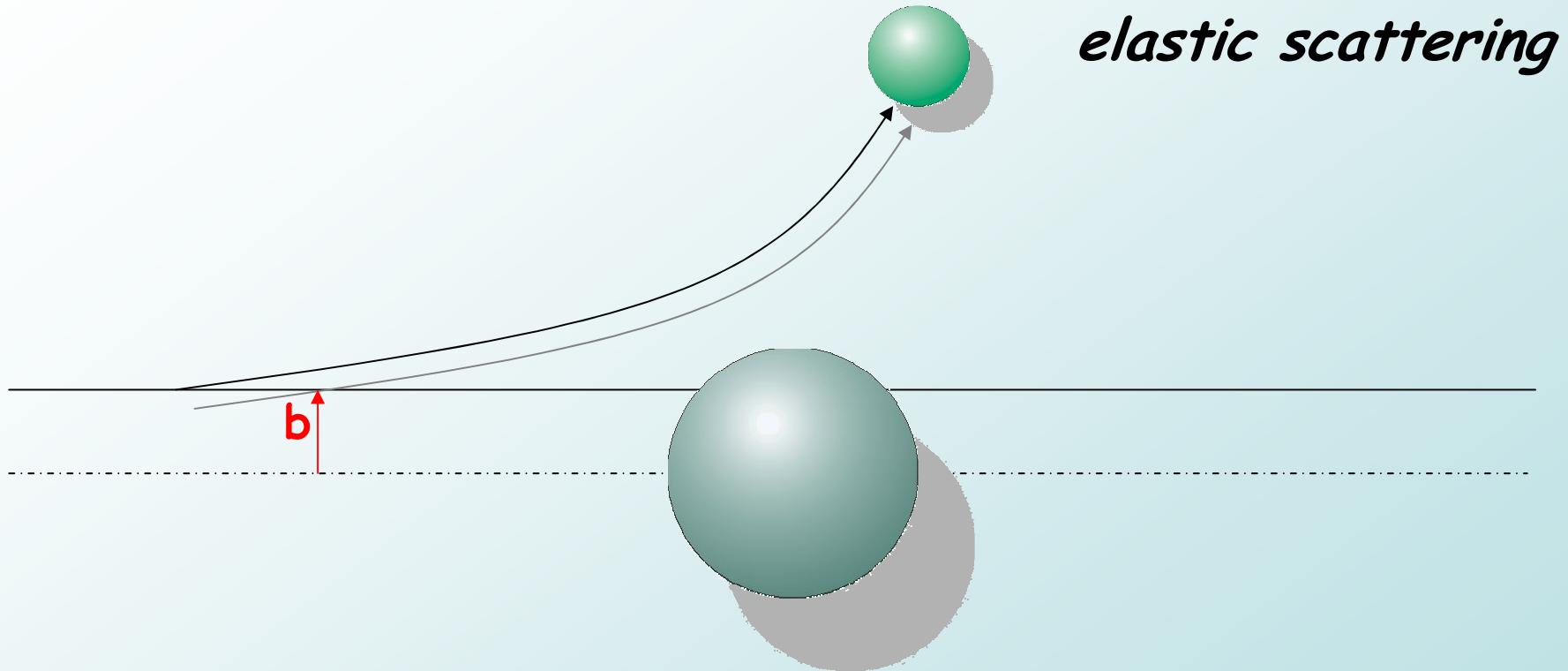


# Heavy Ion Reactions @ the Coulomb Barrier

*elastic scattering*

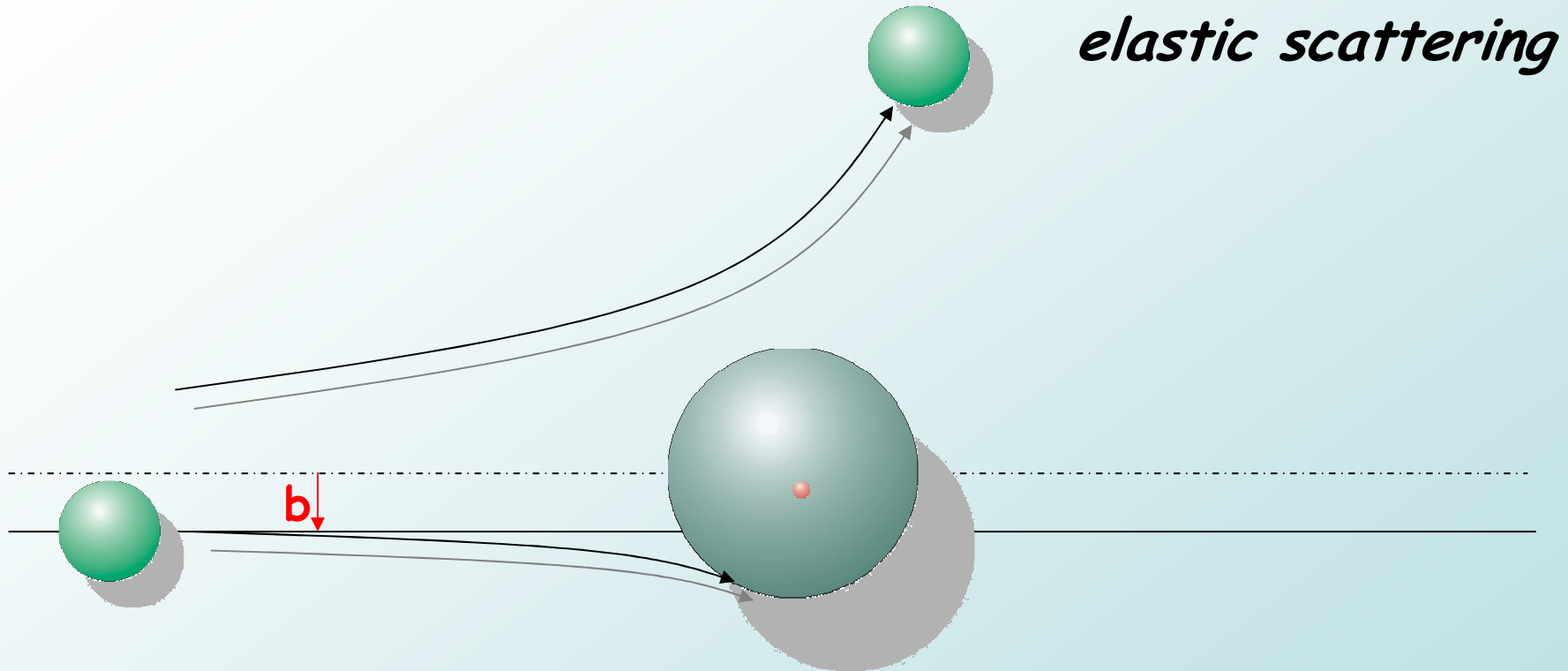


# Heavy Ion Reactions @ the Coulomb Barrier

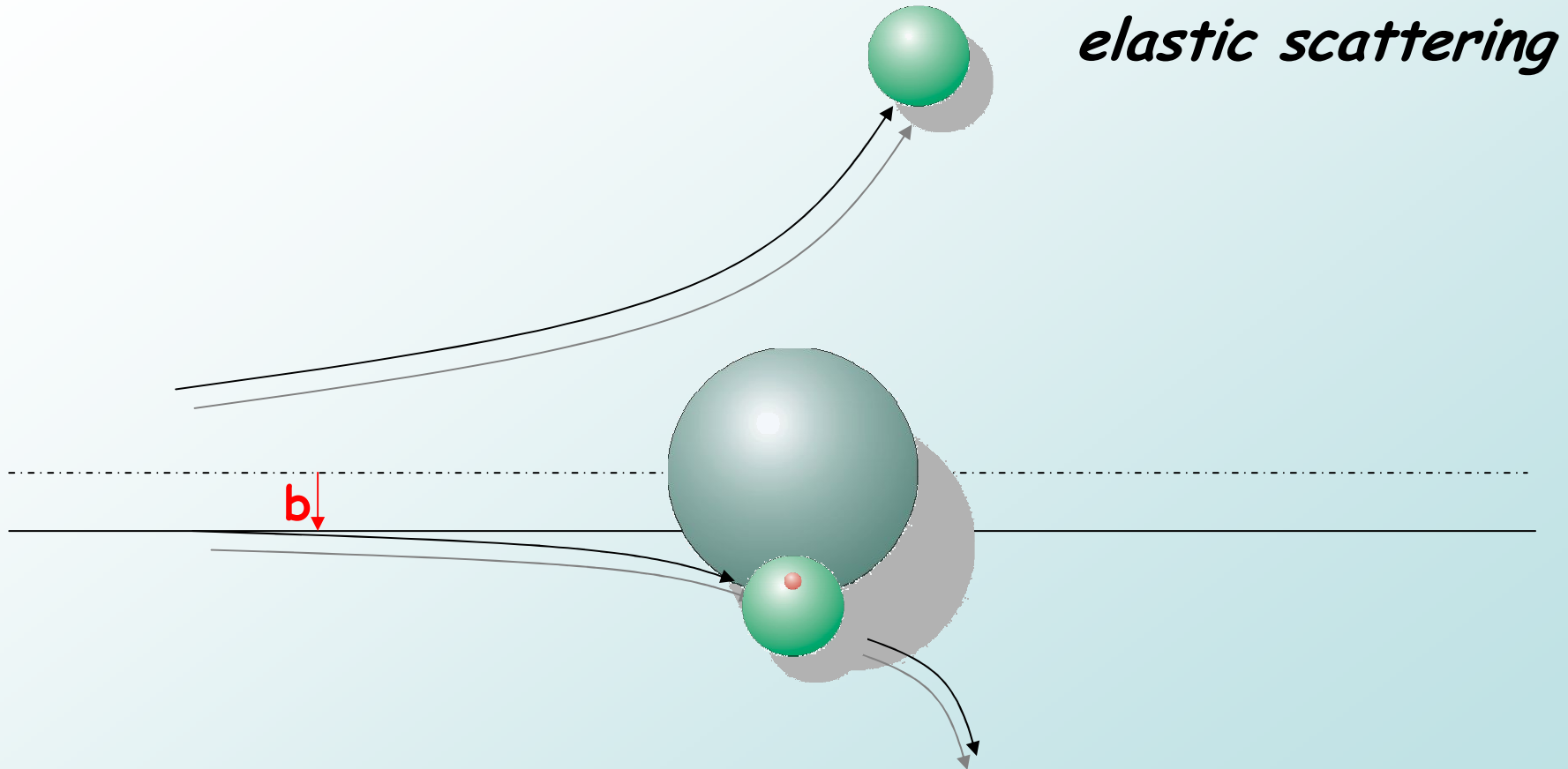




# Heavy Ion Reactions @ the Coulomb Barrier



# Heavy Ion Reactions @ the Coulomb Barrier

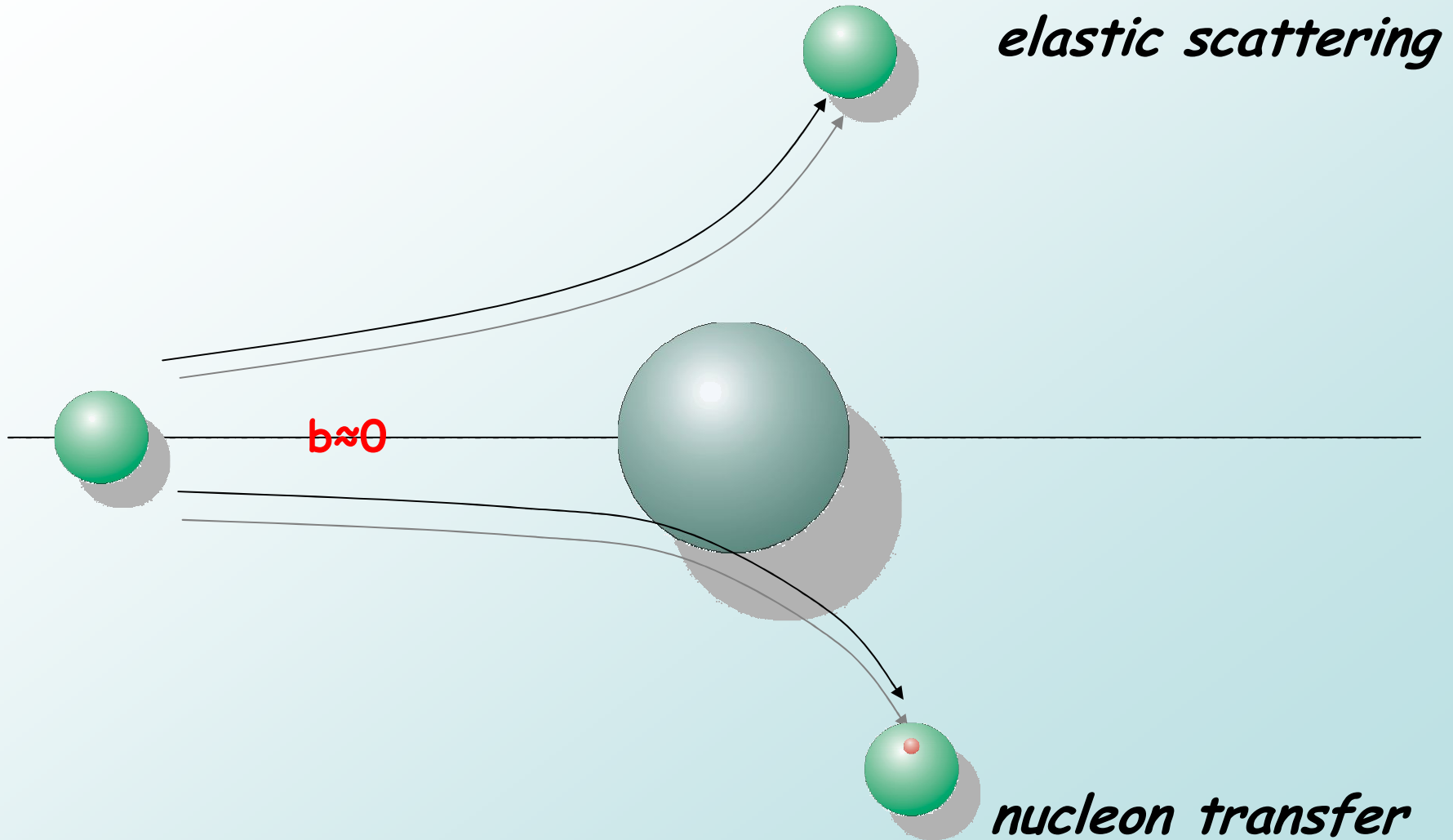


*elastic scattering*

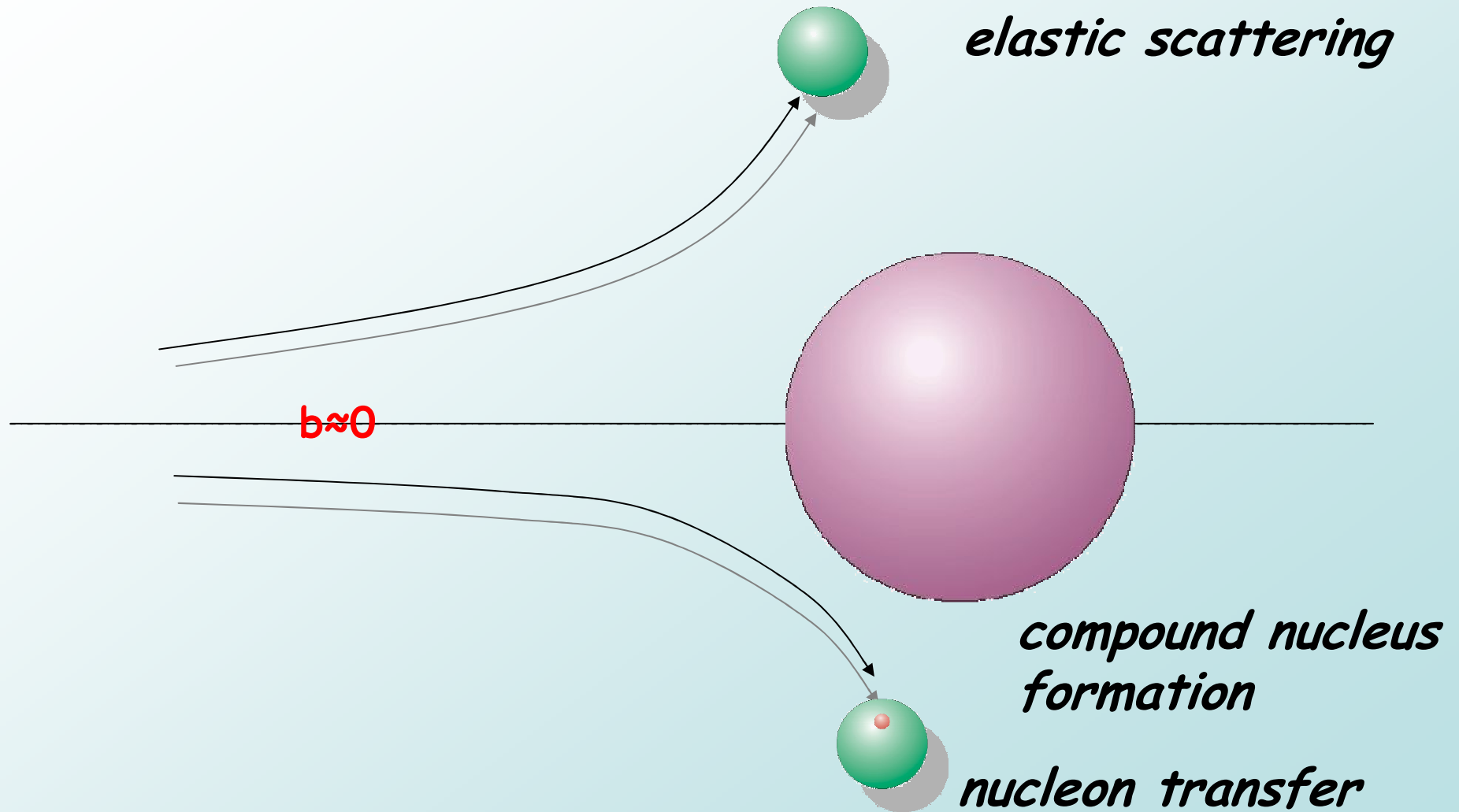
*nucleon transfer*



# Heavy Ion Reactions @ the Coulomb Barrier

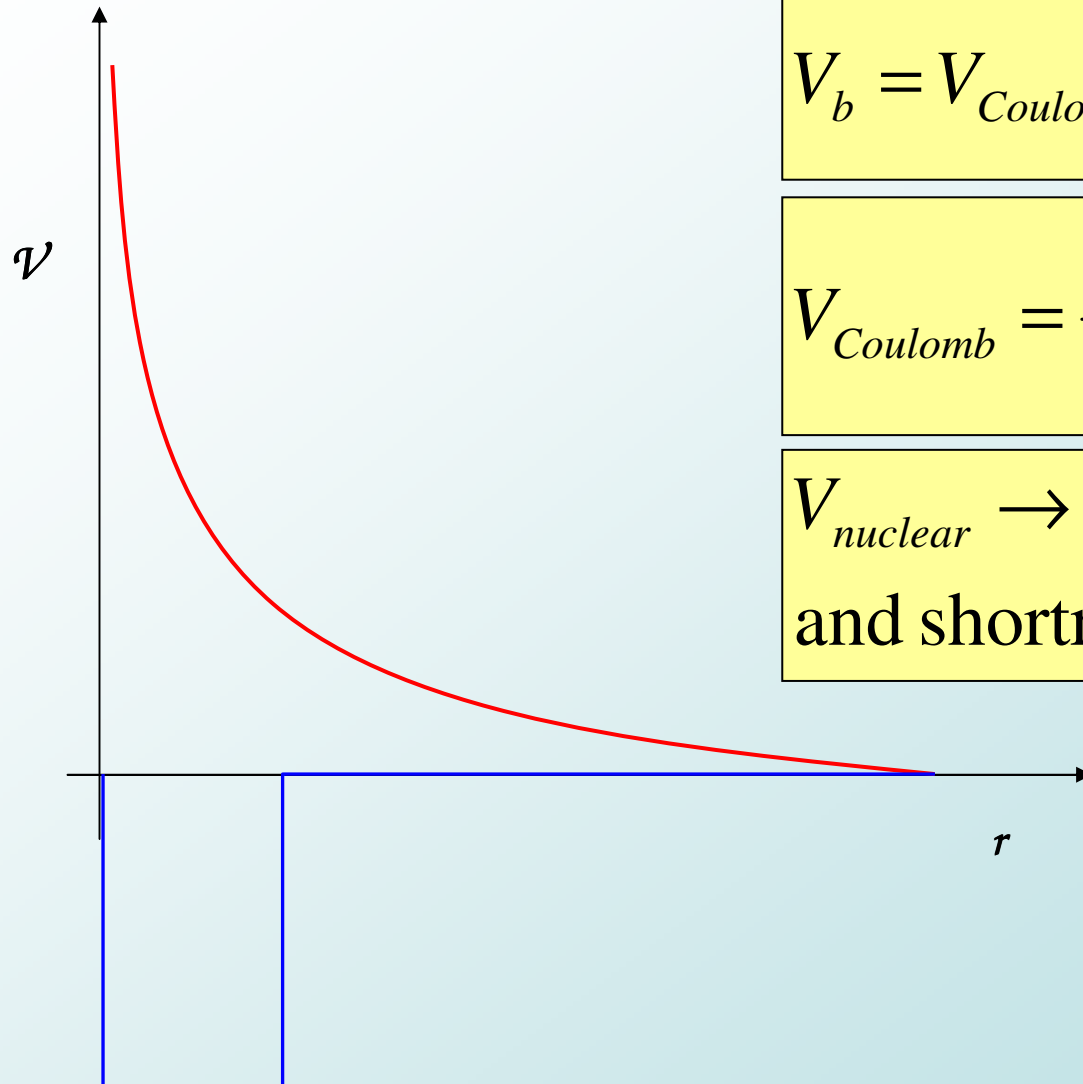


# Heavy Ion Reactions @ the Coulomb Barrier





# The Nuclear Potential

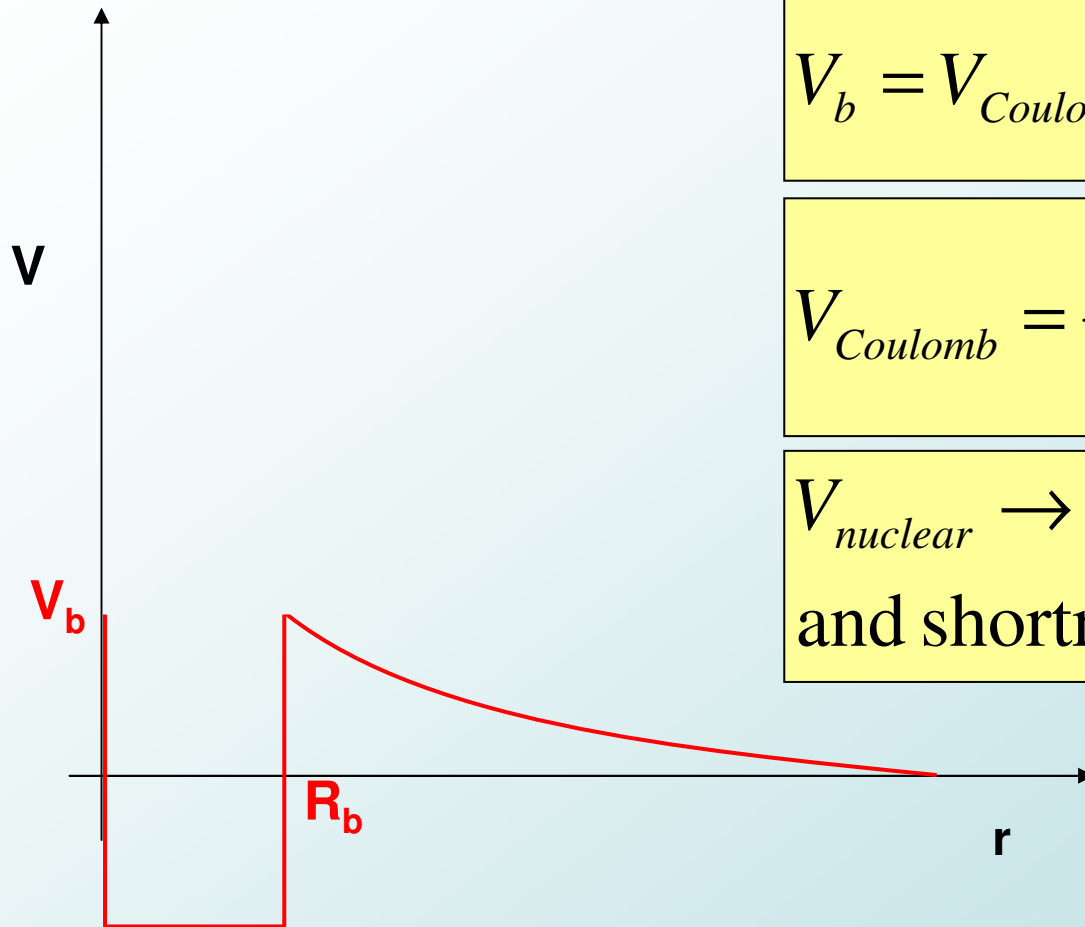


$$V_b = V_{Coulomb} \propto \frac{1}{r} + V_{nuclear} + V_{rotational}$$

$$V_{Coulomb} = \frac{Z_p Z_t e^2}{R_b} \propto \frac{1}{r}$$

$V_{nuclear} \rightarrow$  constant, attractive  
and shortrange  $\rightarrow$  rectangular

# The Nuclear Potential



$$V_b = V_{Coulomb} \propto \frac{1}{r} + V_{nuclear} + V_{rotational}$$

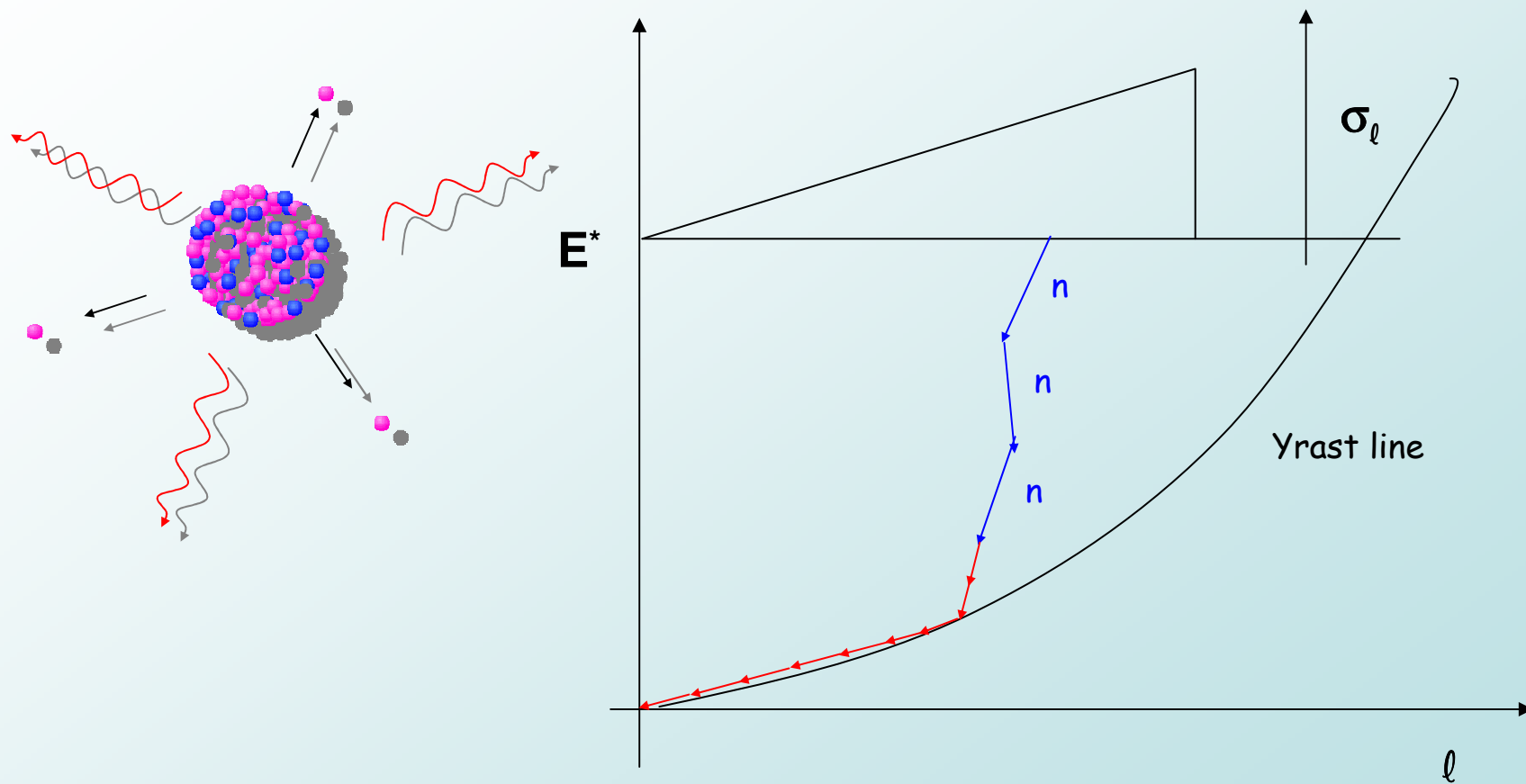
$$V_{Coulomb} = \frac{Z_p Z_t e^2}{R_b} \propto \frac{1}{r}$$

$V_{nuclear} \rightarrow$  constant, attractive  
and shortrange  $\rightarrow$  rectangular

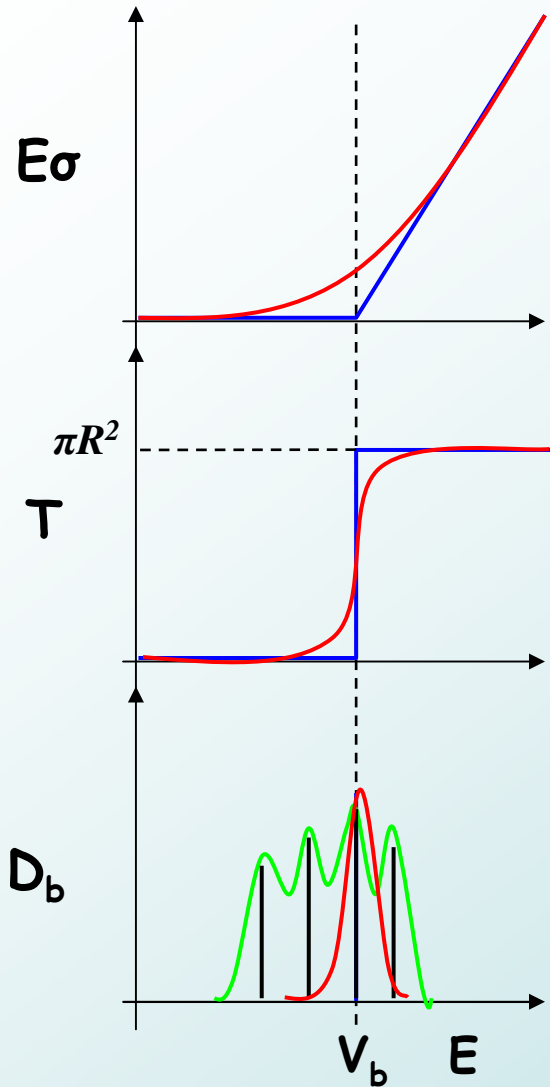


# The Statistical Model

## - de-excitation of the Hot Compound System



# Fusion Barrier Distribution - the Concept



$$\sigma E(E, V_b) = \pi R^2 \left( 1 - \frac{V_b}{E} \right) \quad , E > V_b$$

$$\sigma E(E, V_b) = 0 \quad , E < V_b$$

$$\frac{d(E\sigma(E, V_b))}{dE} = \pi R^2 \quad , E > V_b$$

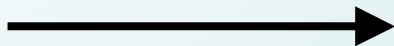
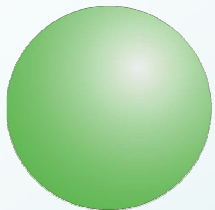
$$\frac{d(E\sigma(E, V_b))}{dE} = 0 \quad , E < V_b$$

$$\frac{d^2(E\sigma(E, V_b))}{dE^2} = \pi R^2 \delta(E - V_b)$$

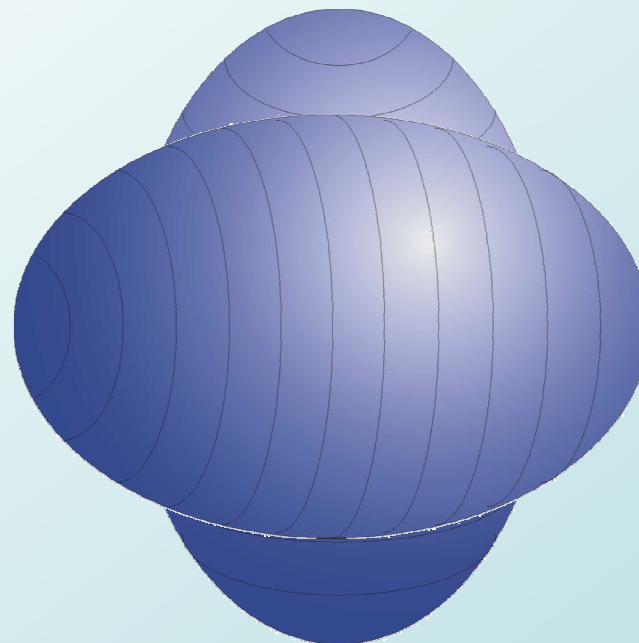


# Fusion Barrier Distribution - Deformed Nuclei

Projectile

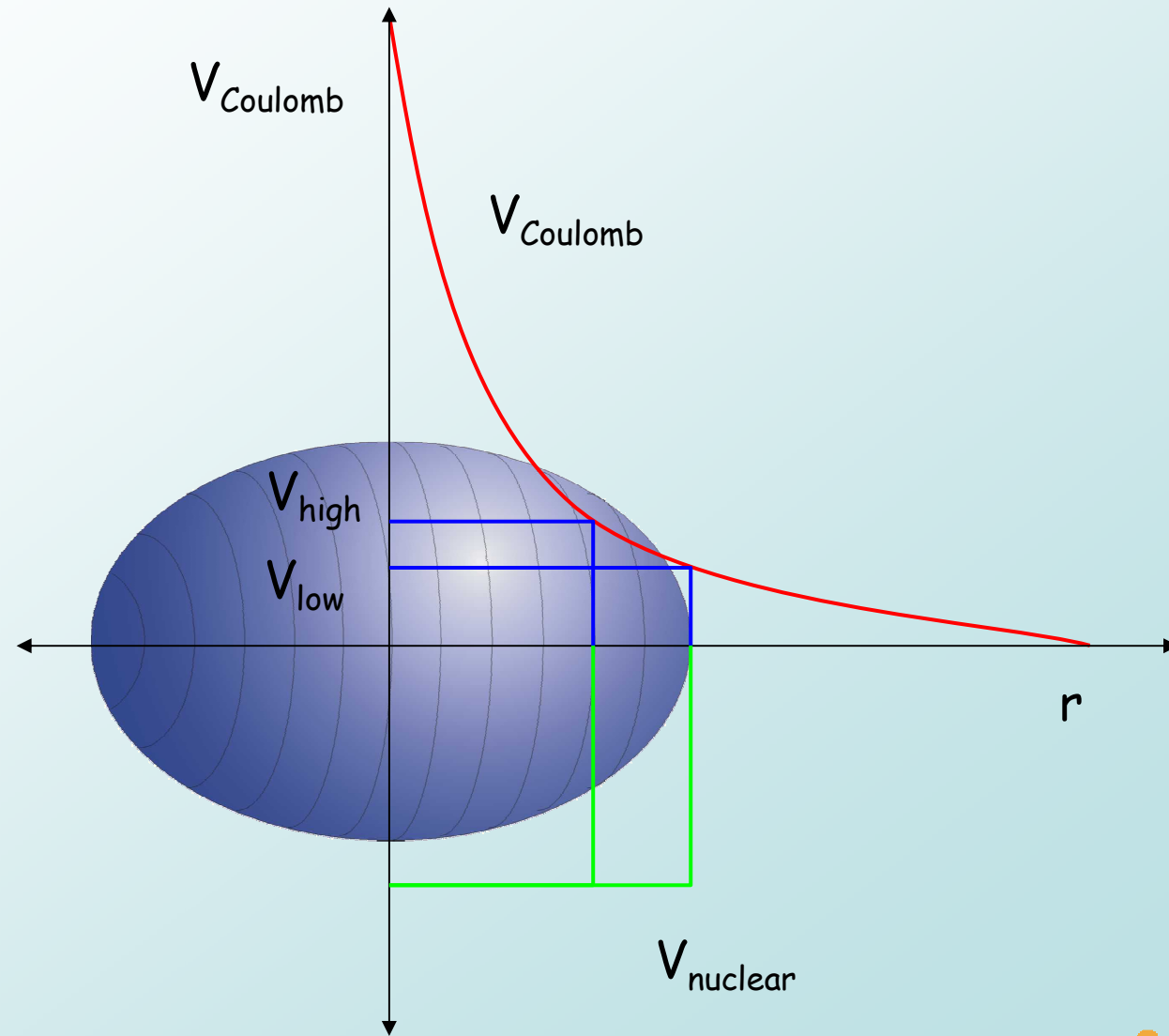


deformed target



# Fusion Barrier Distribution

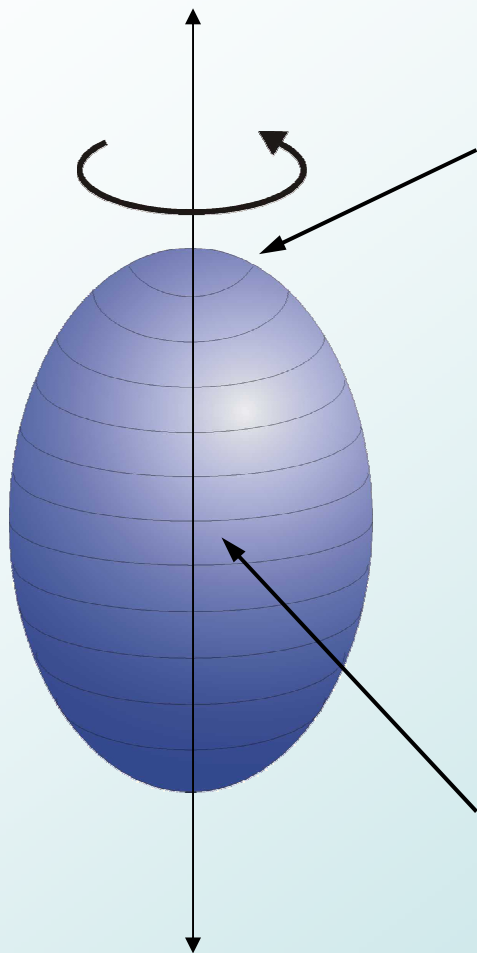
## - Deformed Nuclei and the Potential



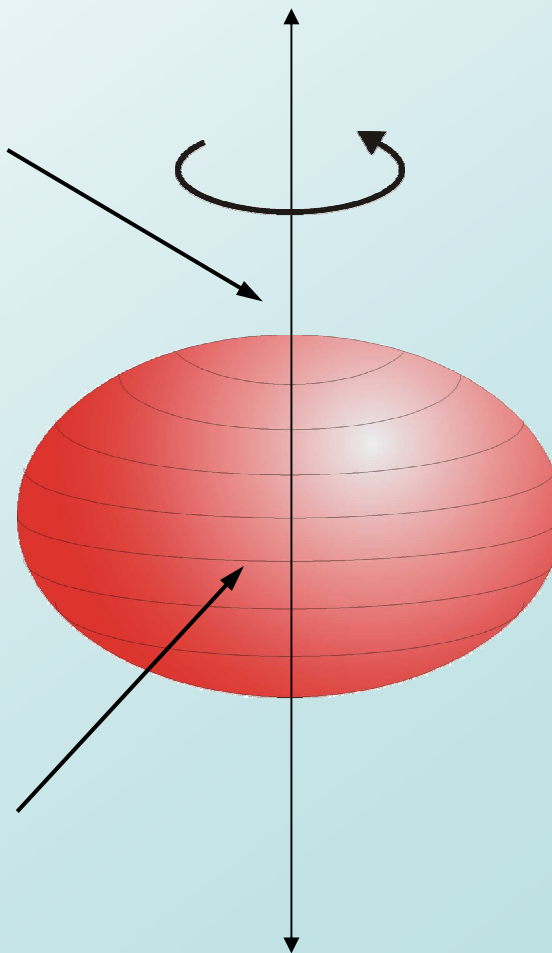
# Fusion Barrier Distribution

## - Deformed Nuclei: prolate and oblate

prolate



oblate

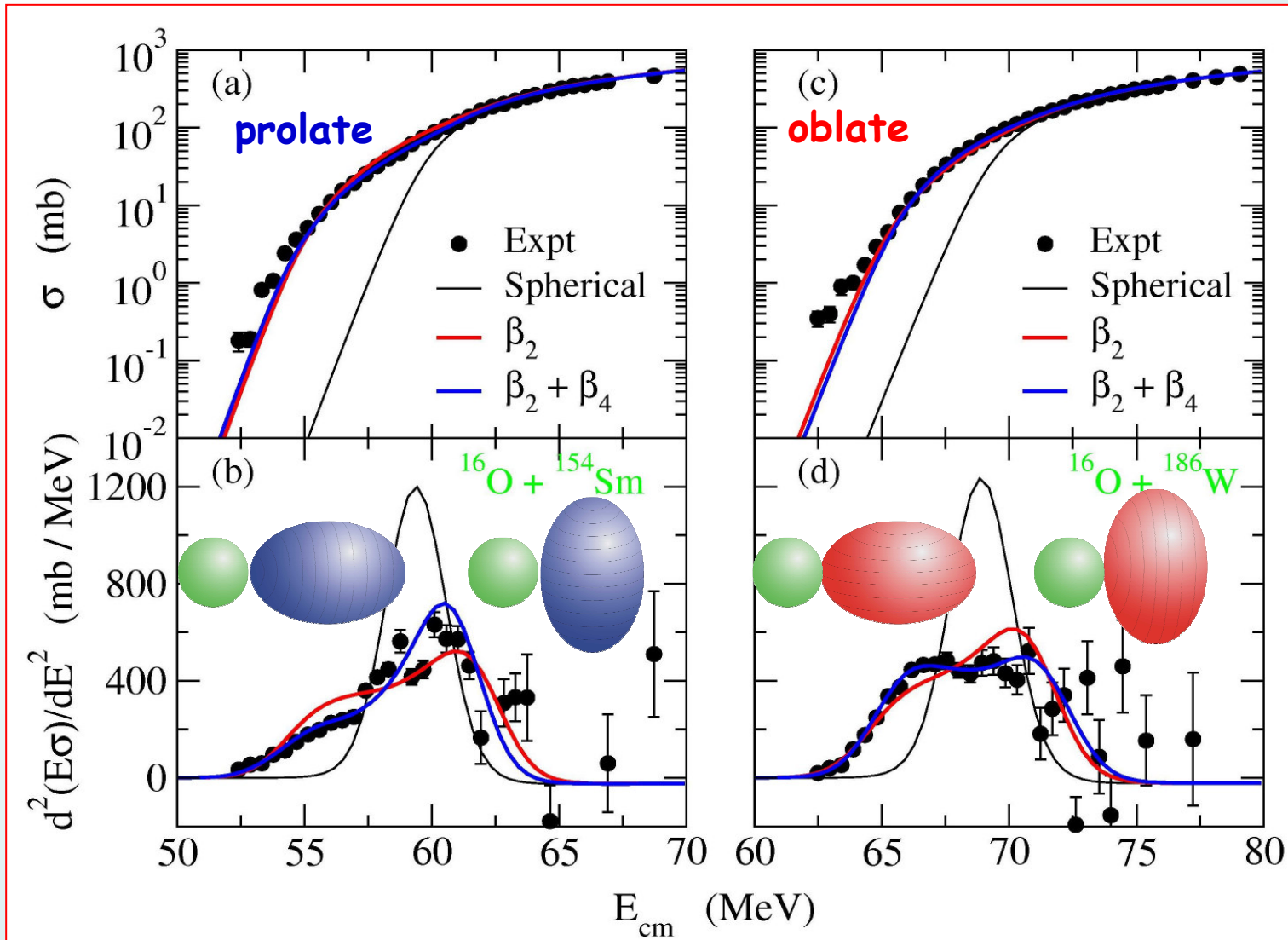


small geometric cross section at the poles

large geometric cross section at the waist

# Fusion Barrier Distribution

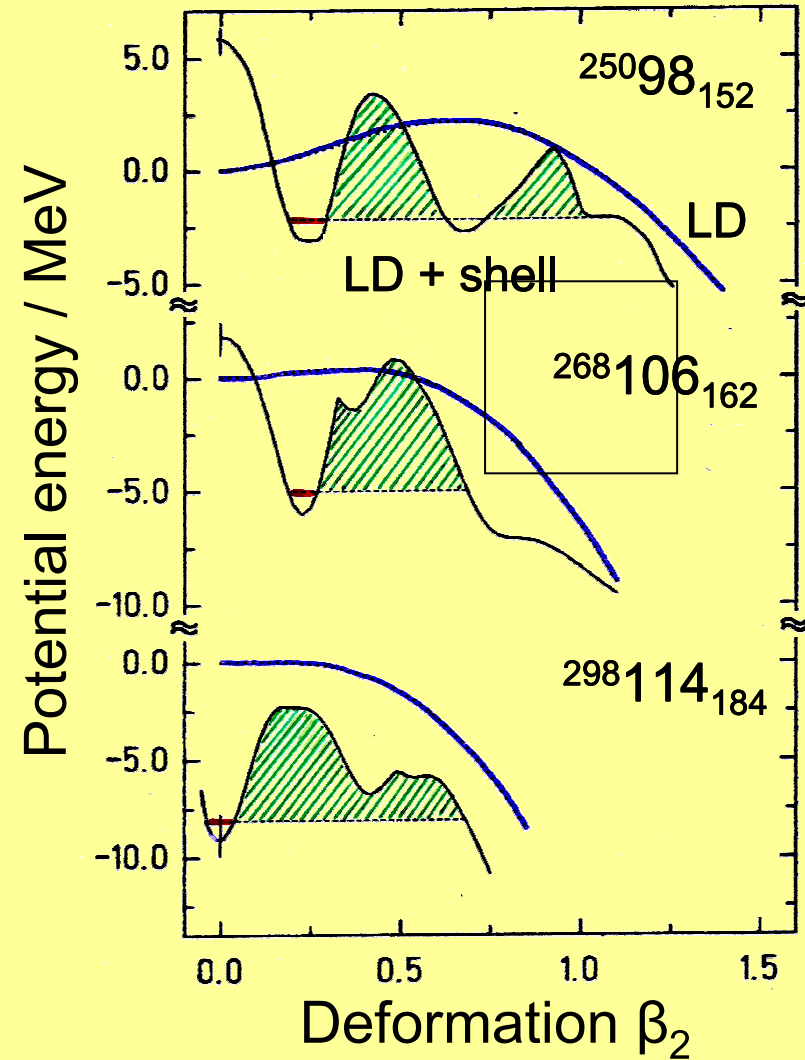
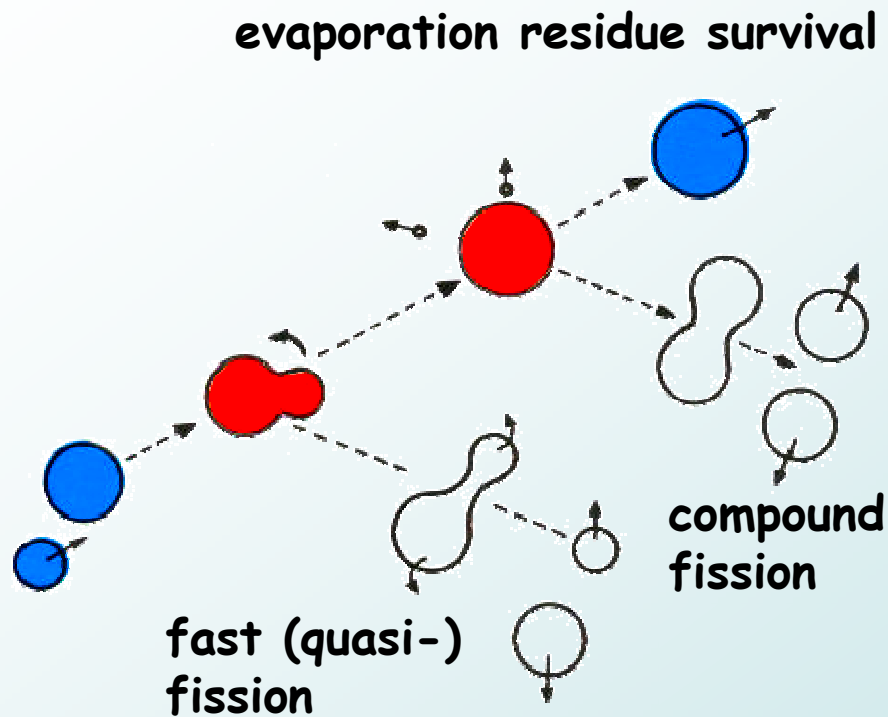
## - Deformed Nuclei: prolate and oblate





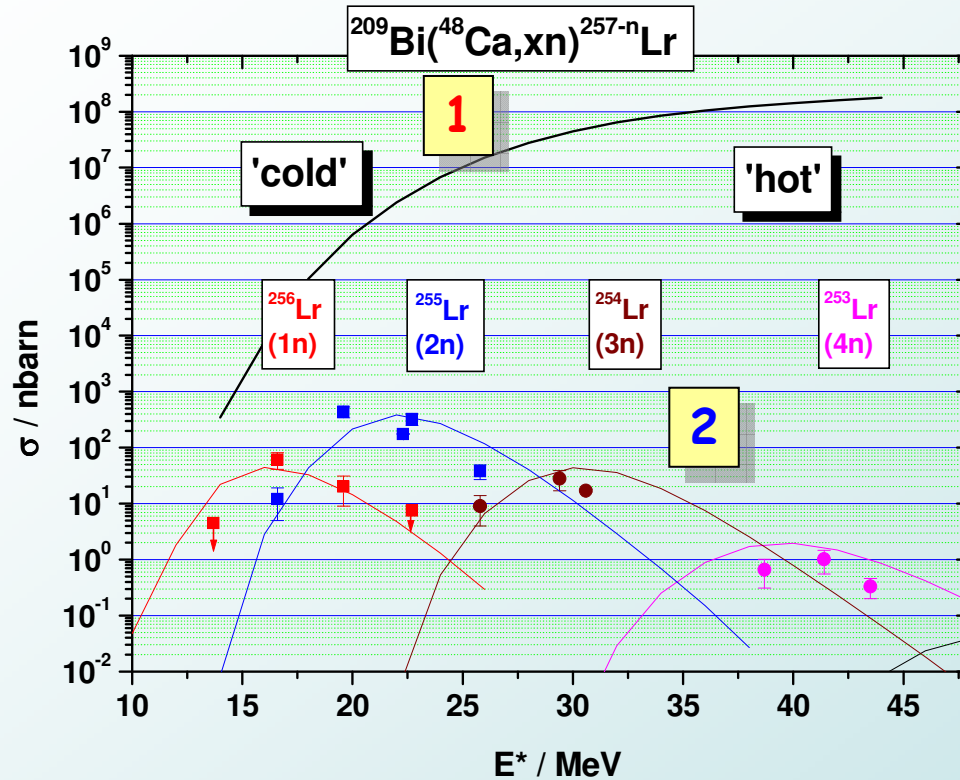
# Fusion/Fission Competition for SHE

## - Liquid Drop + Shell Corrections



*A. Sobiczewski et al.*

# The 2-step process Fusion - Evaporation



F.P. Heßberger 2.5.2005

1. *CN formation*

- *entrance channel properties (nuclear structure, deformation...)*

2. *ER formation*

- *survival*
- *fission competition*

probes:

- *Fusion-fission excitation function (fission and ER-production)*
- *l-distribution*

...



# Synthesis and Investigation of SHE

## Outline

1. Introduction
2. Reaction Mechanism of Heavy Ion Collisions at the Coulomb Barrier
- 3. Synthesis and Investigation of Superheavy Nuclei**
  - Predictions of the next closed p and n shells
  - Separation and identification
  - "cold" and "hot" fusion
4. Nuclear Structure of Heavy and Superheavy Nuclei
5. Additional Methods



# Theoretical Models I

## - Microscopic-Macroscopic Model

The nucleus is treated as a classical liquid drop (macroscopic part) with quantum mechanical corrections (microscopic part):

$$E_{bind}(Z, N) = E_{macro}(Z, N) + E_{micro}(Z, N)$$

Macroscopic part (Bethe-Weizsäcker formula, 1935):

$$E_{macro}(Z, N) = a_c \frac{Z^2}{A^{\frac{1}{3}}} + a_I \frac{(N-Z)^2}{A} + a_V A + a_S A^{\frac{2}{3}}$$

Terms:      Coulomb      Asymmetry      Volume      Surface

deformation dependent

Microscopic part :

$$E_{micro}(Z, N) = E_{shell} + E_{pairing}$$



# Theoretical Models IIa

## - Self-consistent Models: Hartree Fock Bogoliubov

Schrödinger equation for the nuclear many body system:

$$H\Psi = E_0\Psi$$

$H$ : the nuclear Hamiltonian  
 $E_0$ : the total binding energy  
 $\Psi$ : fully antisymmetric wave function

$$H = \sum T + \sum V(i, j)$$

$V(i,j)$ : nucleon-nucleon interaction  
(Gogny force, Skyrme force, ...)

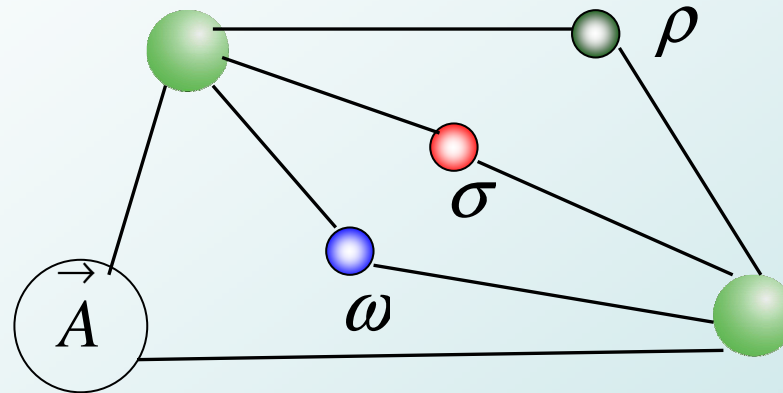




# Theoretical Models IIb

## - Self-consistent Models: Relativistic Mean Field

The nucleon-nucleon interaction is mediated by mesons



$L(\text{nucleon}, \rho, \sigma, \vec{\omega}, A)$  (Lagrangian density)

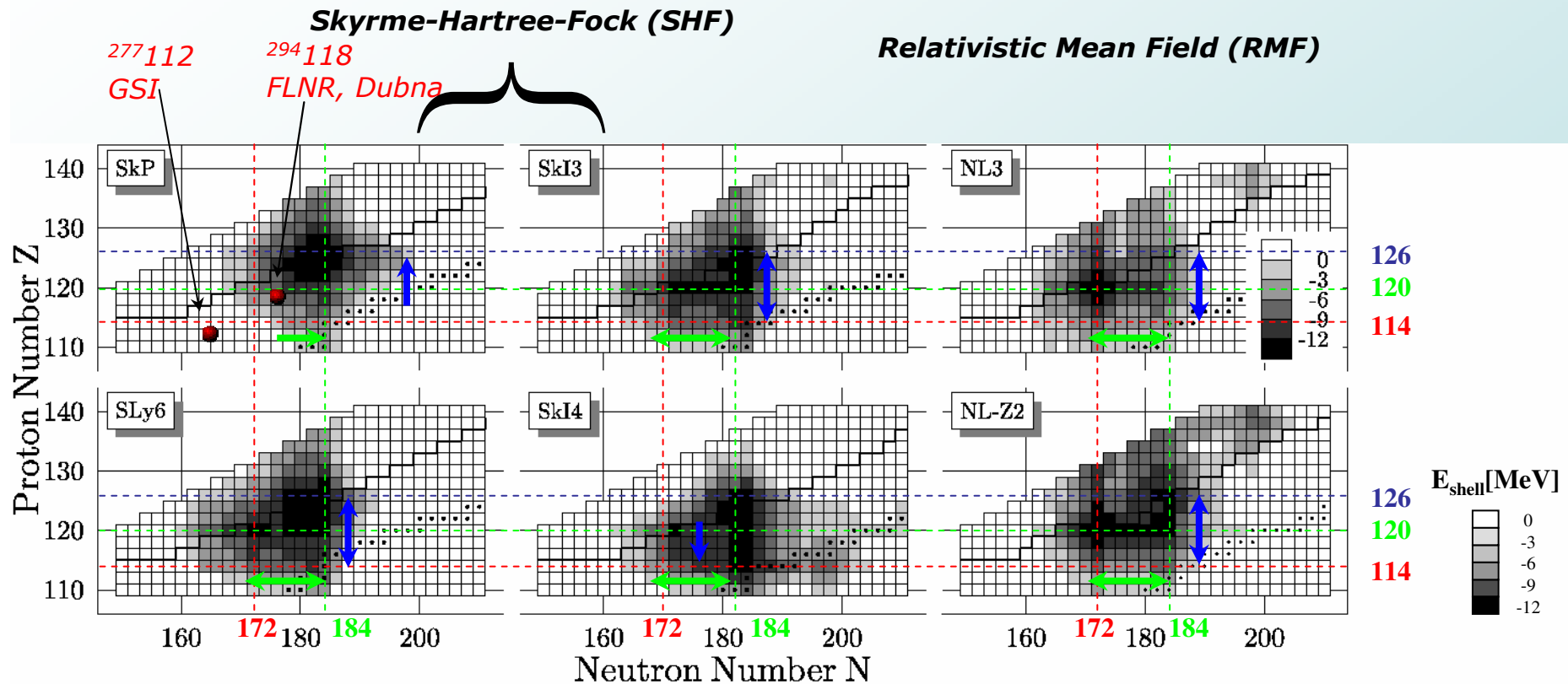
→ Dirac equation + Klein-Gordon equations (for mesons and photons)

Method: solve the system of coupled Dirac equations for the nucleons and Klein-Gordon equations for mesons and photons to obtain the ground state energy of the nucleus and its wave function.  
The pairing energy should be added



# Selbstkonsistente Rechnungen: Stabilitätsbereiche

- M. Bender, W. Nazarewicz, P.-G. Reinhard et al.



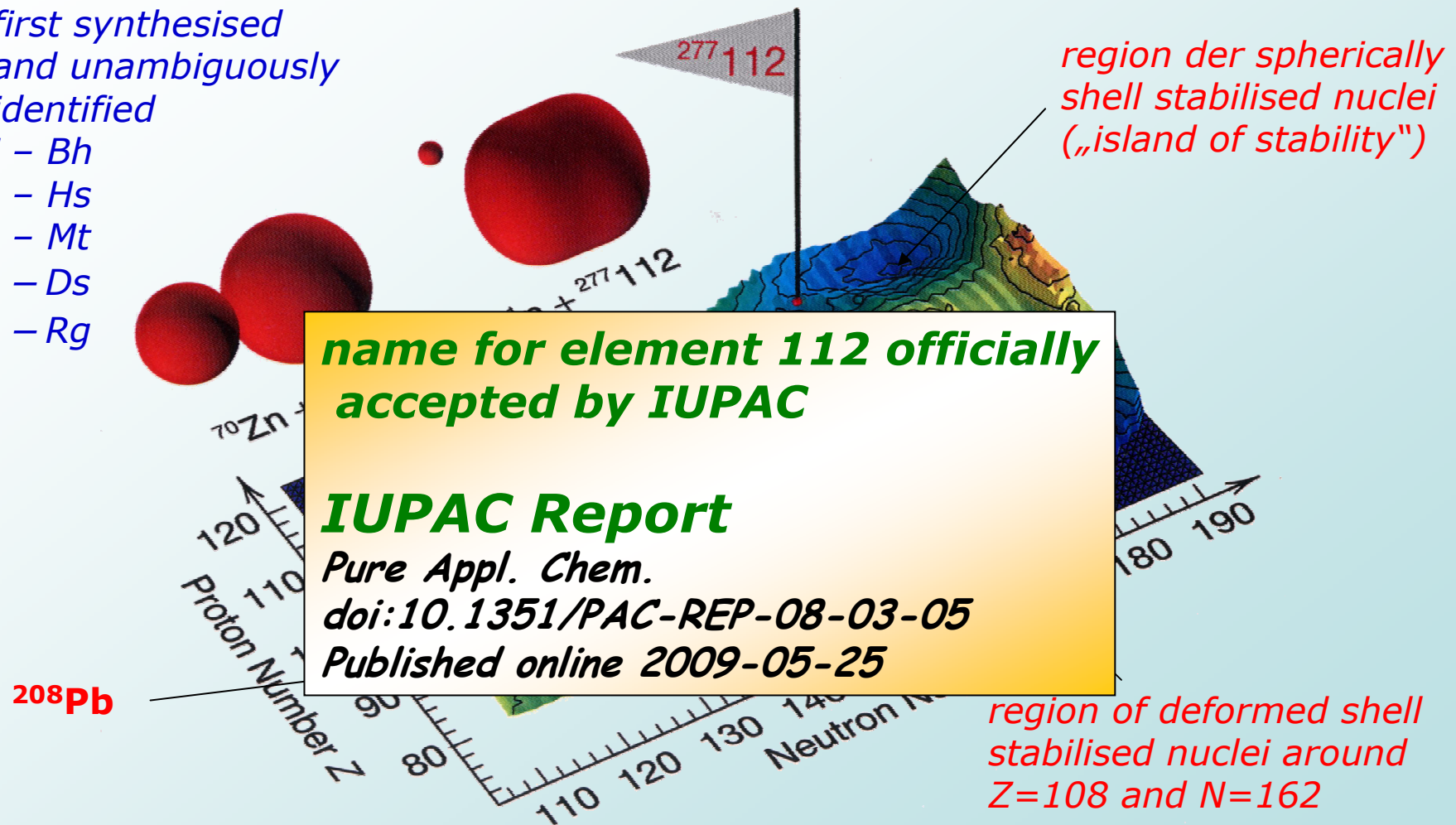
# Shell Correction Energies $E_{shell}$ in the Region of Superheavy Elements

- P. Möller et al.: microscopic-macroscopic model

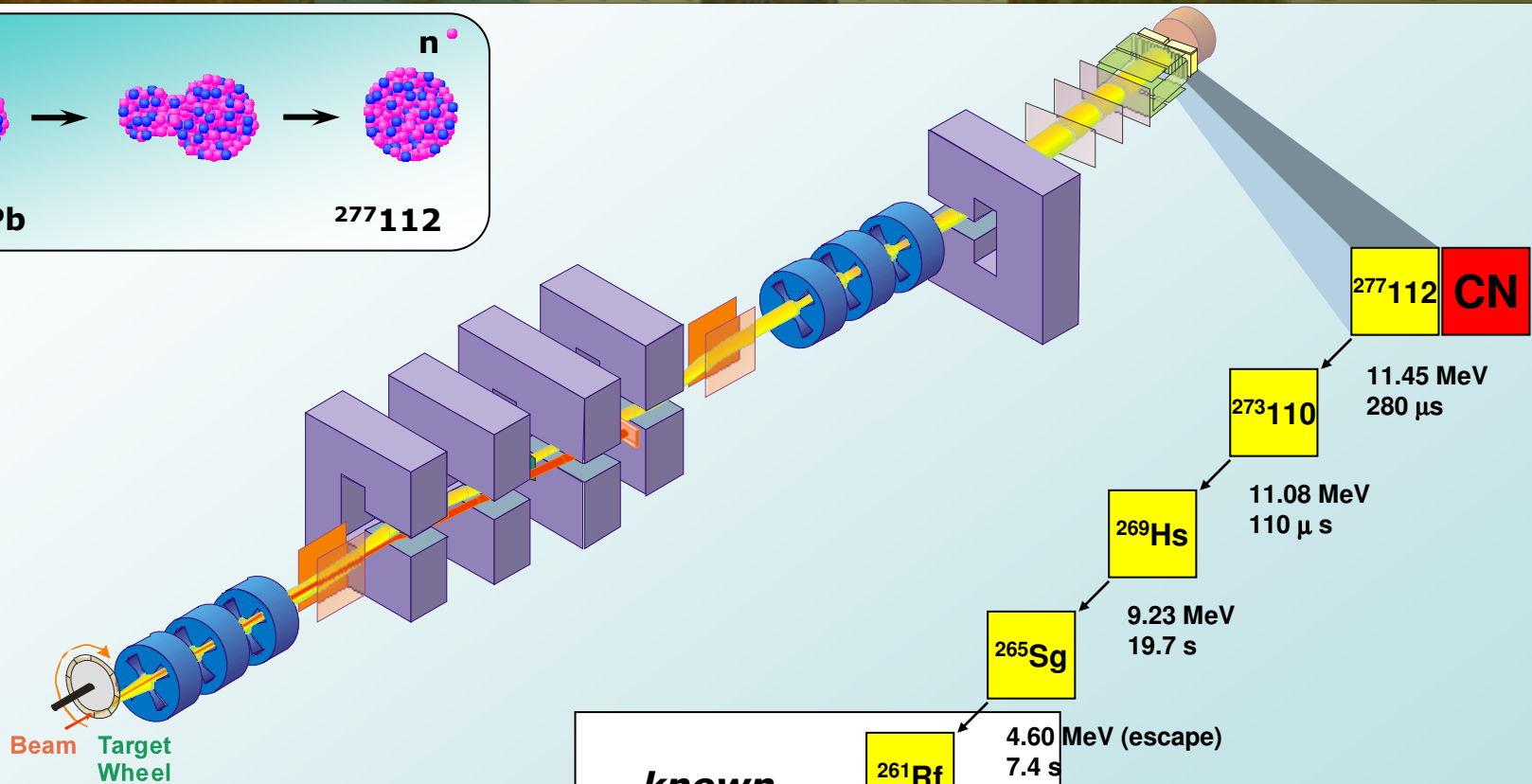
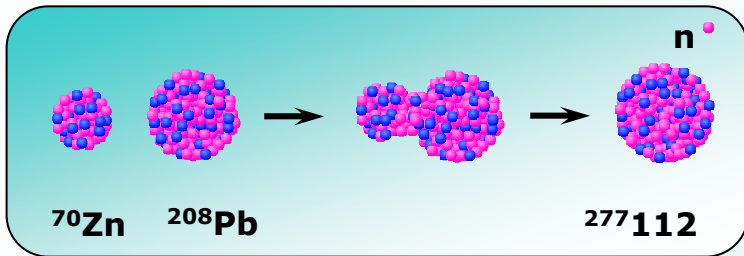
**at GSI:** Elements 107-112

first synthesised  
and unambiguously  
identified

- 107 – Bh
- 108 – Hs
- 109 – Mt
- 110 – Ds
- 111 – Rg

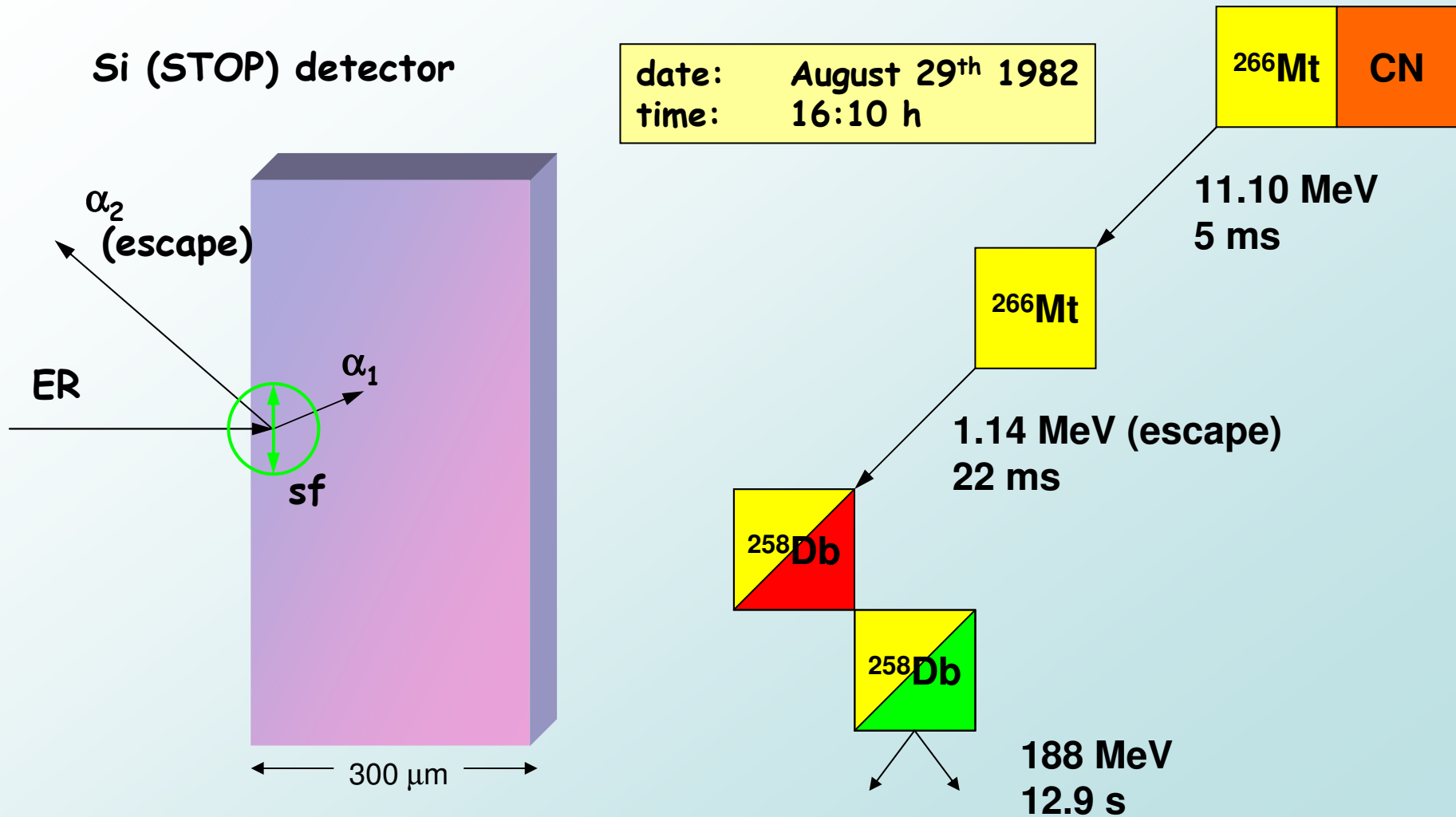


# Synthesis and Identification of SHE at SHIP



# ER- $\alpha$ Correlation method

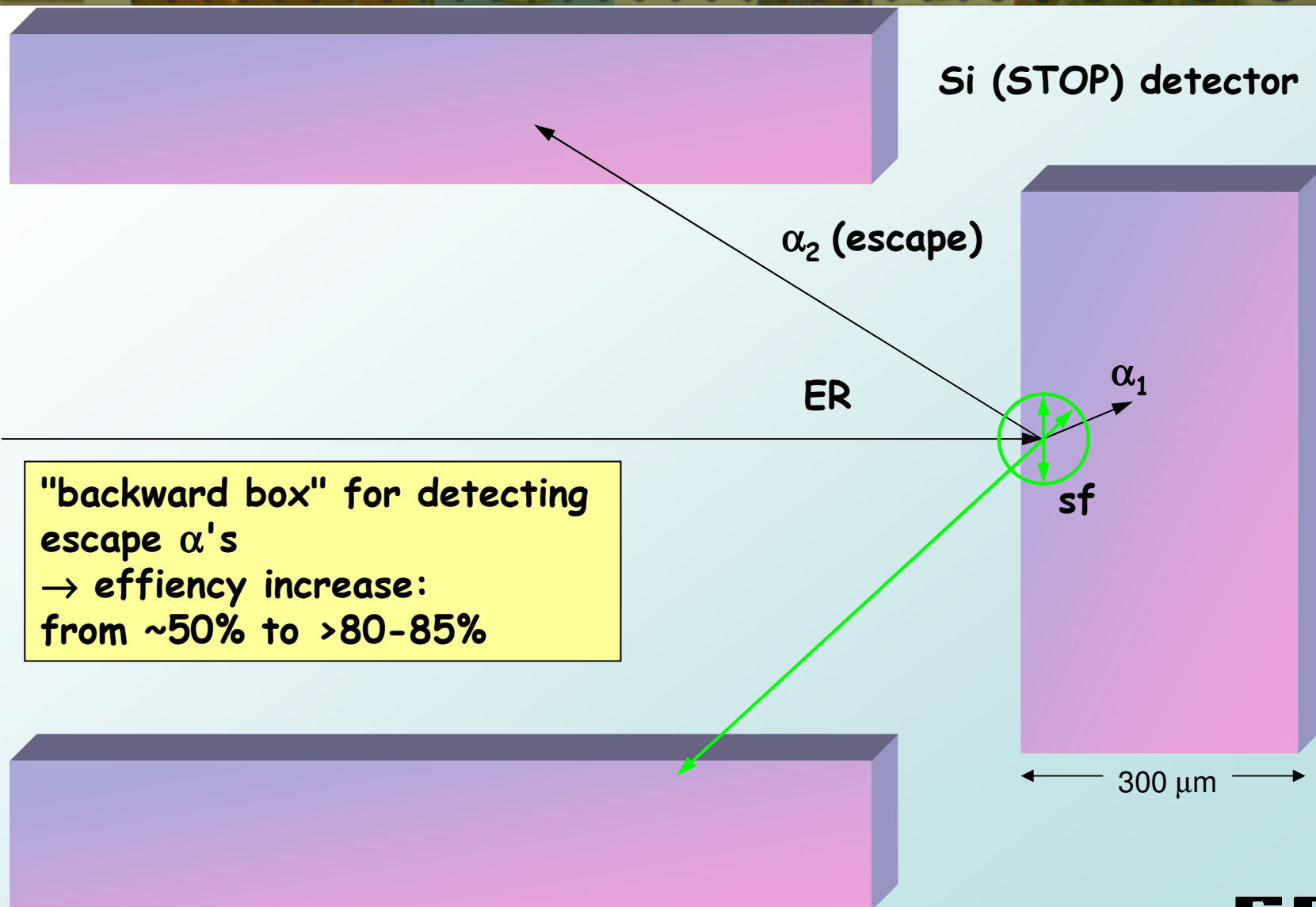
- Example:  $^{58}\text{Fe} + ^{209}\text{Bi} \rightarrow ^{266}\text{Mt} + 1n$





# Revelation of escape $\alpha$ 's

## - "Backward Box" SI detector array



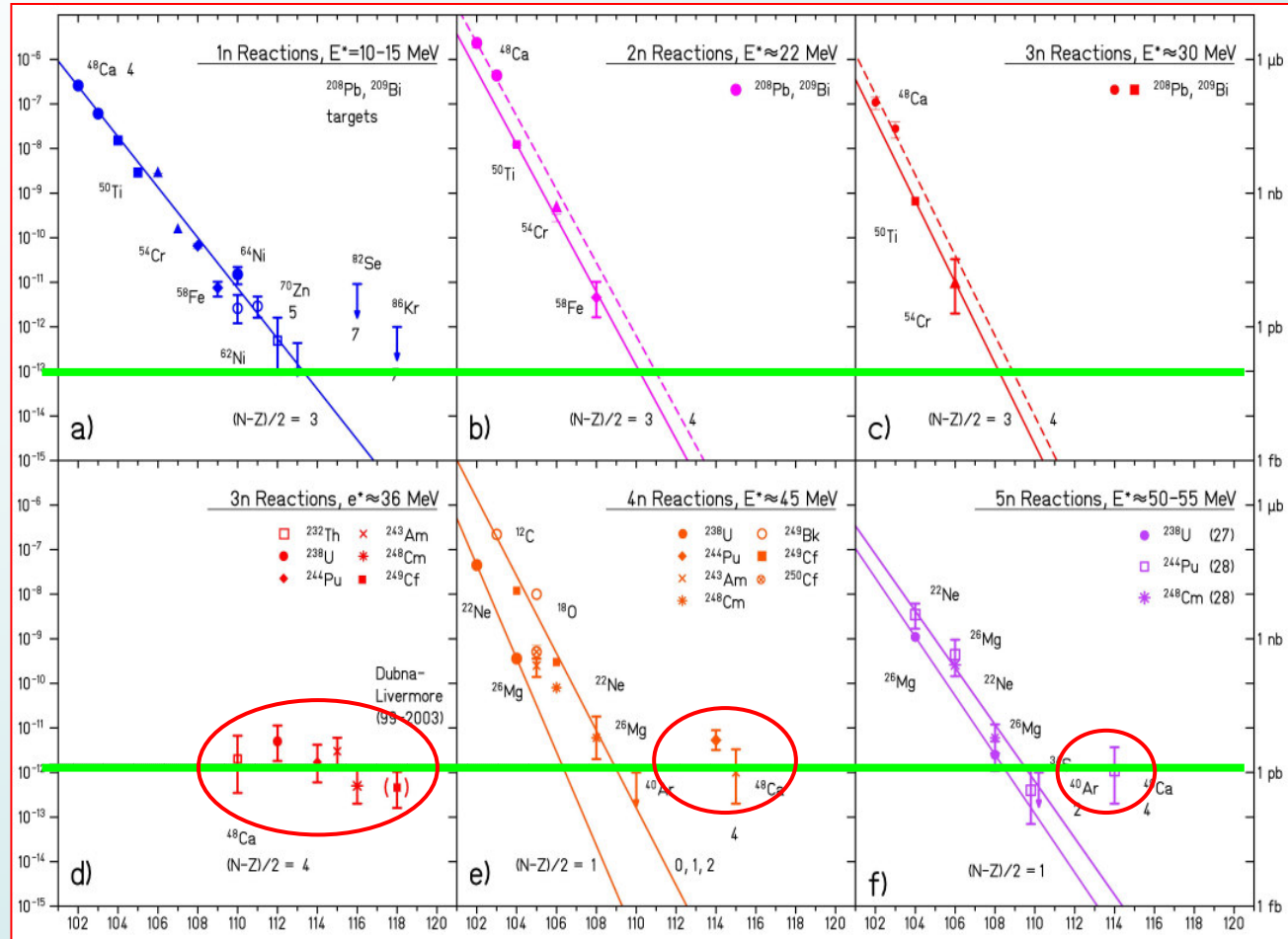
# Cross Section Systematics

**Cold fusion (GSI)**  
 → based on  
 Pb and Bi targets

1 pb

**Hot fusion (JINR)**  
 → based on  
 actinide targets

1 pb



**Surprising high cross-sections (0.5 - 5 pb) for synthesis of spherical SHE**



# Nuclear Structure of Actinoides, Transactinoides and SHE

## Outline

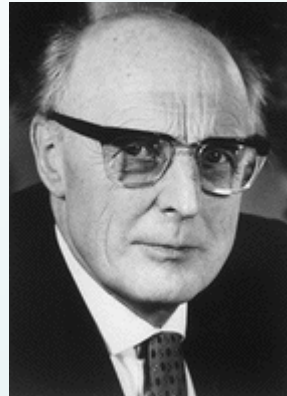
1. Introduction
2. Reaction Mechanism of Heavy Ion Collisions at the Coulomb Barrier
3. Synthesis and Investigation of Superheavy Nuclei
4. Nuclear Structure of Heavy and Superheavy Nuclei
  - The shell model - Maria Goeppert Mayer
  - Single particle levels and deformation
  - Decay spectroscopy - ER- $\alpha$ - $\gamma$ (- $\gamma$ ) correlations
  - Isomeric states
  - Nuclear structure in the vicinity of closed shells
5. Additional Methods





# The Shellmodel

- Maria Goeppert-Mayer and J. Hans D. Jensen



The Shell model:  
Harmonic oscillator and spin orbit coupling → shell structure of single particle levels (Maria Goeppert Mayer and J. Hans D. Jensen)

Table 1 -- Nuclear Shell Structure (from *Elementary Theory of Nuclear Shell Structure*, Maria Goeppert Mayer & J. Hans D. Jensen, John Wiley & Sons, Inc., New York, 1955.)

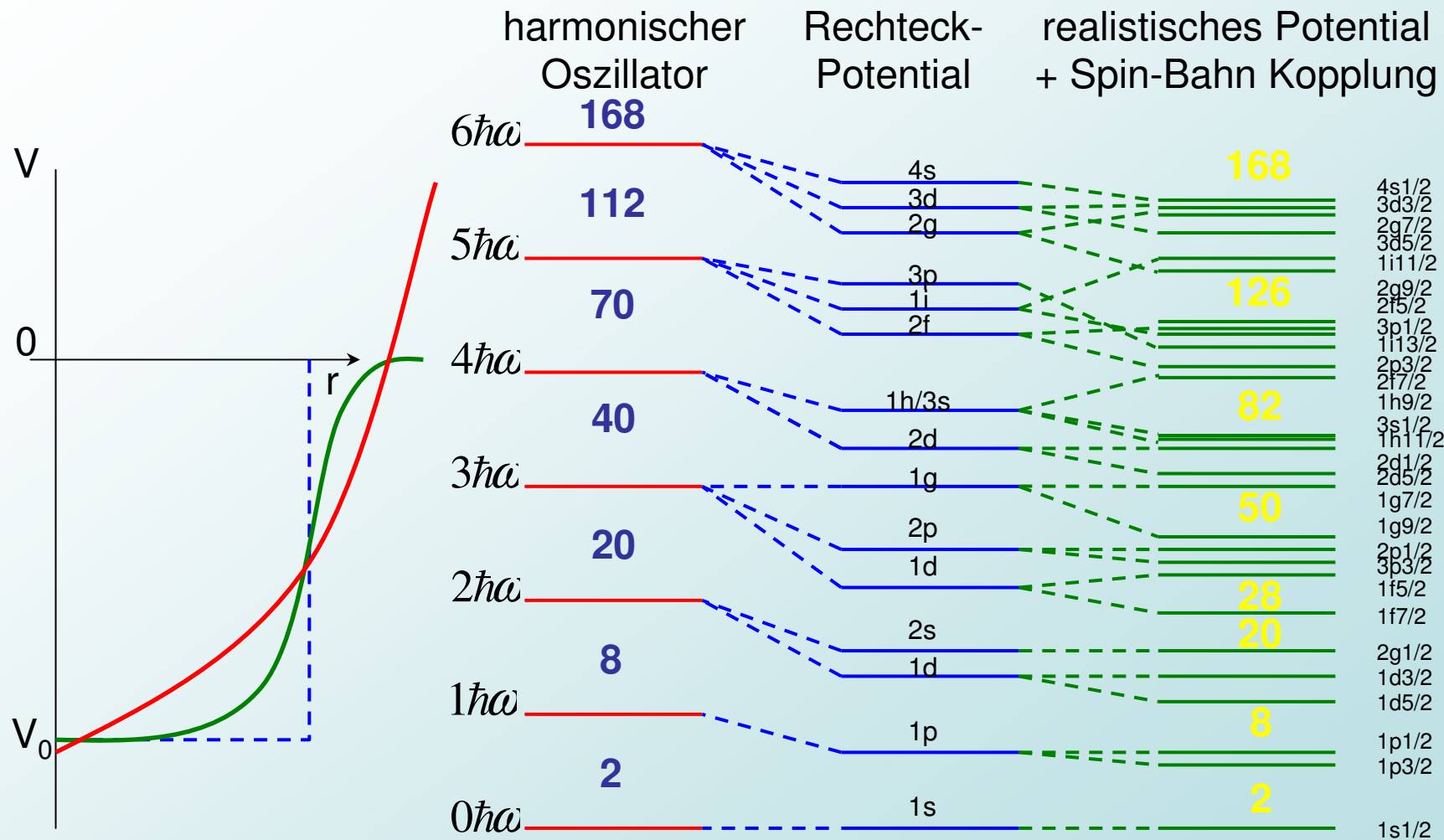
Angular Momentum ( $\hbar\Omega/2\pi$ )	Spin-Orbit Coupling ( $1/2, 3/2, 5/2, 7/2, \dots$ )	Number of Nucleons Shell	Magic Number Total	Magic Number	
7	1j	-1j 15/2	16	[184]	{184}
		3d 3/2	4	[168]	
6	4s	4s 1/2	2	[164]	
6	3d	-2g 7/2	8	[162]	
		-1i 11/2	12	[154]	
6	2g	3d 5/2	6	[142]	
		2g 9/2	10	[136]	
6	1i	-1i 13/2	14	[126]	{126}
		-3p 1/2	2	[112]	
5	3p	3p 3/2	4	[110]	
		-2f 5/2	6	[106]	
5	2f	2f 7/2	8	[100]	
		-1h 9/2	10	[92]	
5	1h	-1h 11/2	12	[82]	{82}
4	3s	3s 1/2	2	[70]	
		-2d 3/2	4	[68]	
4	2d	2d 5/2	6	[64]	
		1g 7/2	8	[58]	
4	1g	-1g 9/2	10	[50]	{50}
		-2p 1/2	2	[40]	{40}
3	2p	-1f 5/2	6	[38]	
		-2p 3/2	4	[32]	
3	1f	-1f 7/2	8	[28]	{28}
		-1d 3/2	4	[20]	{20}
2	2s	-2s 1/2	2	[16]	
2	1d	1d 5/2	6	[14]	
		1p 1/2	2	[8]	{8}
1	1p	1p 3/2	4	[6]	
0	1s	1s 1/2	2	[2]	{2}





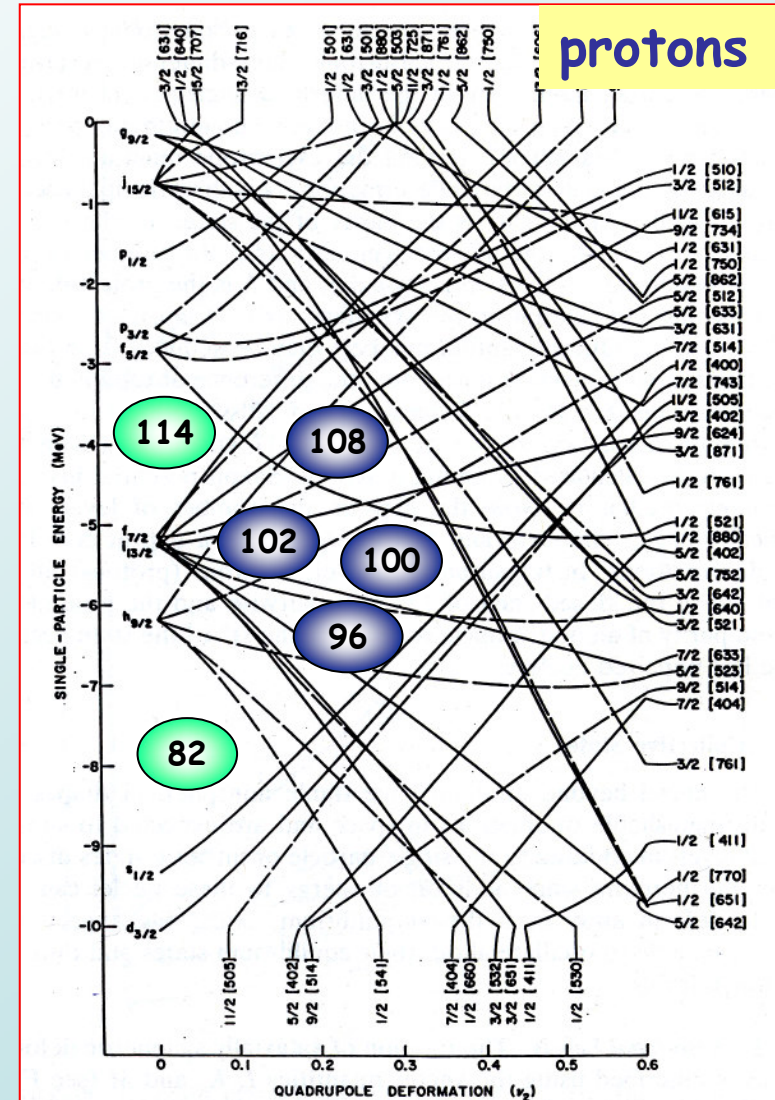
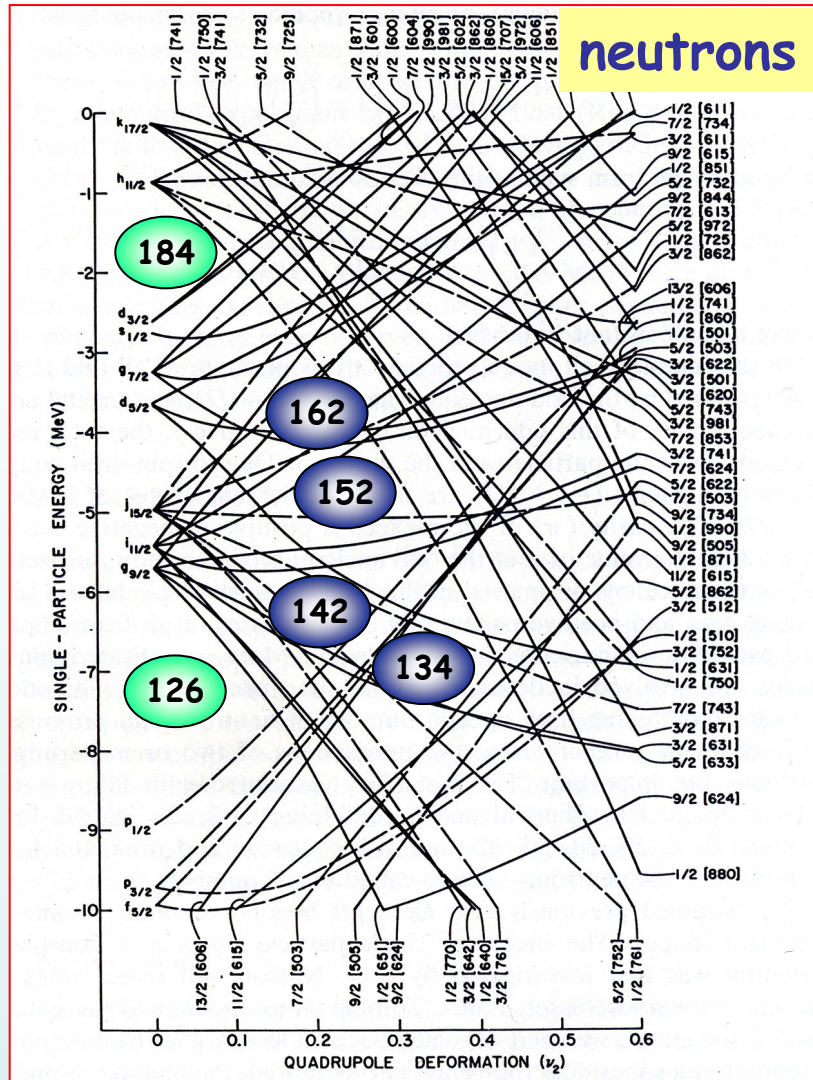
# The Shell Model

- Maria Goeppert-Mayer and J. Hans D. Jensen



# Nuclear Structure of Heavy Nuclei

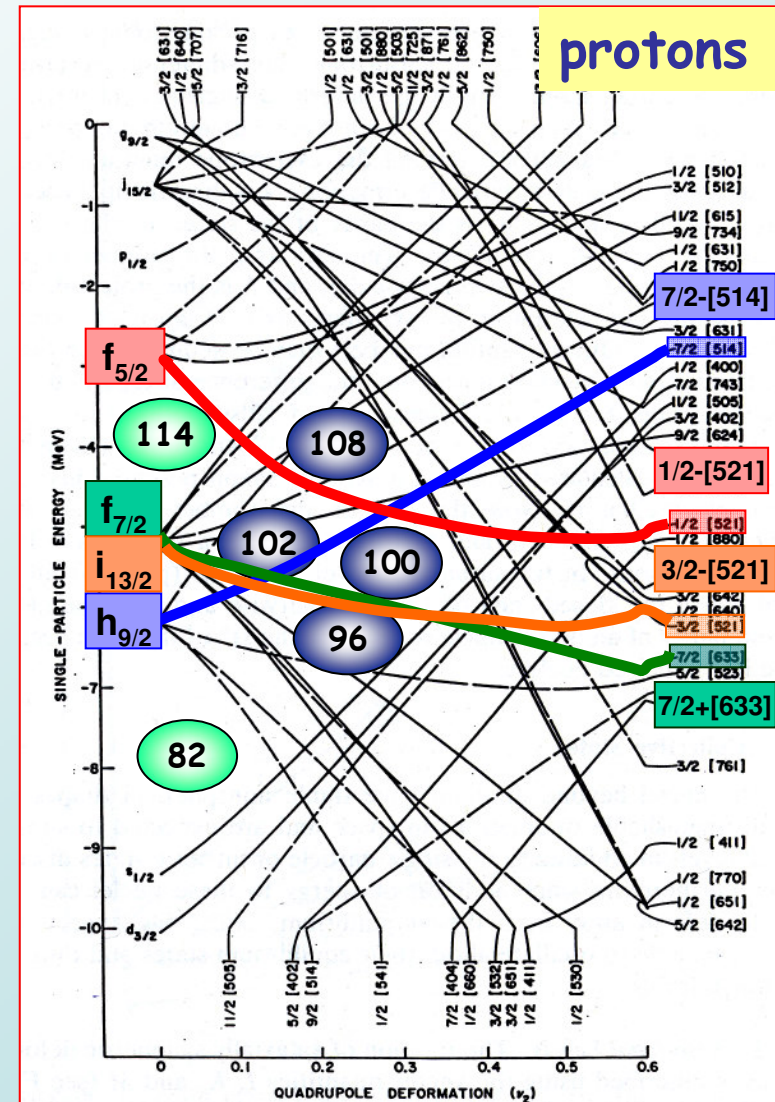
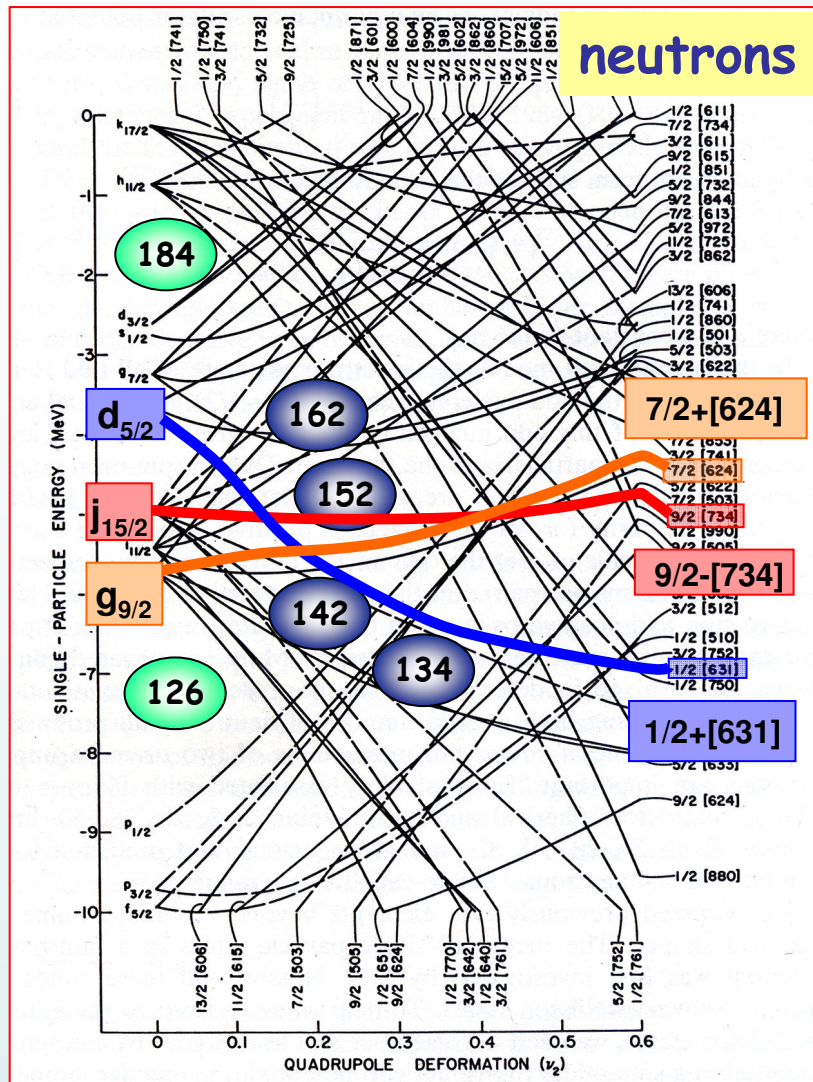
## - Single Particle Levels and Deformation





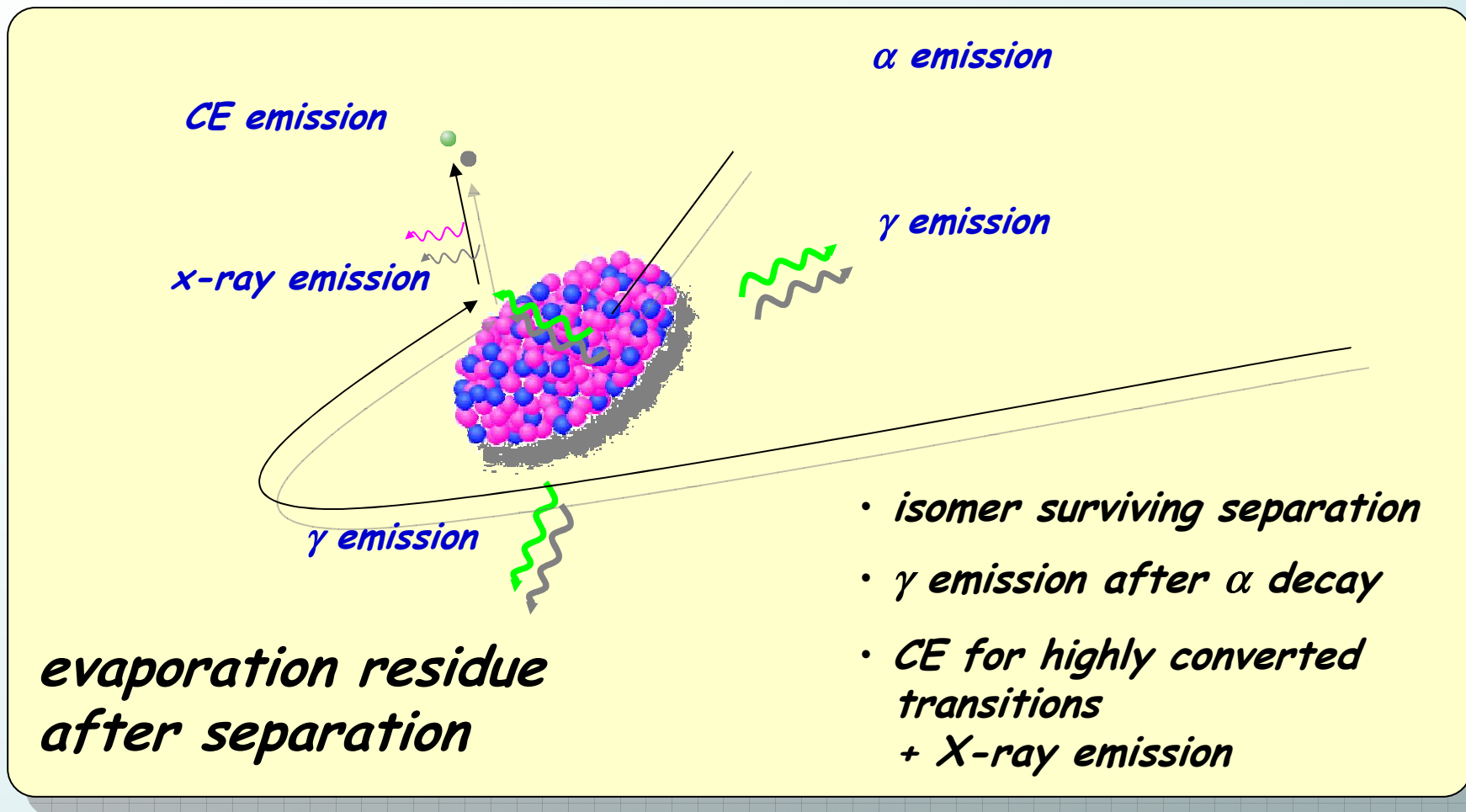
# Nuclear Structure of Heavy Nuclei

## - Single Particle Levels and Deformation



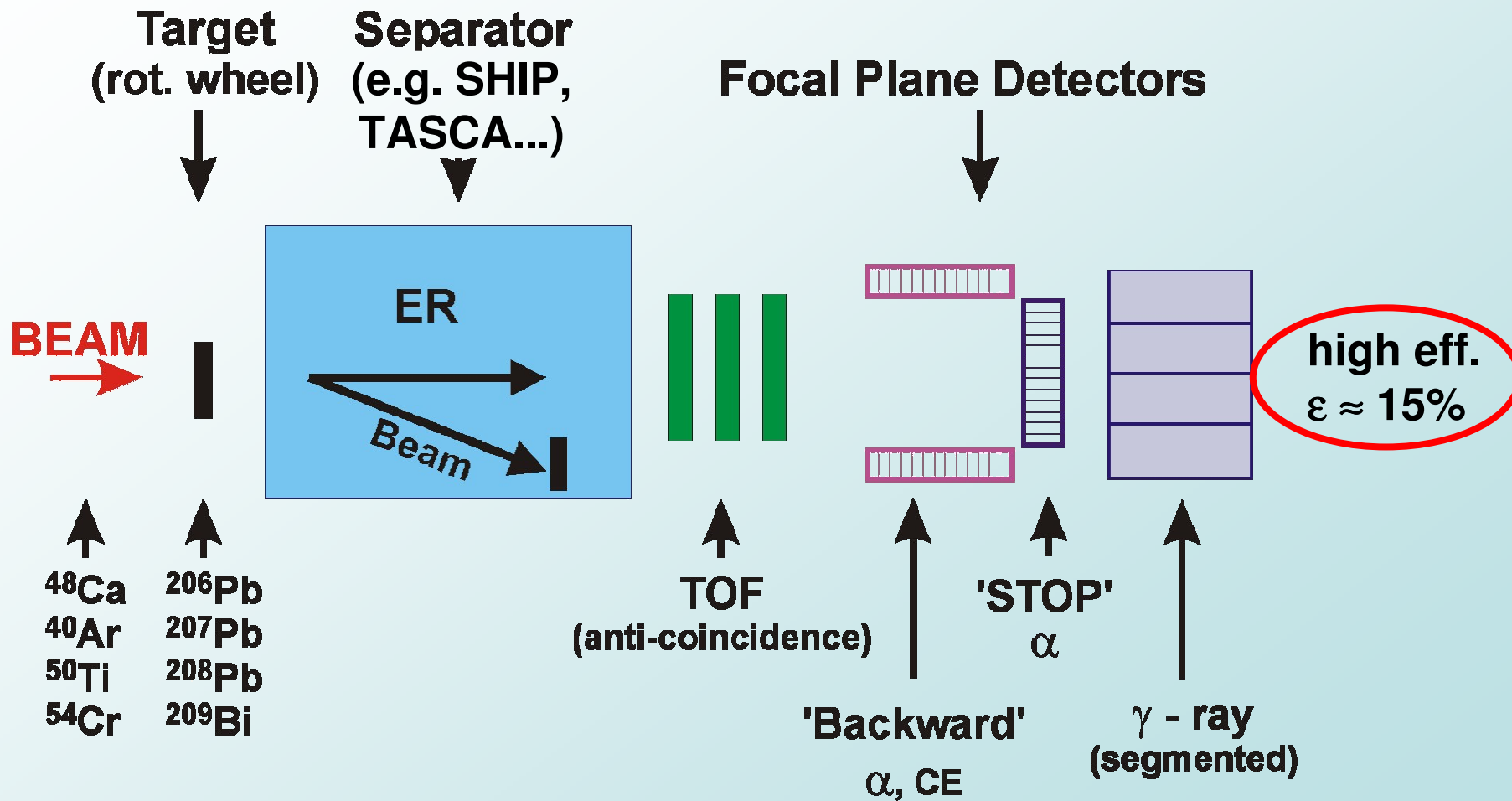
# Nuclear Structure of SHE

## - Decay Spectroscopy at SHIP/TASCA



# Nuclear Structure of SHE

## - Decay Spectroscopy at SHIP/TASCA



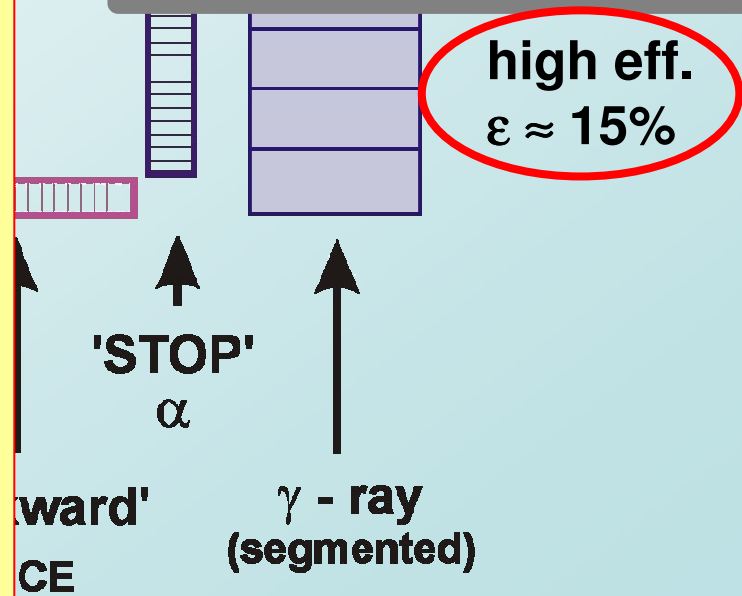
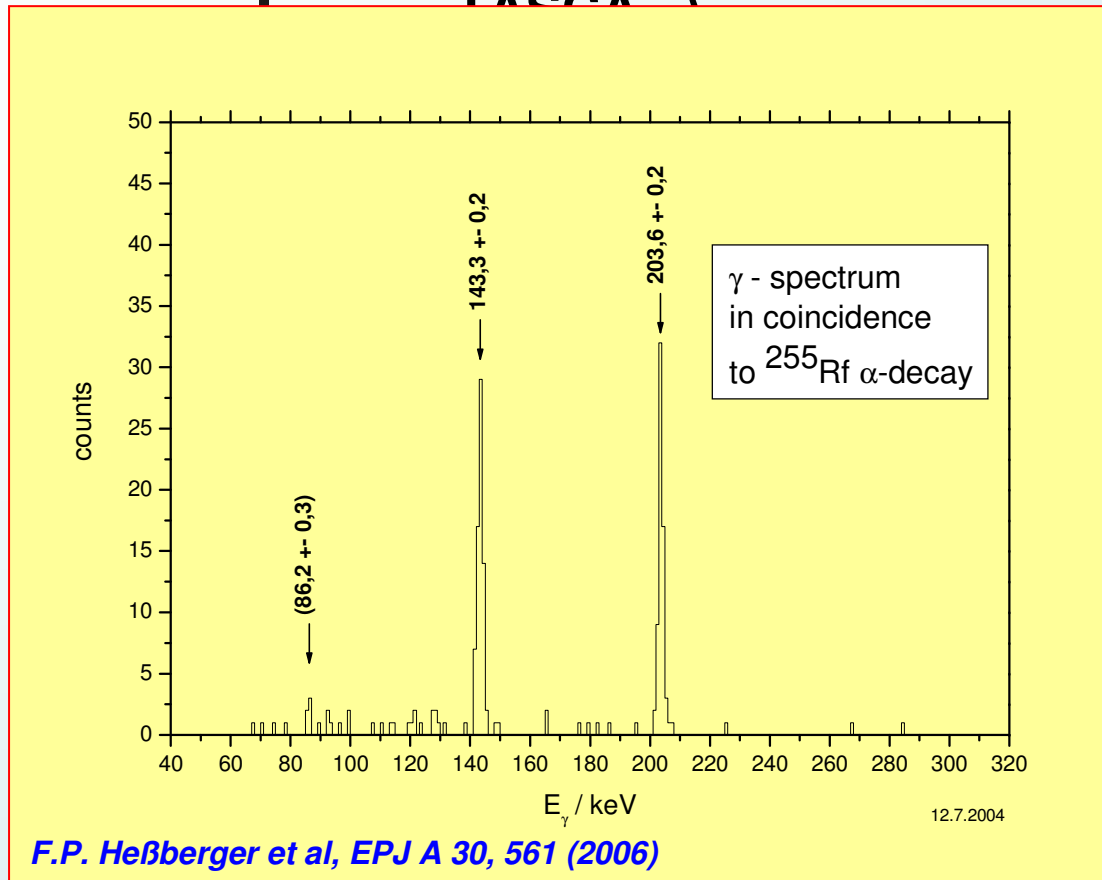


# Nuclear Structure of SHE

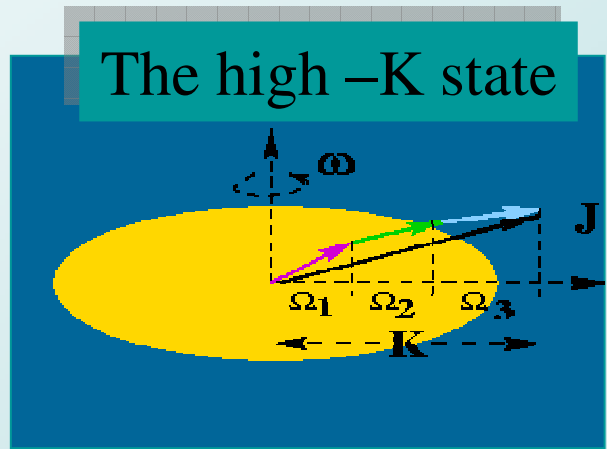
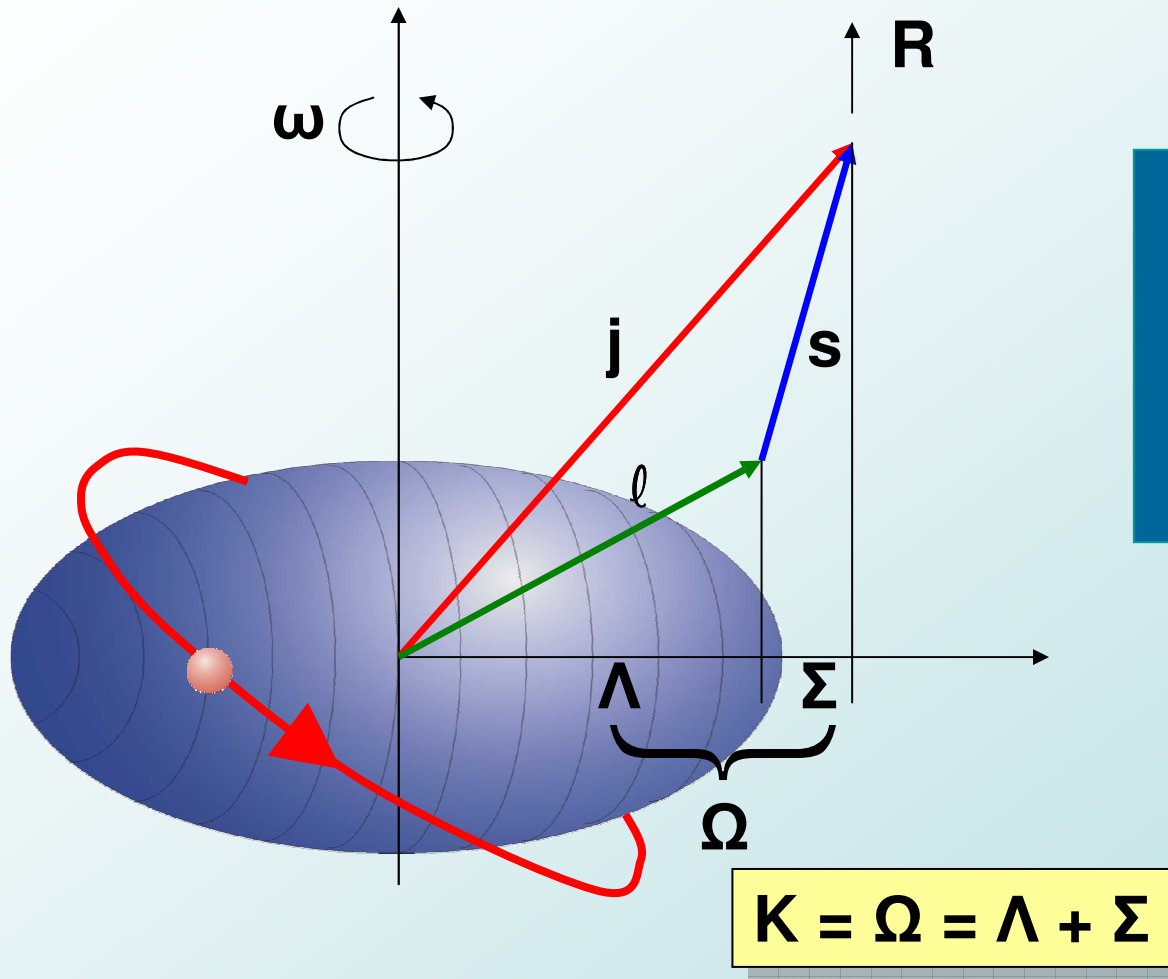
## - Decay Spectroscopy at SHIP/TASCA

Target (rot. wheel) Separator (e.g. SHIP, TASCA) Focal Plane

- **inclusive measurement**
  - ER,  $\alpha$ 's,  $\gamma$ 's and  $e^-$
- **clean**
  - particle discrimination
  - ER- $\alpha$ - $\gamma$  correlations
- **highly efficient**
  - close geometry
  - stopped source



# K-Quantum number - the Definition



# K-isomers for Z = 96 - 110

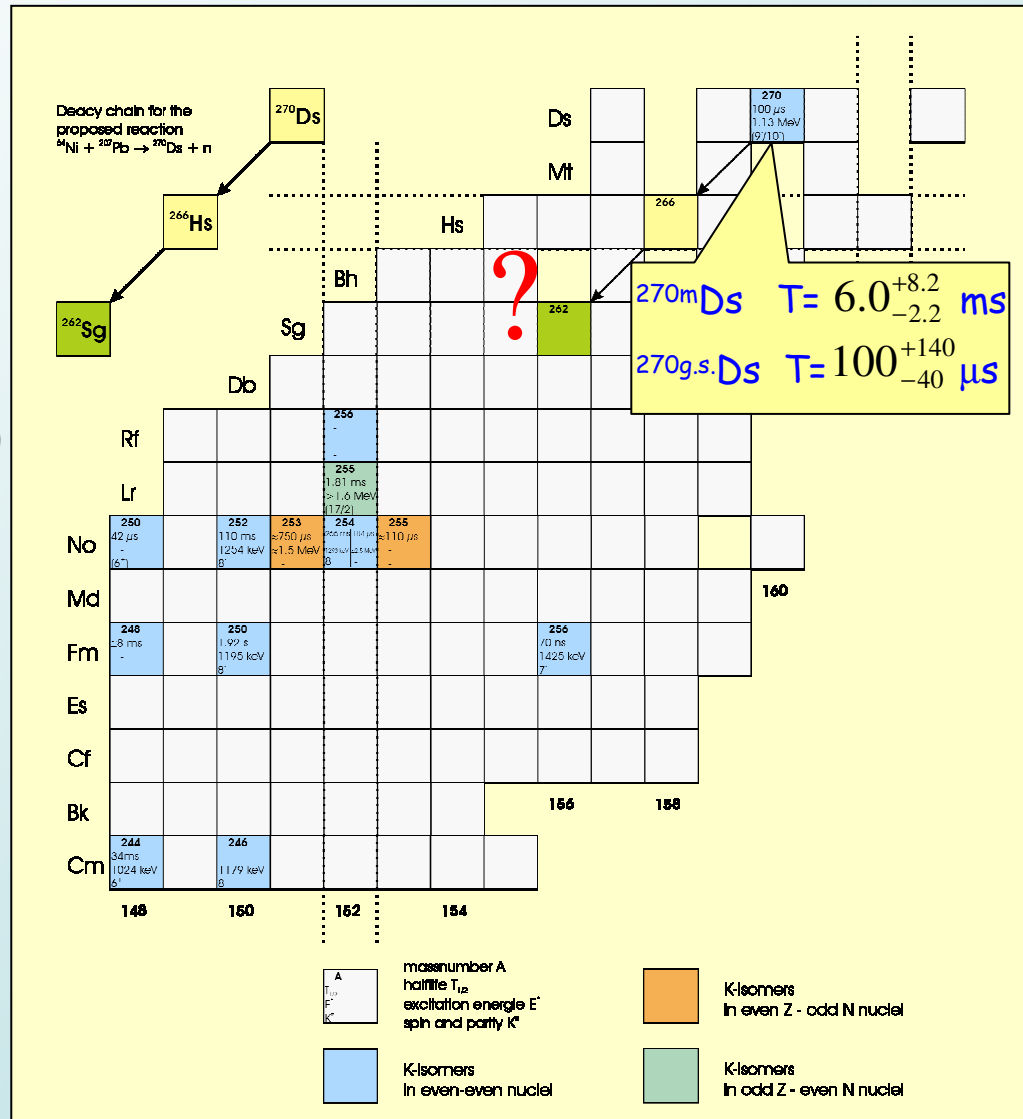
## - Experimental Information

14 cases:

even-even: 11  
 even-odd: 2  
 odd-even: 1

Sg and Hs isotopes?

$T_{1/2}$ : 70 ns ( $^{256}\text{Fm}$ ) - 1.92 s ( $^{250}\text{Fm}$ )  
 $E^*$ : 1-1.5 MeV (2.5 MeV for  $^{254m2}\text{No}$ )



# K-isomers for Z = 96 - 110

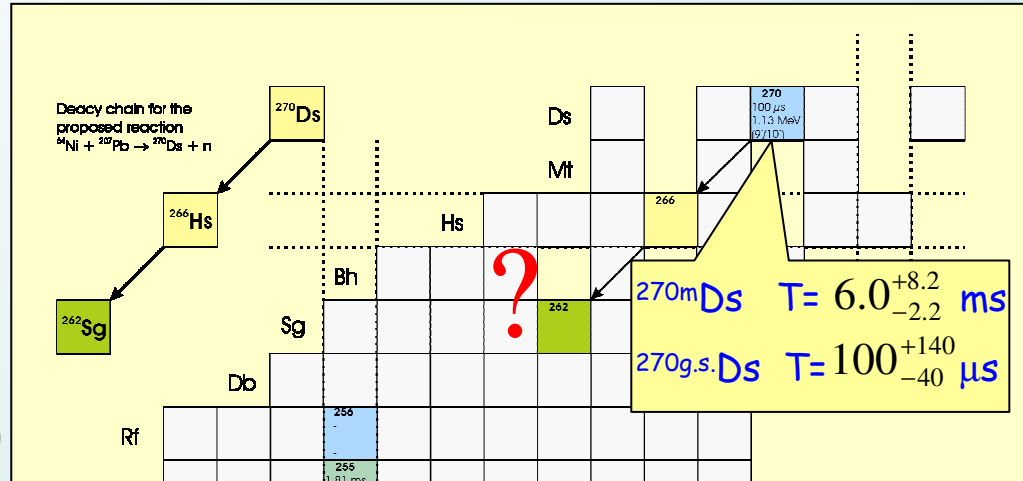
## - Experimental Information

14 cases:

even-even: 11  
 even-odd: 2  
 odd-even: 1

Sg and Hs isotopes?

$T_{1/2}$ : 70 ns ( $^{256}\text{Fm}$ ) - 1.92 s ( $^{250}\text{Fm}$ )  
 $E^*$ : 1-1.5 MeV (2.5 MeV for  $^{254m2}\text{No}$ )



696

R.-D. Herzberg, P.T. Greenlees / Progress in Particle and Nuclear Physics 61 (2008) 674-720

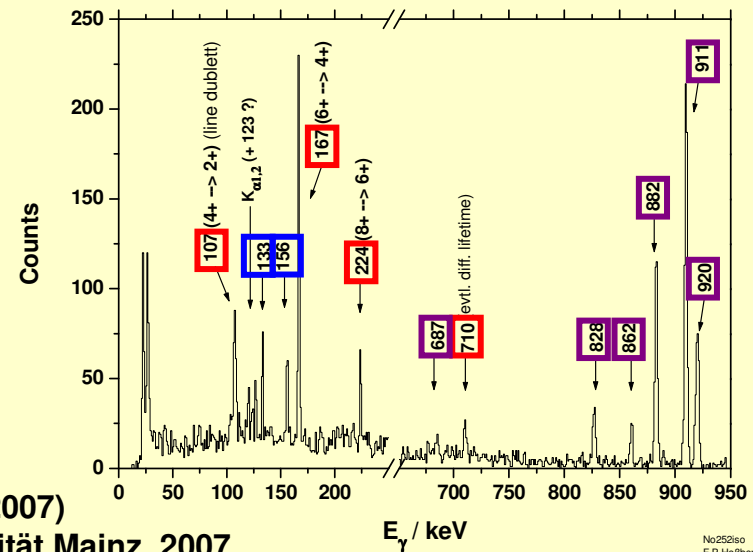
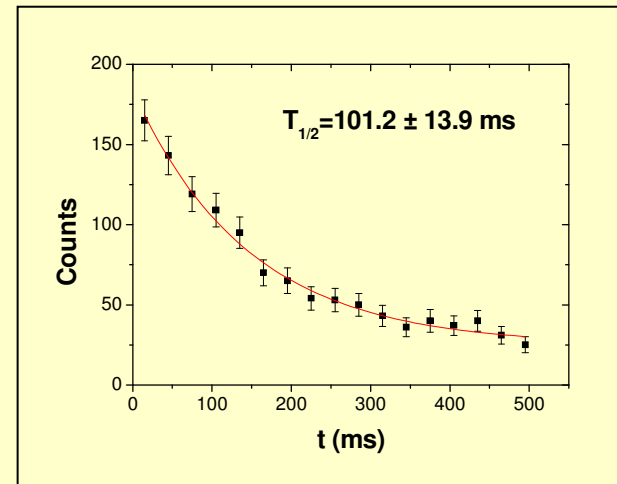
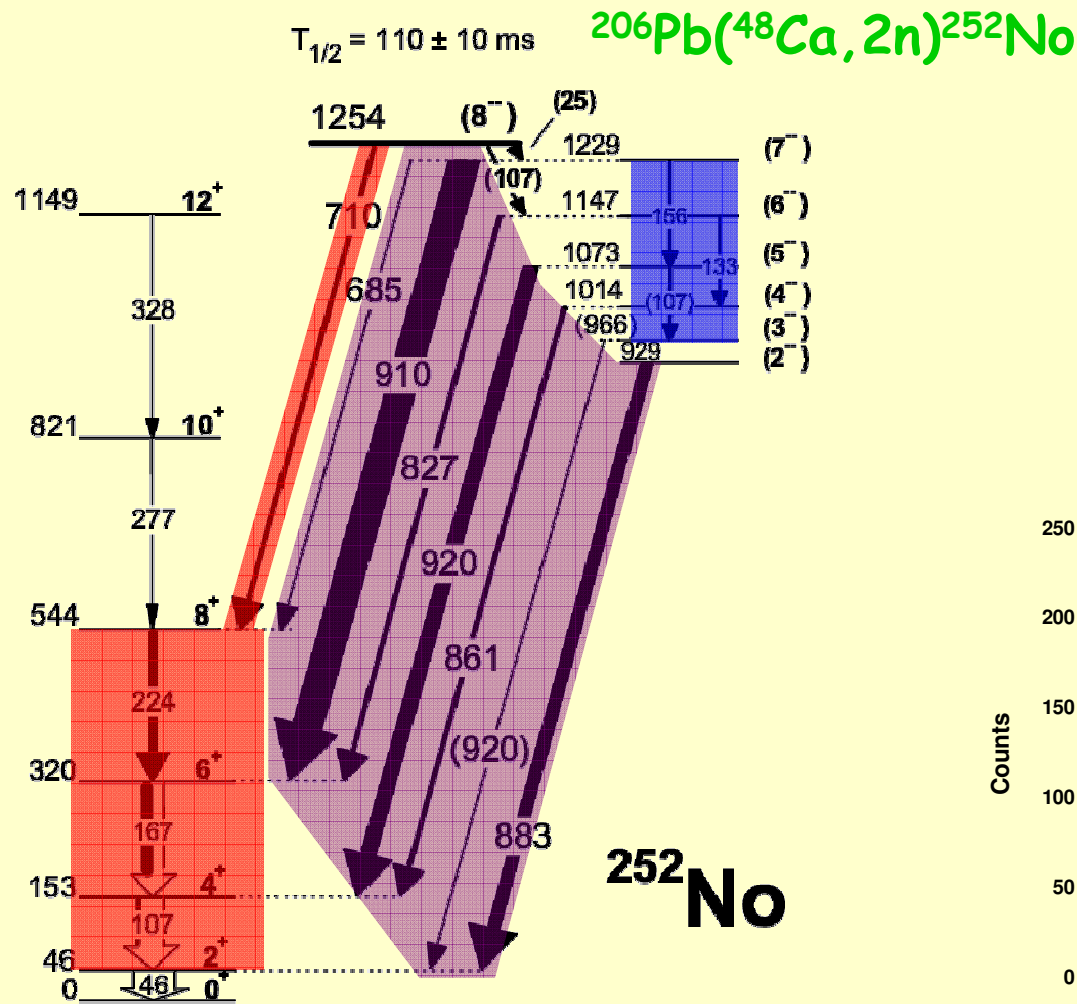
**Table 1**

Table of known K-isomers in even-even nuclei in the heavy and superheavy elements

Nucleus	$K^\pi$	$T_{1/2}$	$E_x$	Decay Mode	Configuration	Reference
$^{244}\text{Cm}$	$6^+$	34 ms	1.040 MeV	$\gamma$	$5/2^+[622]_v \otimes 7/2^+[624]_v$	[135,171]
$^{246}\text{Cm}$	$8^-$	-	1.179 MeV	$\gamma$	$7/2^+[624]_v \otimes 9/2^-[734]_v$	[138]
$^{248}\text{Fm}$	-	$\approx 8$ ms	-	$\gamma$	-	[148]
$^{250}\text{Fm}$	$8^-$	1.92 s	1.195 MeV	$\gamma$	$7/2^+[624]_v \otimes 9/2^-[734]_v$	[82]
$^{256}\text{Fm}$	$7^-$	70 ns	1.425 MeV	$\gamma, \text{SF}$	$7/2^+[633]_\pi \otimes 7/2^-[514]_\pi$	[69]
$^{250}\text{No}$	$(6^+)$	42 $\mu\text{s}$	-	SF, $\gamma$ ?	$(5/2^+[622]_v \otimes 7/2^+[624]_v)$	[118]
$^{252}\text{No}$	$8^-$	110 ms	1.254 MeV	$\gamma$	$7/2^+[624]_v \otimes 9/2^-[734]_v$	[169]
$^{254}\text{No}$	$8^-$	266 ms	1.293 MeV	$\gamma$	$7/2^-[514]_\pi \otimes 9/2^+[624]_\pi$	[77,78]
$^{254}\text{No}$	-	184 $\mu\text{s}$	$\approx 2.5$ MeV	$\gamma$	-	[77,78]
$^{270}\text{Ds}$	$9^-, 10^-$	6 ms	$\approx 1.13$ MeV	$\alpha$	$11/2^-[725]_v \otimes 7/2^+[613]_v$ $11/2^-[725]_v \otimes 9/2^+[615]_v$	[22]

In some cases the  $K^\pi$  or configuration assignments are tentative and have not been made on the basis of unambiguous experimental data. See relevant references for details.

# Nuclear Structure of the Heaviest Nuclei: Isomeric states – $^{252}\text{No}$ (Ph.D. Thesis B. Sulignano)



B. Sulignano et al. EPJ A33, 327 (2007)

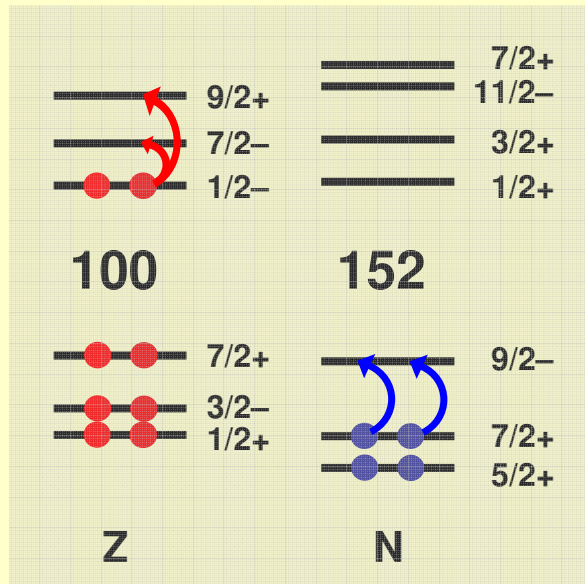
B. Sulignano, PHD thesis, Universität Mainz, 2007



# Nuclear Structure of the Heaviest Nuclei: – $^{252}\text{No}$ Hartree Fock Bogolyubov/Gogny D1S

4+, 5-, 8-

8-



$^{252}\text{No}$

$E^*$  [MeV]

2.0

theory

experiment

1.5

1450  $\nu 7^-$

1300  $\pi 7^-$

1254  $8^-$

1.0

1070  $\nu 8^-$

929  $2^-$

0.5

0.0

$^{252}\text{No}$

**2-quasineutron state**

$$\{\nu[624]_{7/2+} \otimes \nu[734]_{9/2-}\} 8^-$$

$$\beta_2 = 0.25$$

J.P. Delaroche et al., Nucl. Phys. A 771, 103 (2006)

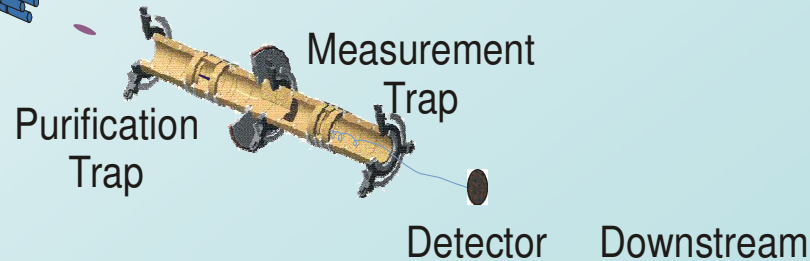
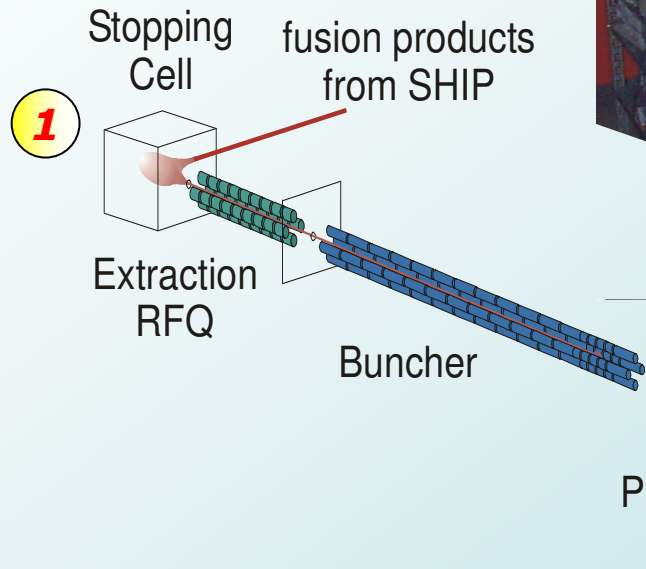
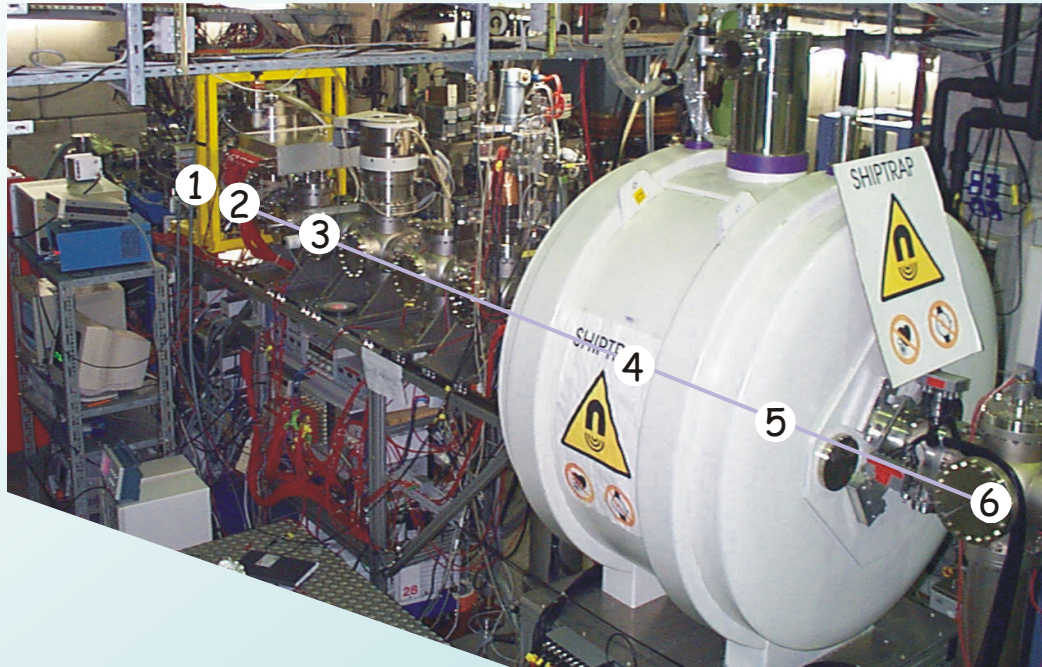
# Additional Methods

## Outline

1. Introduction
2. Reaction Mechanism of Heavy Ion Collisions at the Coulomb Barrier
3. Synthesis and Investigation of Superheavy Nuclei
4. Nuclear Structure of Heavy and Superheavy Nuclei
5. **Additional Methods**
  - Precision mass measurements
  - Chemistry

# SHIPTRAP

## 1. deceleration

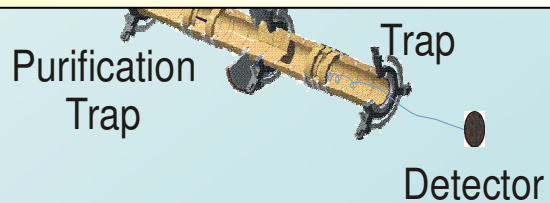
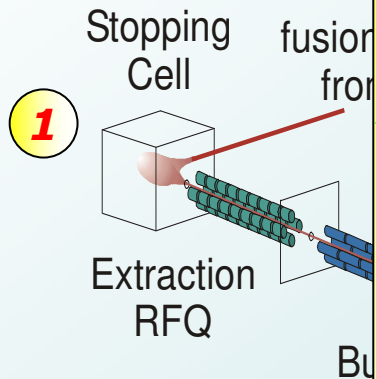
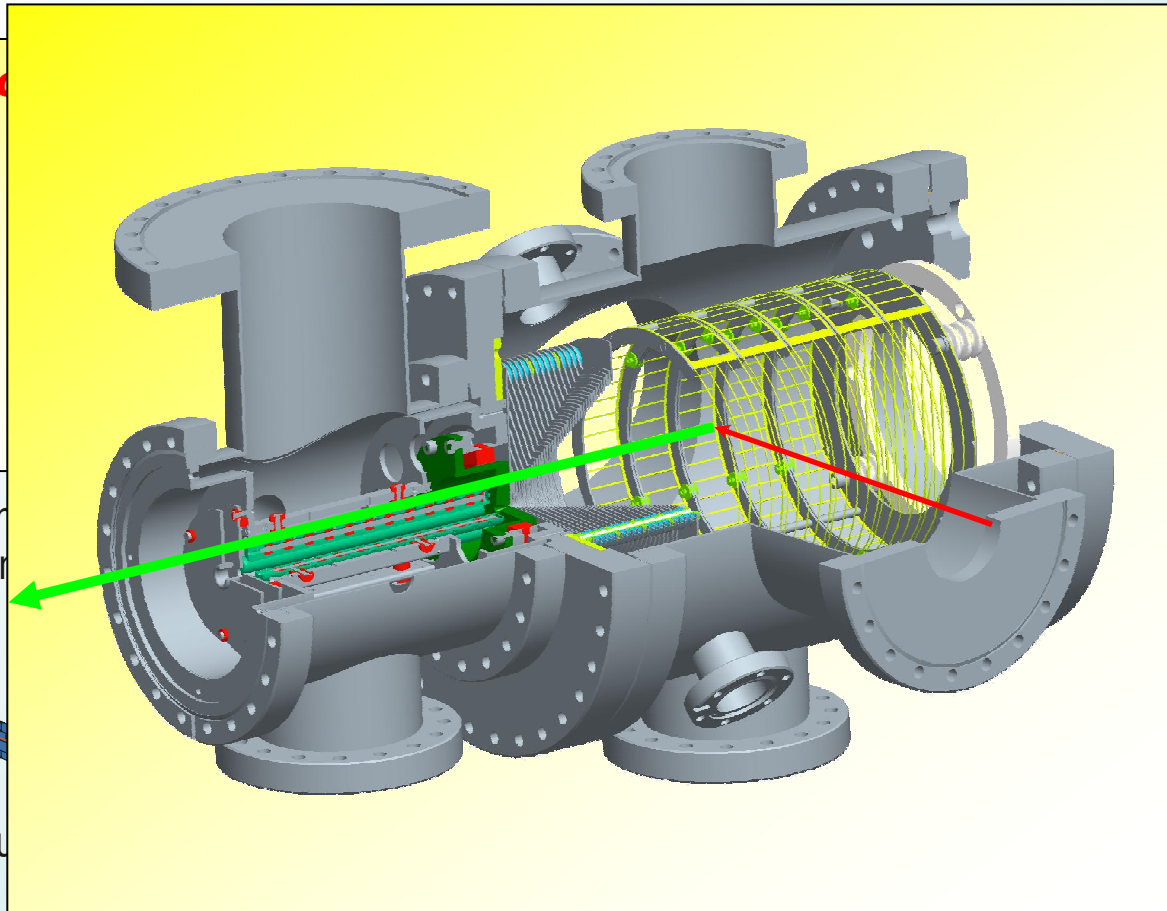


Downstream Experiments  
July 3<sup>rd</sup> 2009



# SHIPTRAP

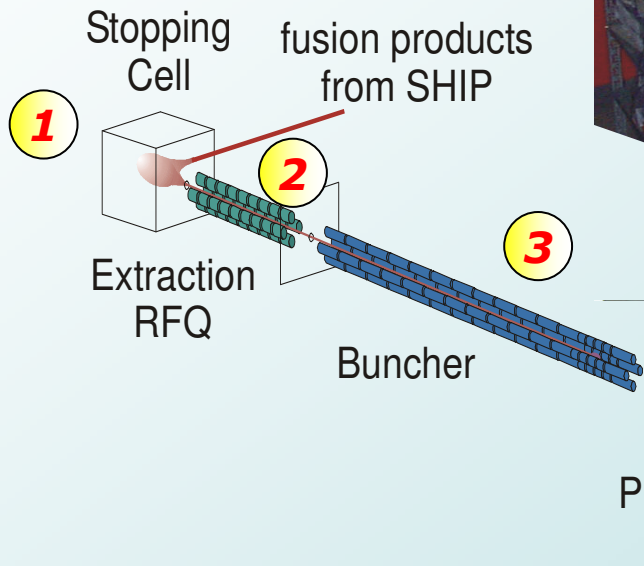
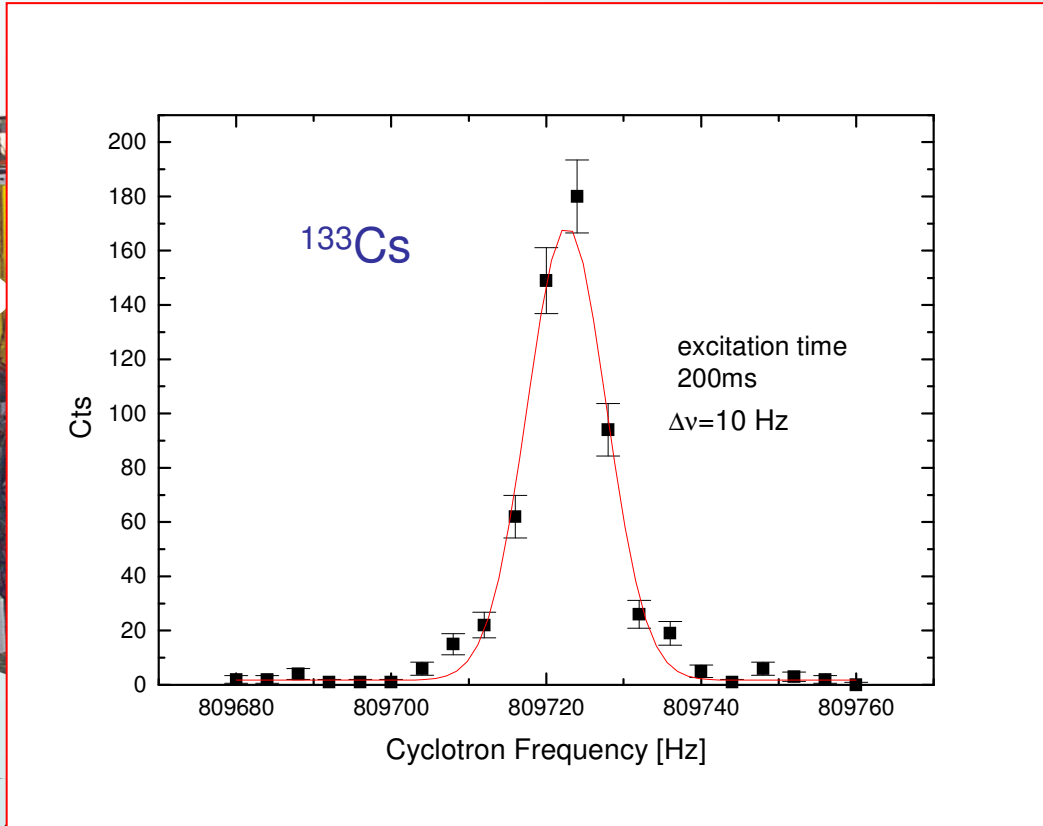
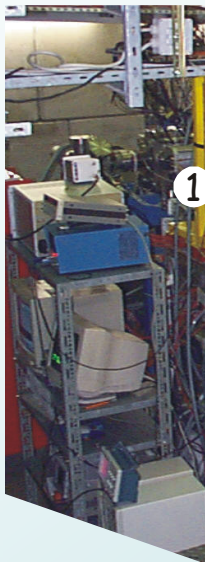
## 1. deceleration



Downstream Experiments  
July 3<sup>rd</sup> 2009

# SHIPTRAP

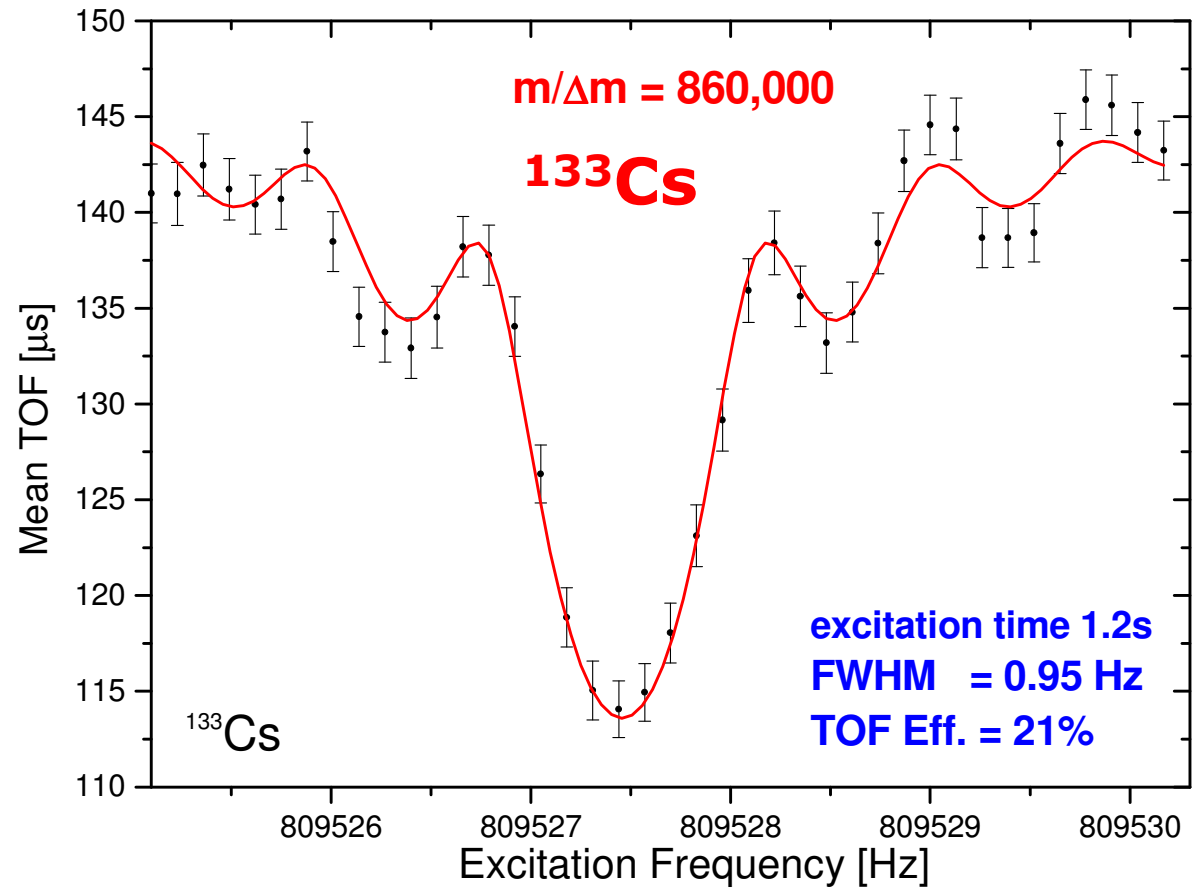
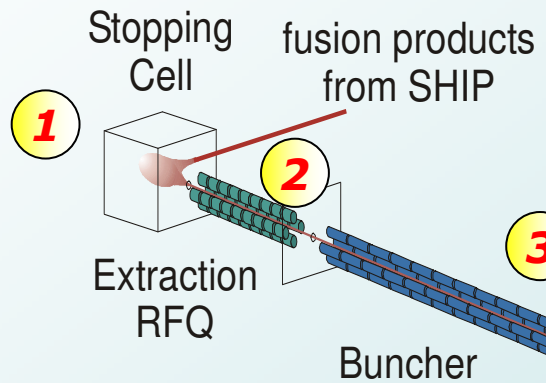
1. deceleration
2. cooling
3. accumulation
4. purification





# SHIPTRAP

1. deceleration
2. cooling
3. accumulation
4. purification
5. storage
6. detection...

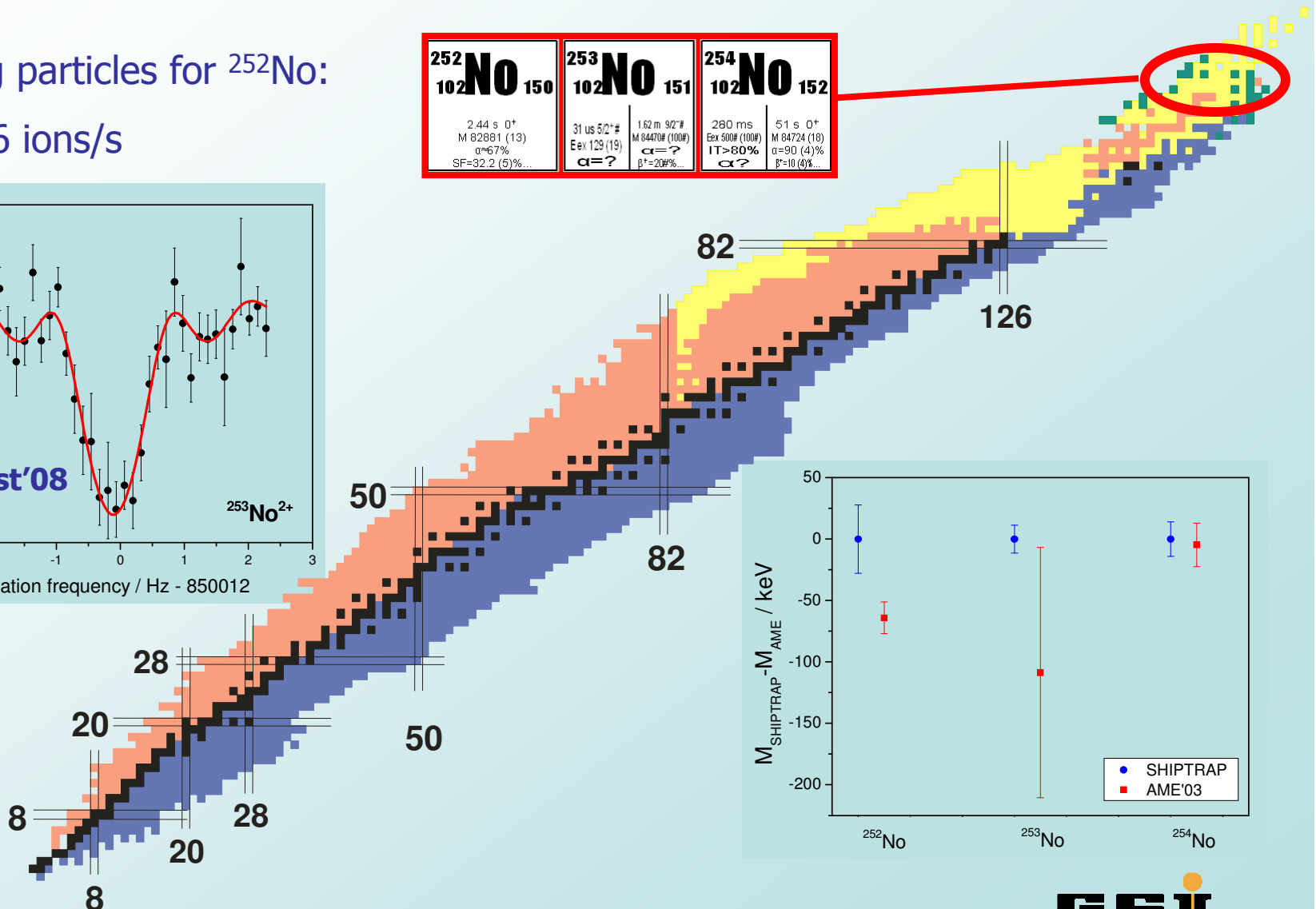
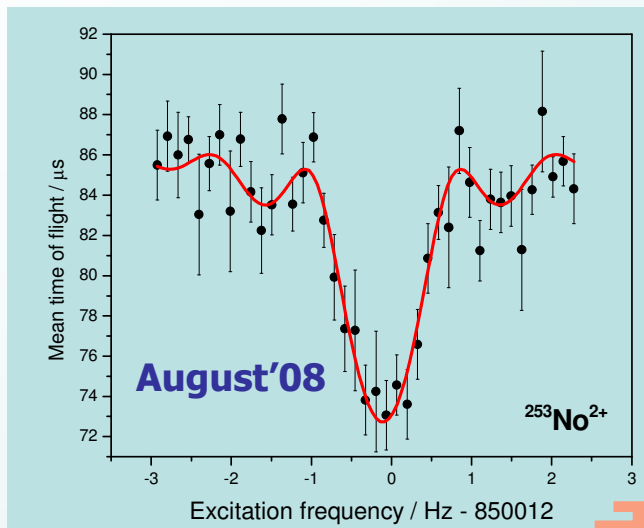


Detector Downstream Experiments

# First direct mass measurements of $^{252-254}\text{No}$ @ SHIPTRAP

Incoming particles for  $^{252}\text{No}$ :  
only  $\sim 0.6$  ions/s

$^{252}\text{No}$ 102 <b>No</b> 150	$^{253}\text{No}$ 102 <b>No</b> 151	$^{254}\text{No}$ 102 <b>No</b> 152
2.44 s $0^+$ M 82881 (13) $\alpha=67\%$ SF=32.2 (5)%...	31 $\mu\text{s}$ $5/2^+$ # Eex 129 (19) $\alpha=?$	1.62 m $9/2^+$ # M 84470# (100#) $\alpha=?$ $\beta^+=20\%$ ...
	280 ms Eex 500# (100#) IT>80%	51 s $0^+$ M 84724 (18) $\alpha=90$ (4)% $\beta^+=10$ (4)%...



# Periodic Table of the Elements: , forms Hs a gaseous molecule with oxygen?

1 H																	2 He				
3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne				
11 Na	12 Mg	3	4	5	6	7	8	9	10	11	12	13 Al	14 Si	15 P	16 S	17 Cl	18 Ar				
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr				
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe				
55 Cs	56 Ba	57 La	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn				
87 Fr	88 Ra	89 Ac	104 Rf	105 Db	106 Sg	107 Bh	108 Hs					112									
								109 Mt	110 Ds	111 Rg					113	114	115	116			118

Lanthanides

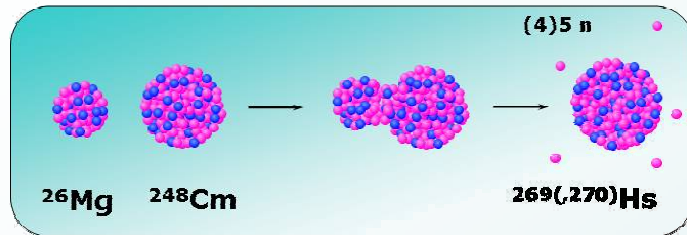
58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu
----------	----------	----------	----------	----------	----------	----------	----------	----------	----------	----------	----------	----------	----------

Actinides

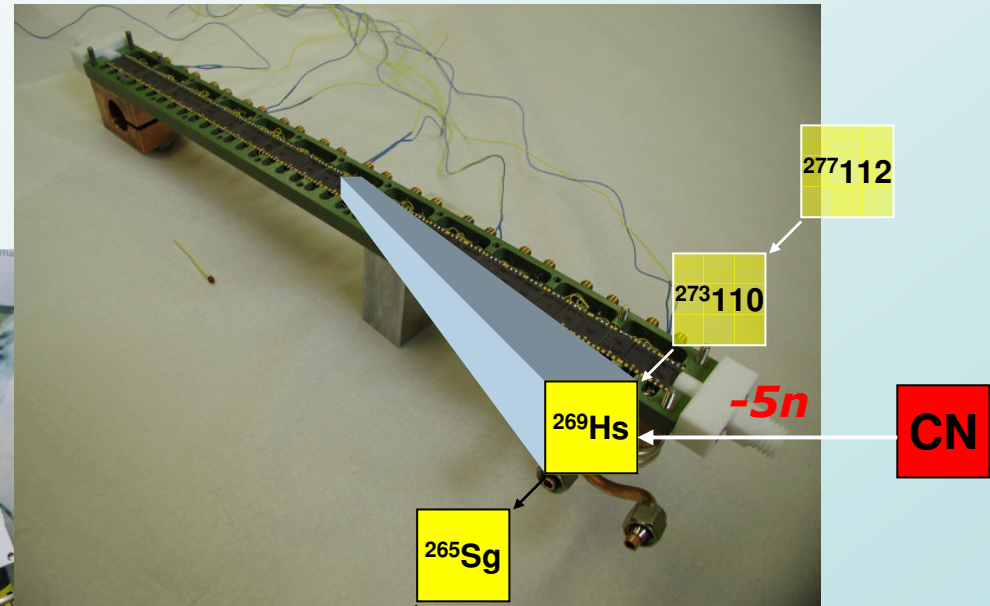
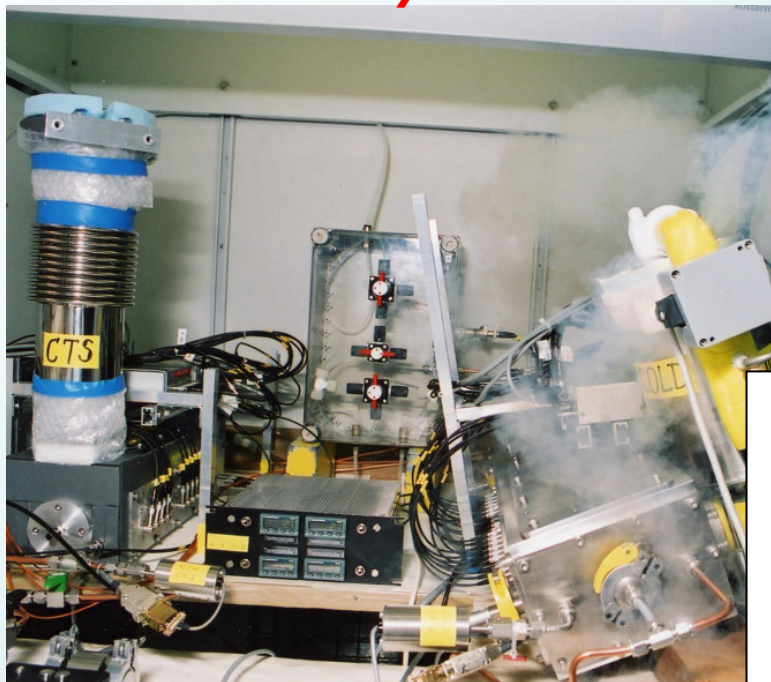
90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr
----------	----------	---------	----------	----------	----------	----------	----------	----------	----------	-----------	-----------	-----------	-----------

(courtesy of A. Türler, H. Gäggeler, M. Schädel et al.)

# Chemistry of Hassium - Thermochromatography



**+ chemistry**

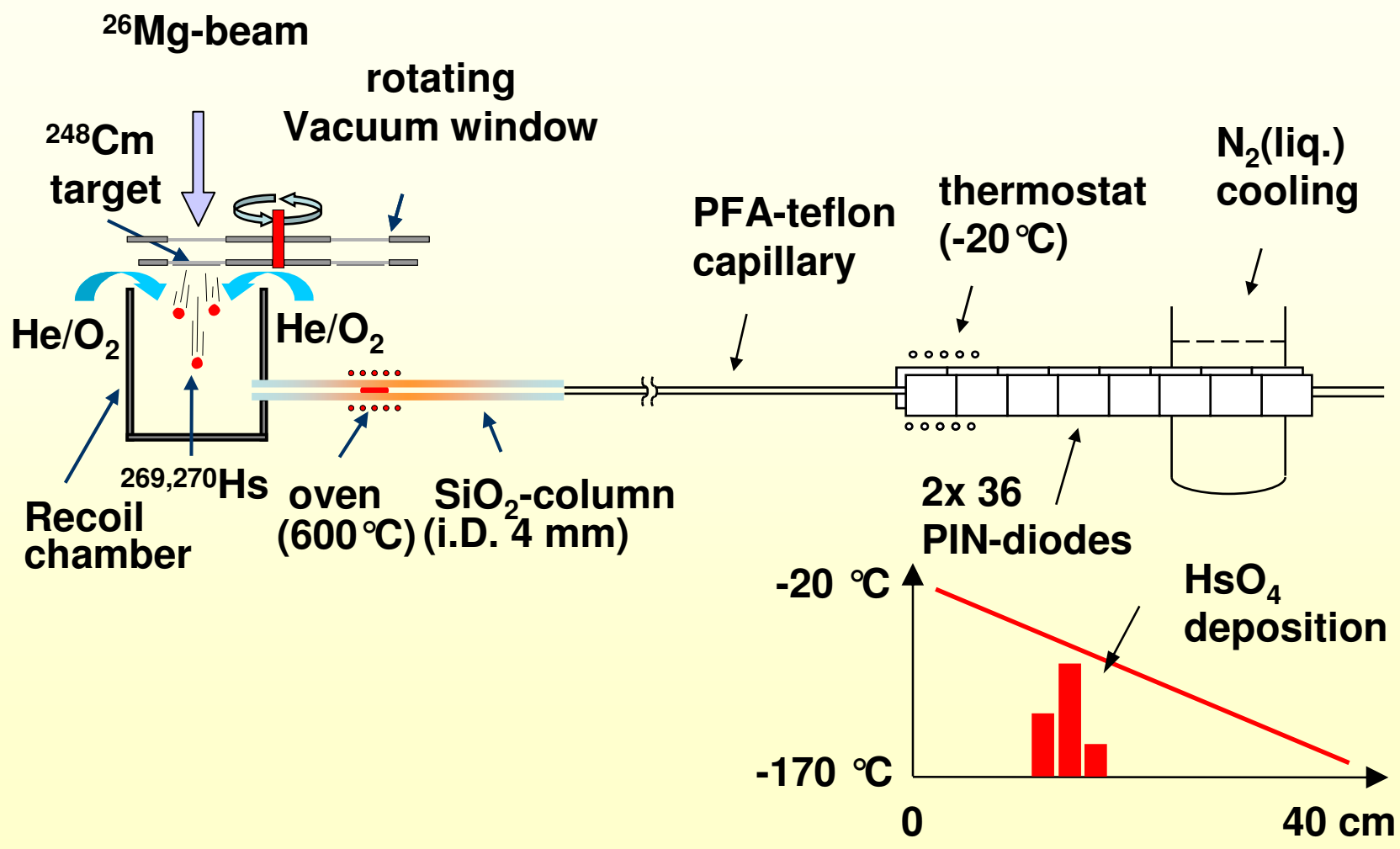


**3 events for  $^{269}\text{Hs}$   
(2 events for  $^{270}\text{Hs}$ ) confirm the SHIP-data**

**determination of the chemical Properties of Hassium**

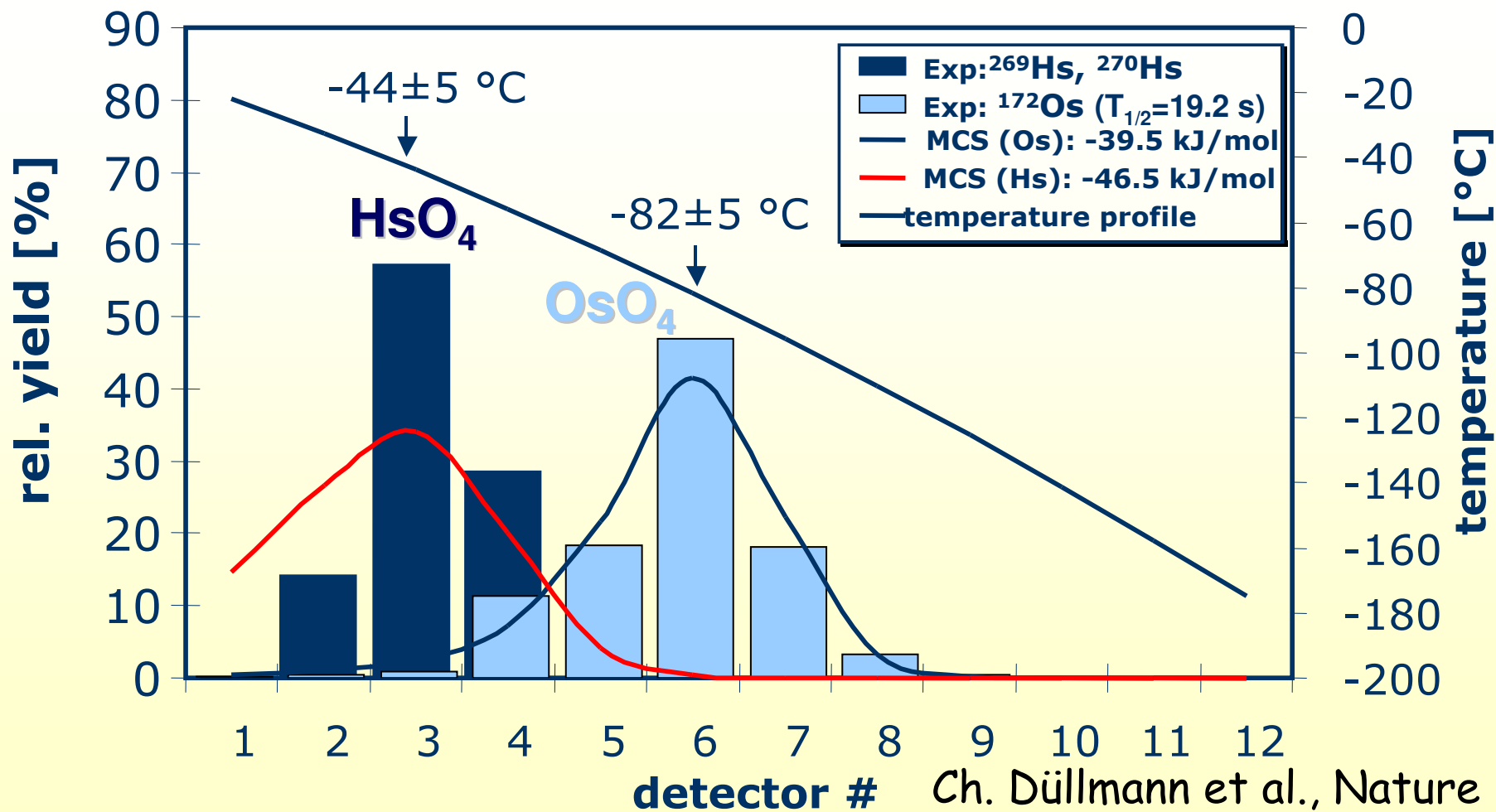
Dieter Ackermann

# In-Situ Volatilization and On-line detection - IVO





# Thermochromatography of $\text{OsO}_4$ and $\text{HsO}_4$



# Periodic Table of the Elements: is E112 like Hg?

1 H																	2 He				
3 Li	4 Be											5 B	6 C	7 N	8 O	9 F	10 Ne				
11 Na	12 Mg	3 Sc	4 Ti	5 V	6 Cr	7 Mn	8 Fe	9 Co	10 Ni	11 Cu	12 Zn	13 Al	14 Si	15 P	16 S	17 Cl	18 Ar				
19 K	20 Ca	21 Sc	22 Ti	23 V	24 Cr	25 Mn	26 Fe	27 Co	28 Ni	29 Cu	30 Zn	31 Ga	32 Ge	33 As	34 Se	35 Br	36 Kr				
37 Rb	38 Sr	39 Y	40 Zr	41 Nb	42 Mo	43 Tc	44 Ru	45 Rh	46 Pd	47 Ag	48 Cd	49 In	50 Sn	51 Sb	52 Te	53 I	54 Xe				
55 Cs	56 Ba	57 La	72 Hf	73 Ta	74 W	75 Re	76 Os	77 Ir	78 Pt	79 Au	80 Hg	81 Tl	82 Pb	83 Bi	84 Po	85 At	86 Rn				
87 Fr	88 Ra	89 Ac	104 Rf	105 Db	106 Sg	107 Bh	108 Hs					112									
								109 Mt	110 Ds	111 Rg					113	114	115	116			118

Lanthanides

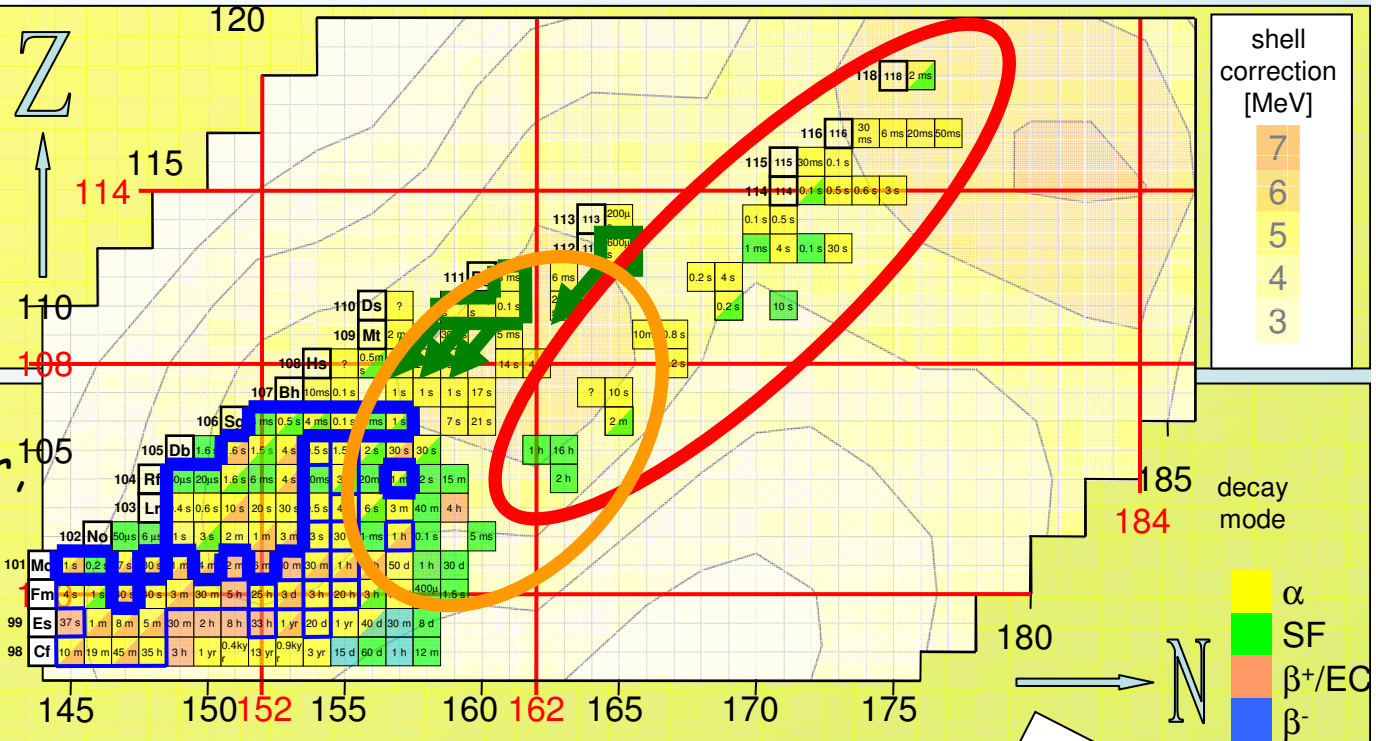
Actinides

58 Ce	59 Pr	60 Nd	61 Pm	62 Sm	63 Eu	64 Gd	65 Tb	66 Dy	67 Ho	68 Er	69 Tm	70 Yb	71 Lu
90 Th	91 Pa	92 U	93 Np	94 Pu	95 Am	96 Cm	97 Bk	98 Cf	99 Es	100 Fm	101 Md	102 No	103 Lr

# SHE Synthesis and Nuclear Structure of SHE

## - Roadmap/Long Term

- cold fusion at SHIP
- hot fusion at FLNR
- spectroscopy from transactinides to SHE



- reaction mechanism systematics (transfer, incomplete fusion, spin distribution, ...)
- **efficiency upgrade**
- mass measurement /determination
- employment of **all** available technology and methods (ER- $\alpha$ - $\gamma$  correlations, chemistry, traps, mass determination)

- "rare isotopes"? - **yes** for systematic investigations
  - **maybe(???)** for SHE synthesis (low beam intensity!!!)
- **localisation of the region of spherical shell-stabilized SHE**



*The End*

*The End*

